

9.1

$f(x,y)$  derivative

$$\frac{\partial f}{\partial x} = \lim_{\delta x \rightarrow 0} \frac{f(x+\delta x, y) - f(x, y)}{\delta x}$$

continuous  $f(x,y)$

numerical

$$\frac{\partial f}{\partial x} \approx \frac{f(x+1, y) - f(x, y)}{\Delta x = 1}$$

correlation kernel  $[-1 \ 1]$

$$f(x,y) * [-1 \ 1] \approx \frac{\partial f}{\partial x}$$

centered  $[-1 \ 0 \ 1]$  ← no shift

$$[-1 \ 1] \text{ or } \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

9.2

I

1	1	0.6	0.3	0	0
1	1	0.6	0.3	0	0
0	0	0	0	0	0
0	0	0	0	0	0

$\frac{\partial I}{\partial x} \quad [-1 \ 1]$

0	-0.4	-0.3	-0.3	0	0
0	-0.4	-0.3	-0.3	0	0
0	0	0	0	0	0
0	0	0	0	0	0

$\frac{\partial I}{\partial y} \quad \begin{bmatrix} 1 \\ -1 \end{bmatrix}$

0	0	0	0	0	0
1	1	0.6	0.3	0	0
0	0	0	0	0	0

Forward diff

$$f(x+1, y) - f(x, y)$$

$$\begin{bmatrix} \vdots & & \\ -1 & & 1 \\ \vdots & & \end{bmatrix}$$

Backward diff

$$f(x, y) - f(x-1, y)$$

$$\begin{bmatrix} -1 & & \\ & 1 & \\ & & \end{bmatrix}$$

centred diff

$$\frac{1}{2}(f(x+1, y) - f(x-1, y))$$

$$\begin{bmatrix} -1 & 0 & 1 \end{bmatrix} \frac{1}{2}$$

$\Delta x = 2$

Sobel

$$\begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}$$

