

Homework 4, 2024 Individual

(1) 9.2.36 (d,e)

(d) True. If L_1, L_2 are Duck-decidable,

then $L_1 = \sum^{k_1} \cup \dots \cup \sum^{k_m}$ and

$L_2 = \sum^{k'_1} \cup \dots \cup \sum^{k'_m}$. Hence

$$L_1 \setminus L_2 = \bigcup_{k \in K} \sum^k \quad \text{where } K = \{k_1, \dots, k_m\} \setminus \{k'_1, \dots, k'_m\}$$

so K is a finite subset of $\mathbb{Z}_{\geq 0}$. Hence

$L_1 \setminus L_2$ is Duck recognizable.

(e) False. If $L_1 = \{a\}$ and $L_2 = \sum_{ASCI_{\downarrow}} \{a\}$

then $L_1, L_2 \subset \sum_{ASCI_{\downarrow}}^1$ but L_1, L_2 are not all

of $\sum_{ASCI_{\downarrow}}^1$. Hence L_1, L_2 are Duck

undecidable. But $L_1 \cup L_2 = \Sigma_{ASCII}^*$,
which is Decidable.

(2) 9.2.37. No: $L = \text{ACCEPTANCE}$ and
 $\text{ACCEPTANCE}_{\text{Comp}}$ are both undecidable,
but $L = \text{ACCEPTANCE}$ is recognizable.