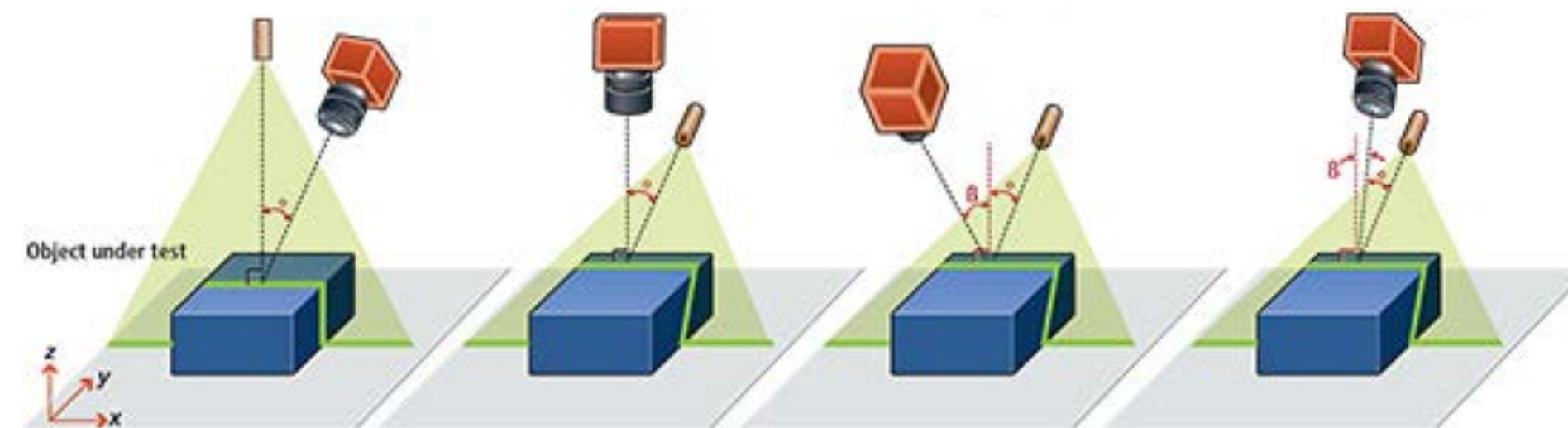


CPSC 425: Computer Vision



Lecture 2: Image Formation

(slide credits / thanks to **Bob Woodham, Jim Little** and **Fred Tung**)

This Lecture

Topics: Image Formation

- Image Formation
- Cameras and Lenses
- Projection

Readings:

- **Today's** Lecture: Szeliski Chapter 2, Forsyth & Ponce (2nd ed.) 1.1.1 — 1.1.3
- **Next** Lecture: Forsyth & Ponce (2nd ed.) 4.1, 4.5

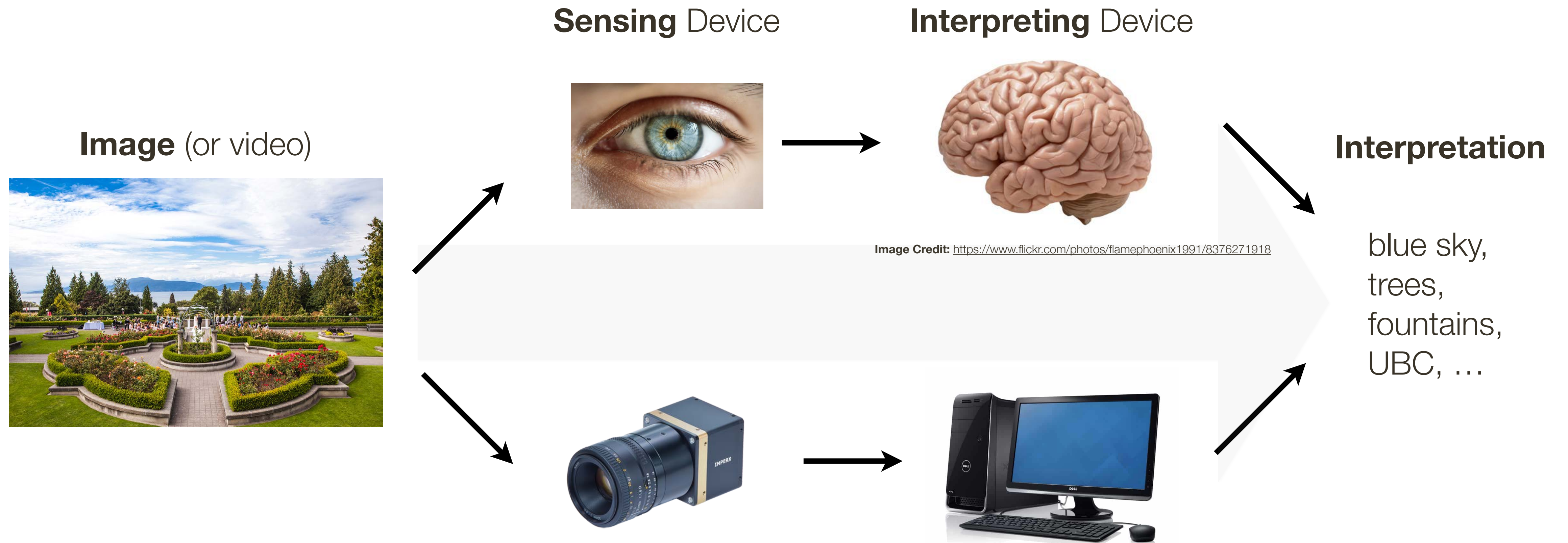
Lecture 2: Goal

To understand how images are formed

(and develop relevant mathematical
concepts and abstractions)

What is **Computer Vision**?

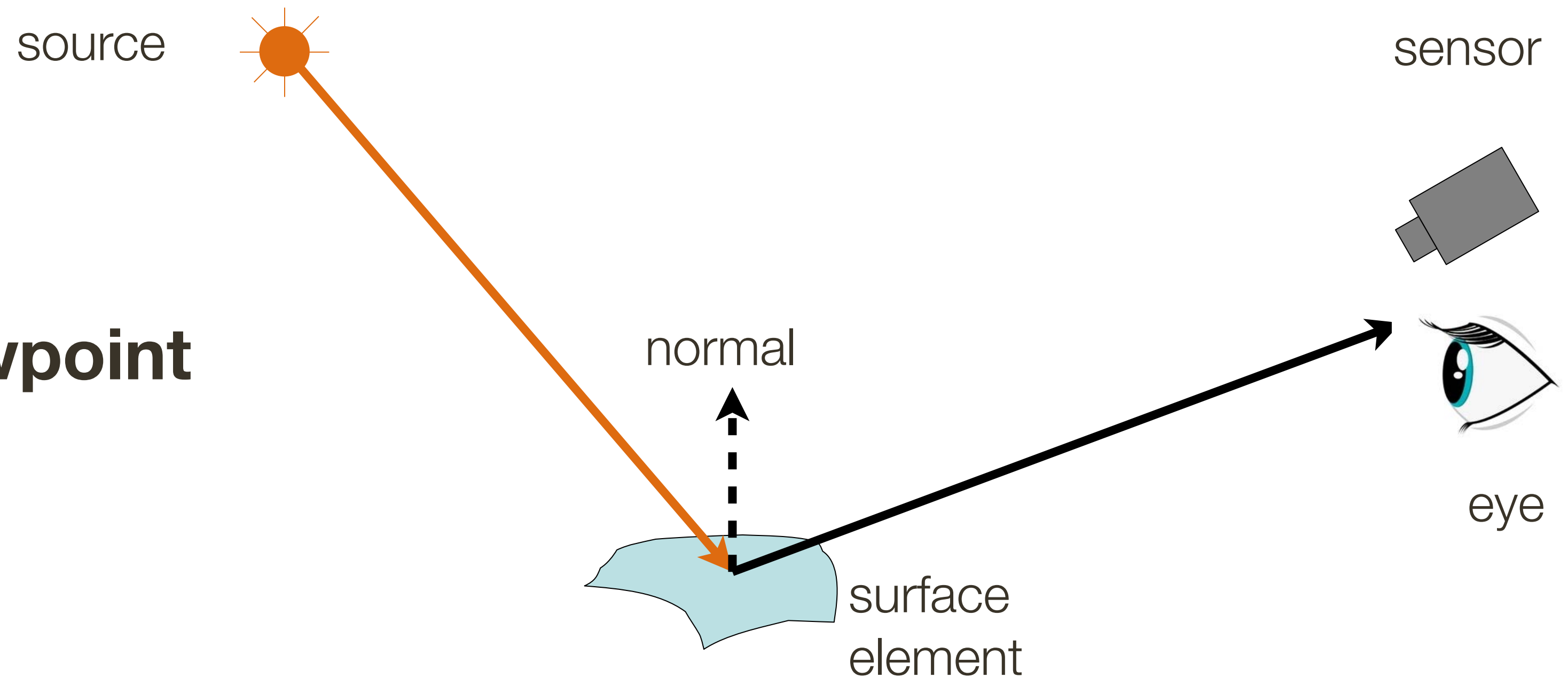
Computer vision, broadly speaking, is a research field aimed to enable computers to **process and interpret visual data**, as sighted humans can.



Overview: Image Formation, Cameras and Lenses

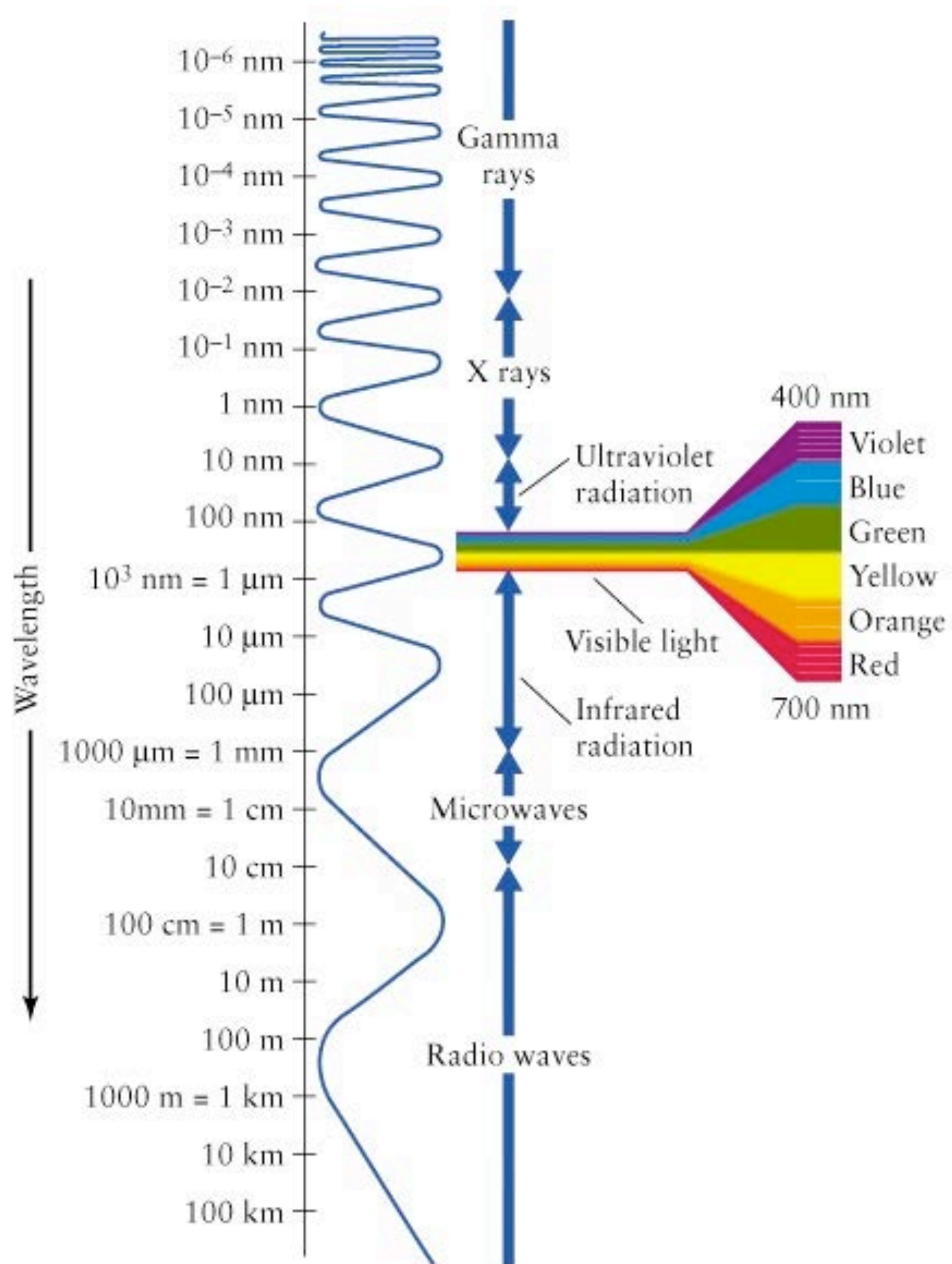
The **image formation process** that produces a particular image depends on

- **Lighting** condition
- Scene **geometry**
- **Surface** properties
- Camera **optics** and **viewpoint**



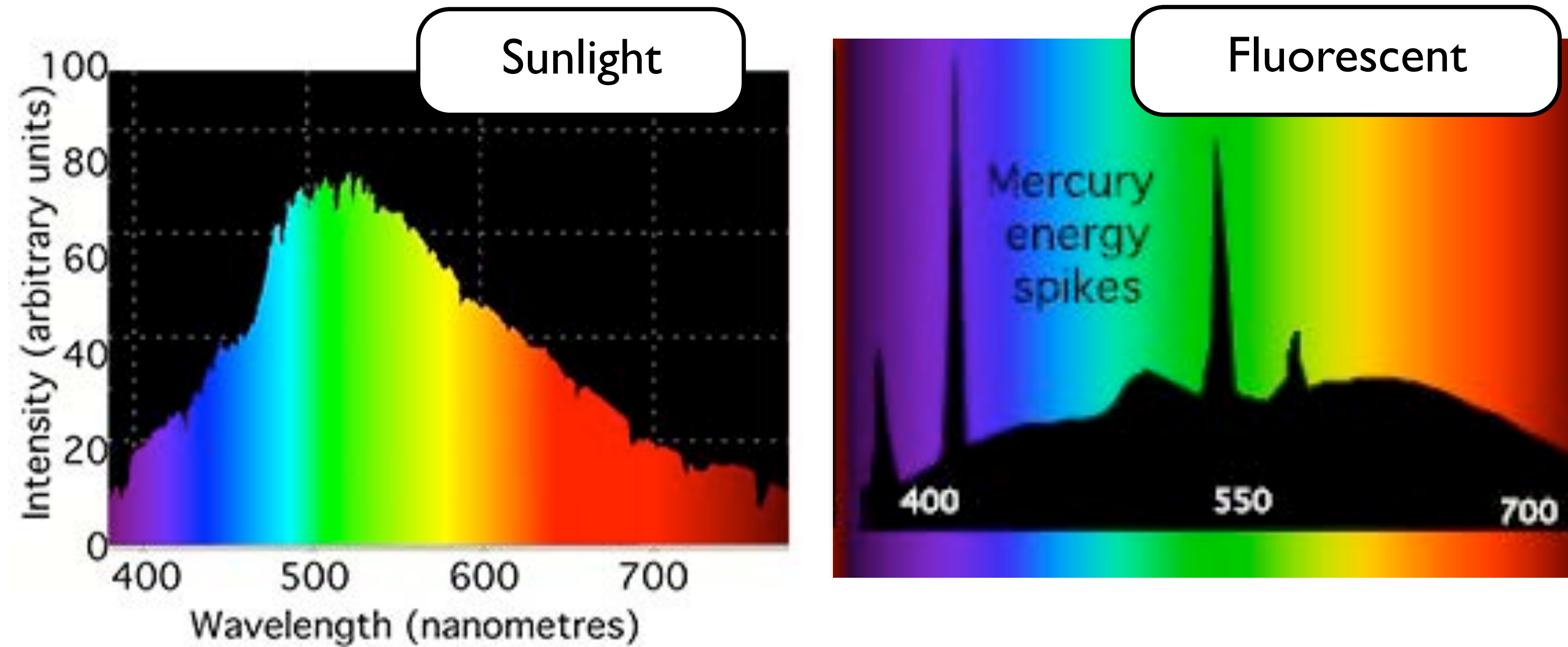
Sensor (or eye) **captures amount of light** reflected from the object

Light and Color



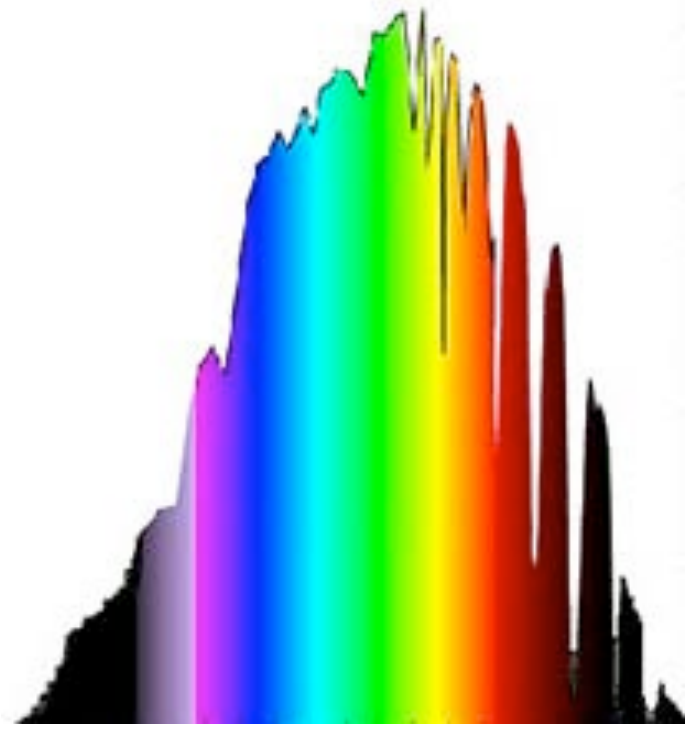
- Light is electromagnetic radiation in the 400-700nm band
- This is the peak in the spectrum of sunlight passing through the atmosphere
- Newton's Prism experiment showed that white light is composed of all frequencies
- Black is the absence of light!

Spectral Power Distribution

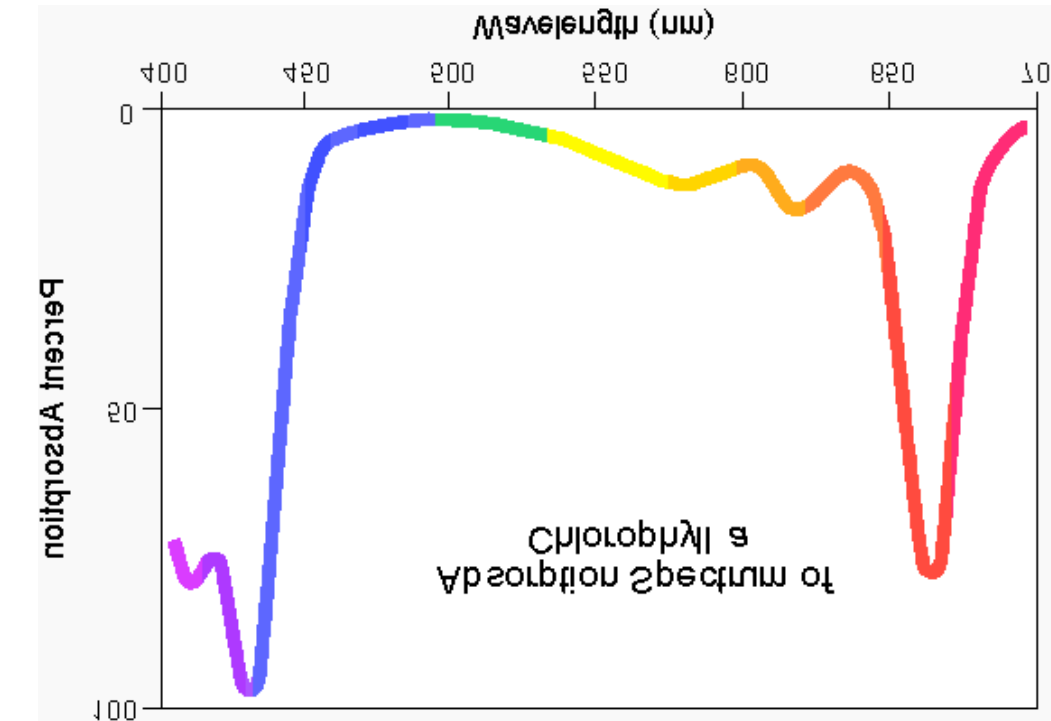
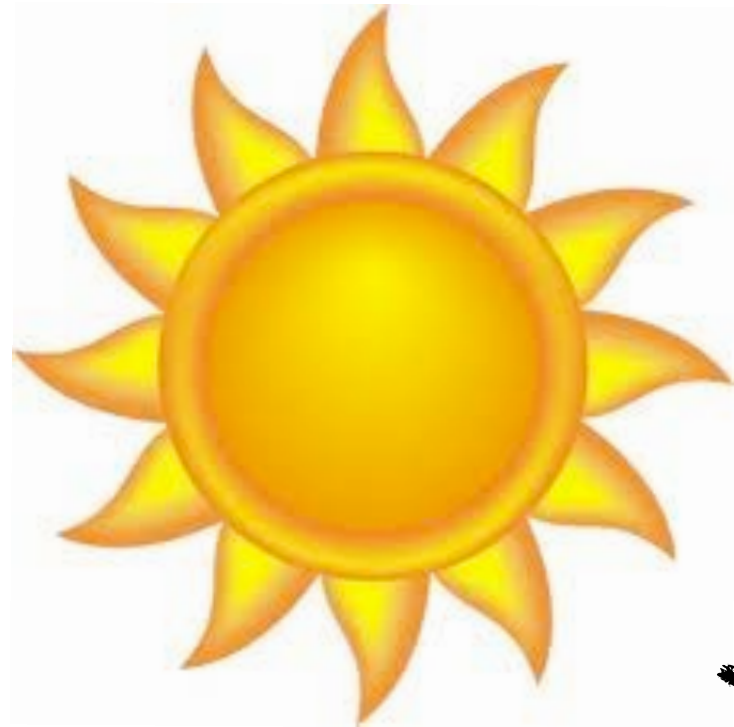


- The spectral distribution of energy in a light ray determines its colour
- Surfaces reflect light energy according to a spectral distribution as well
- The combination of incident spectra and reflectance spectra determines the light colour

Spectral Reflectance Example



$$E(\lambda)$$



$$S(\lambda)$$



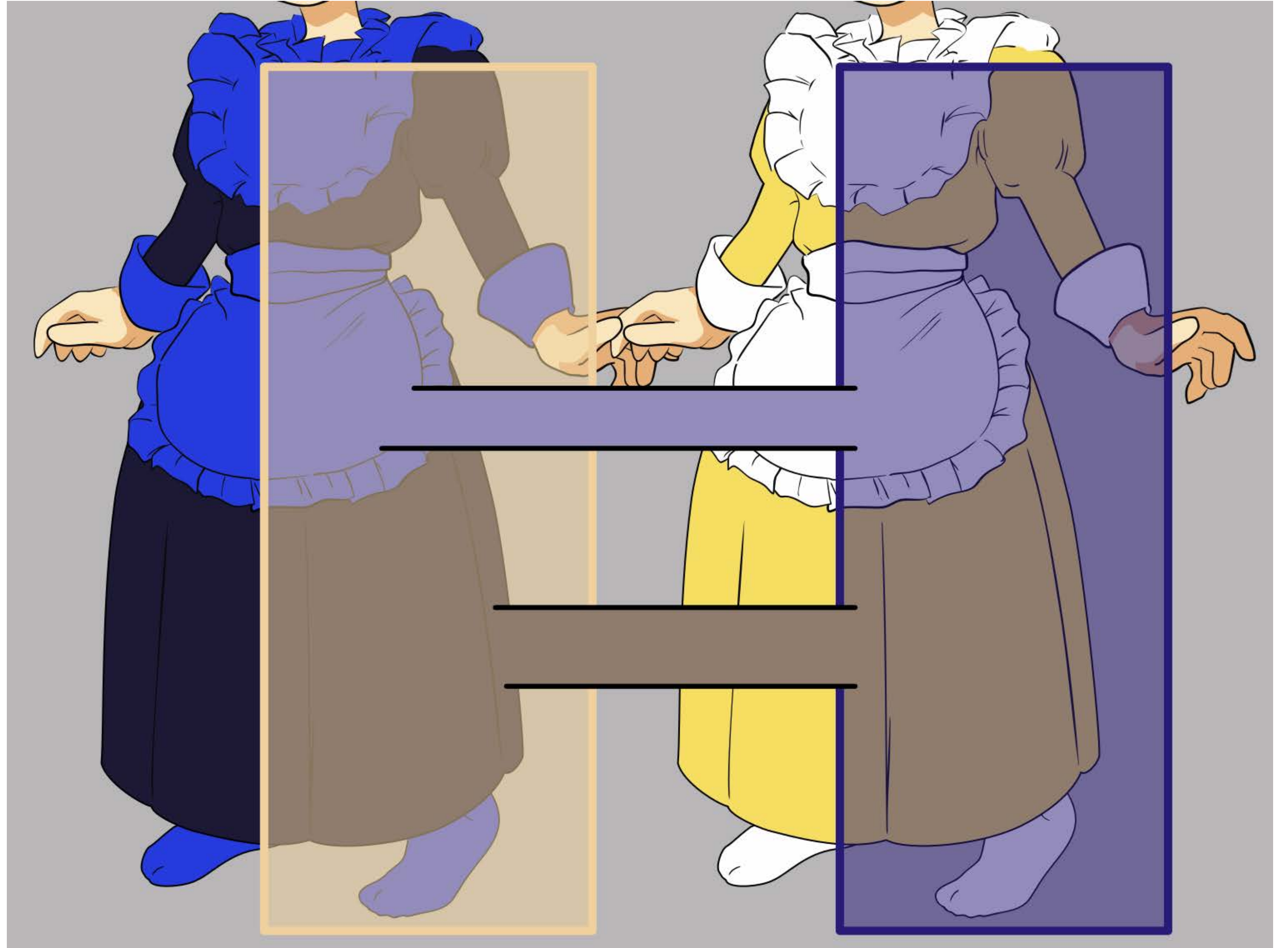
$$E(\lambda)S(\lambda)$$



Our brains already knows this



Our brains already knows this



Surface Reflectance

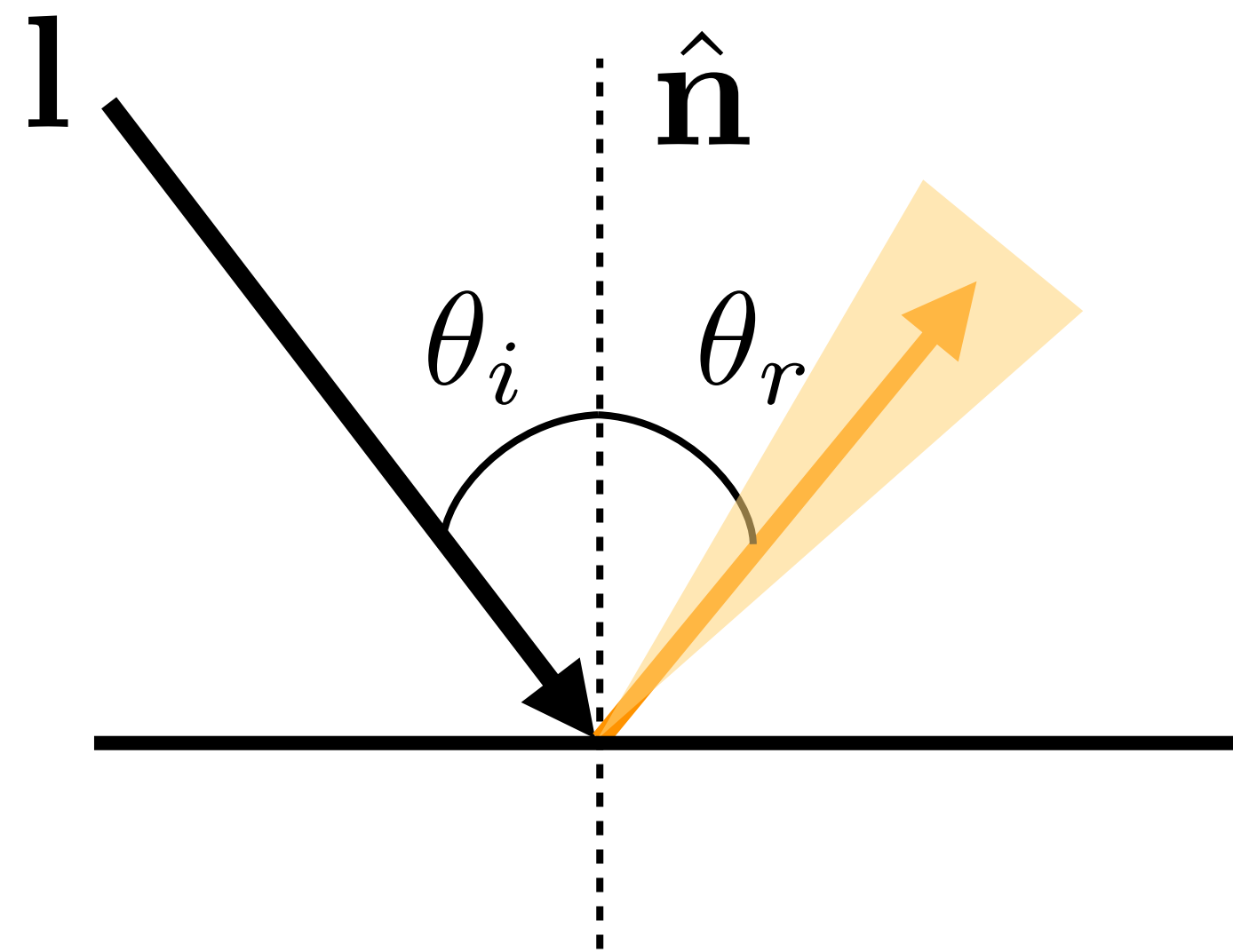
- Reflected intensity also depends on geometry: surface orientation, viewer position, shadows, etc.



It also depends on surface properties, e.g., diffuse or specular

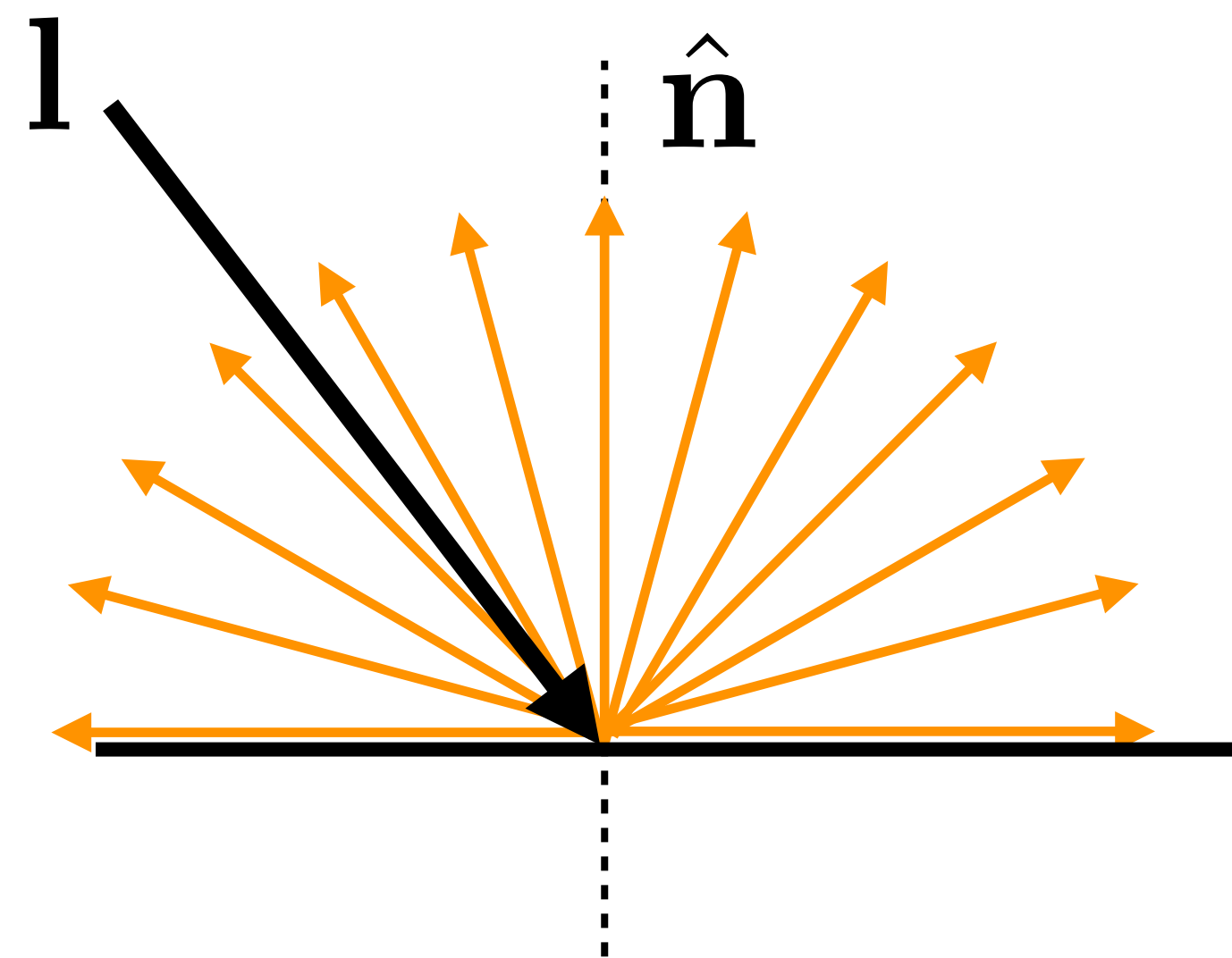
Diffuse and Specular Reflection

- A pure mirror reflects light along a line symmetrical about the surface normal
- A pure diffuse surface scatters light equally in all directions



Pure Mirror Reflection

$$\theta_i = \theta_r$$



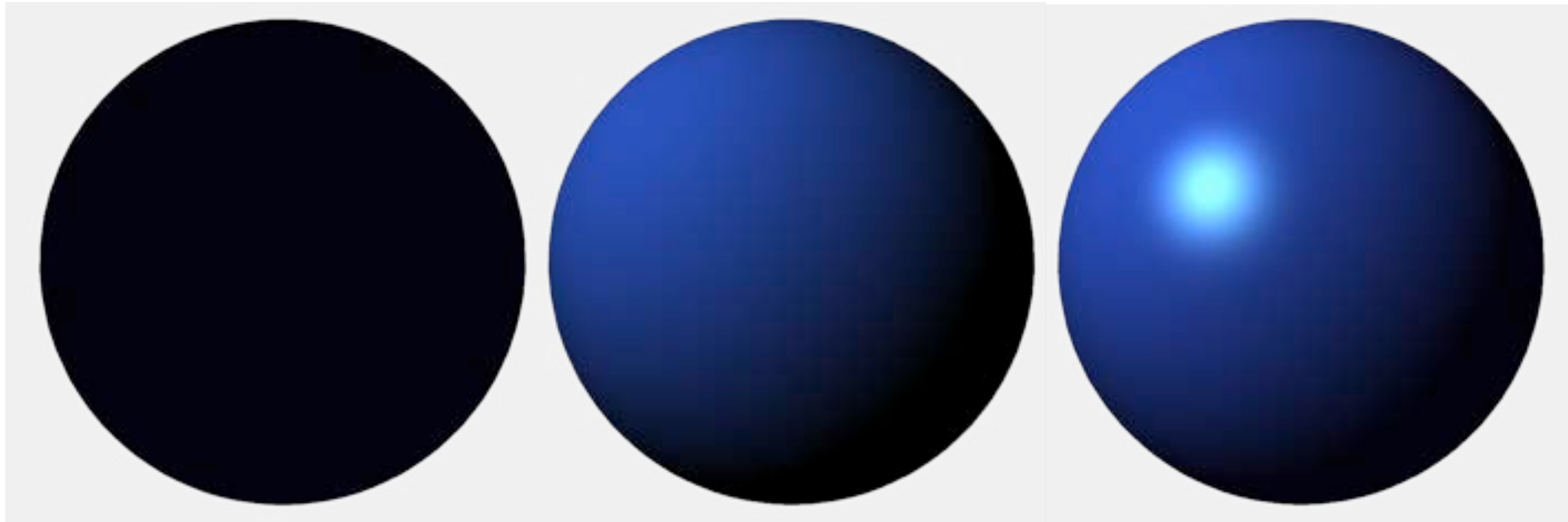
Lambertian Reflection

(Diffuse)

Specular surfaces directly reflect over a small angle

Diffuse and Specular Reflection

- A sphere lit with ambient, +diffuse, +specular reflectance



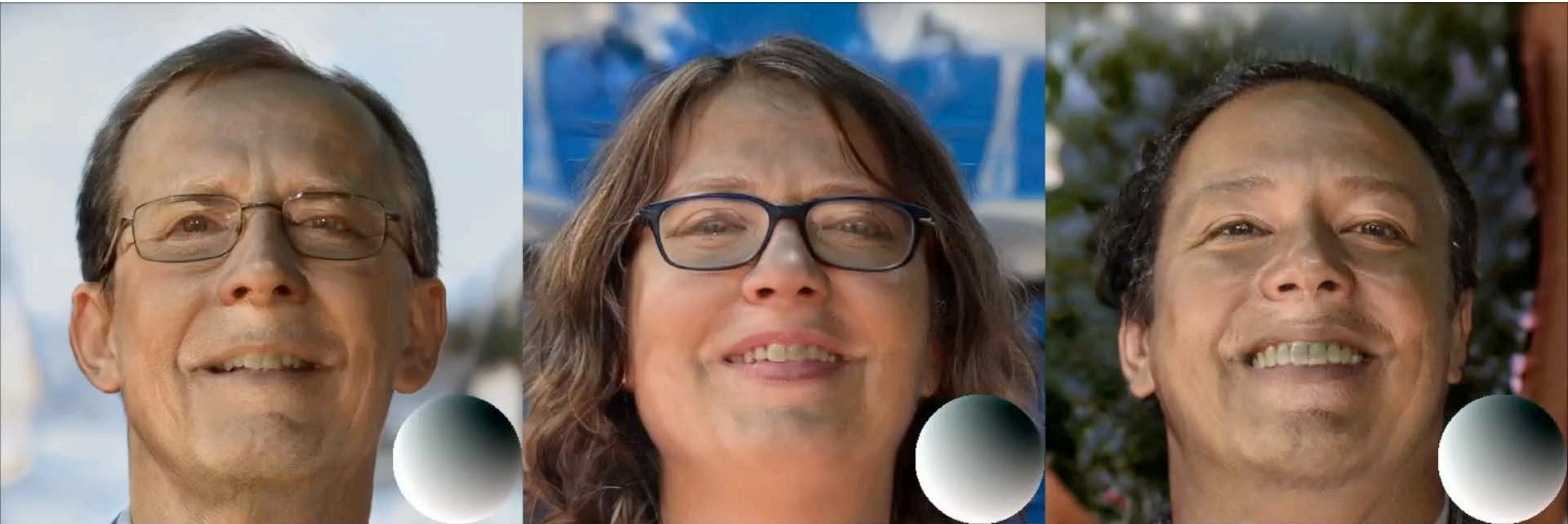
Ambient

+Diffuse

+Specular

Diffuse and Specular Reflection

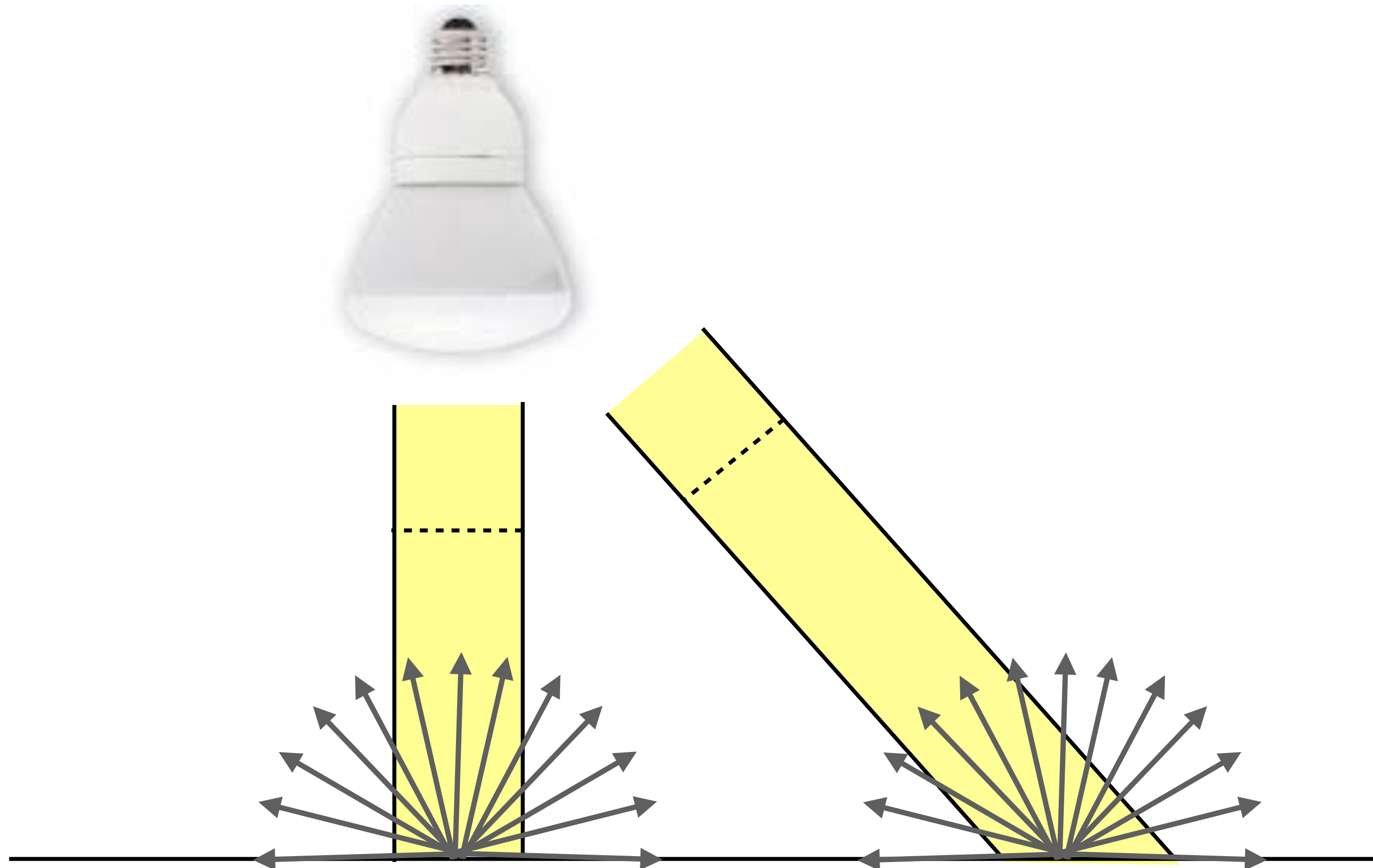
- A motivating example that uses this model



View + Light Control

Diffuse Reflection

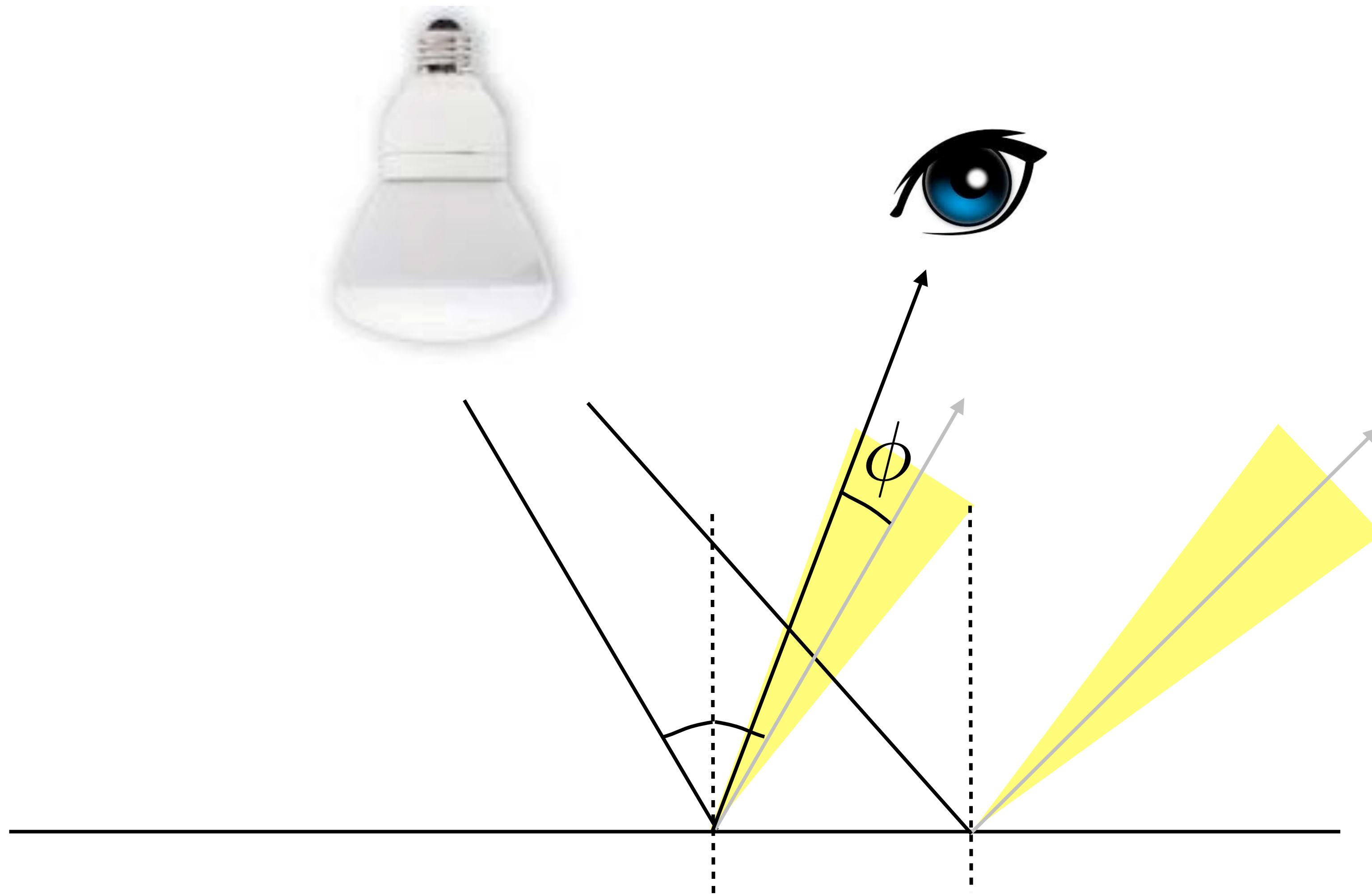
- Light is reflected equally in all directions (Lambertian surface)
- But the amount of light reaching unit surface area depends on the angle between the light and the surface...



2.1

Specular Reflection

- Light reflected strongly around the mirror reflection direction
- Intensity depends on viewer position

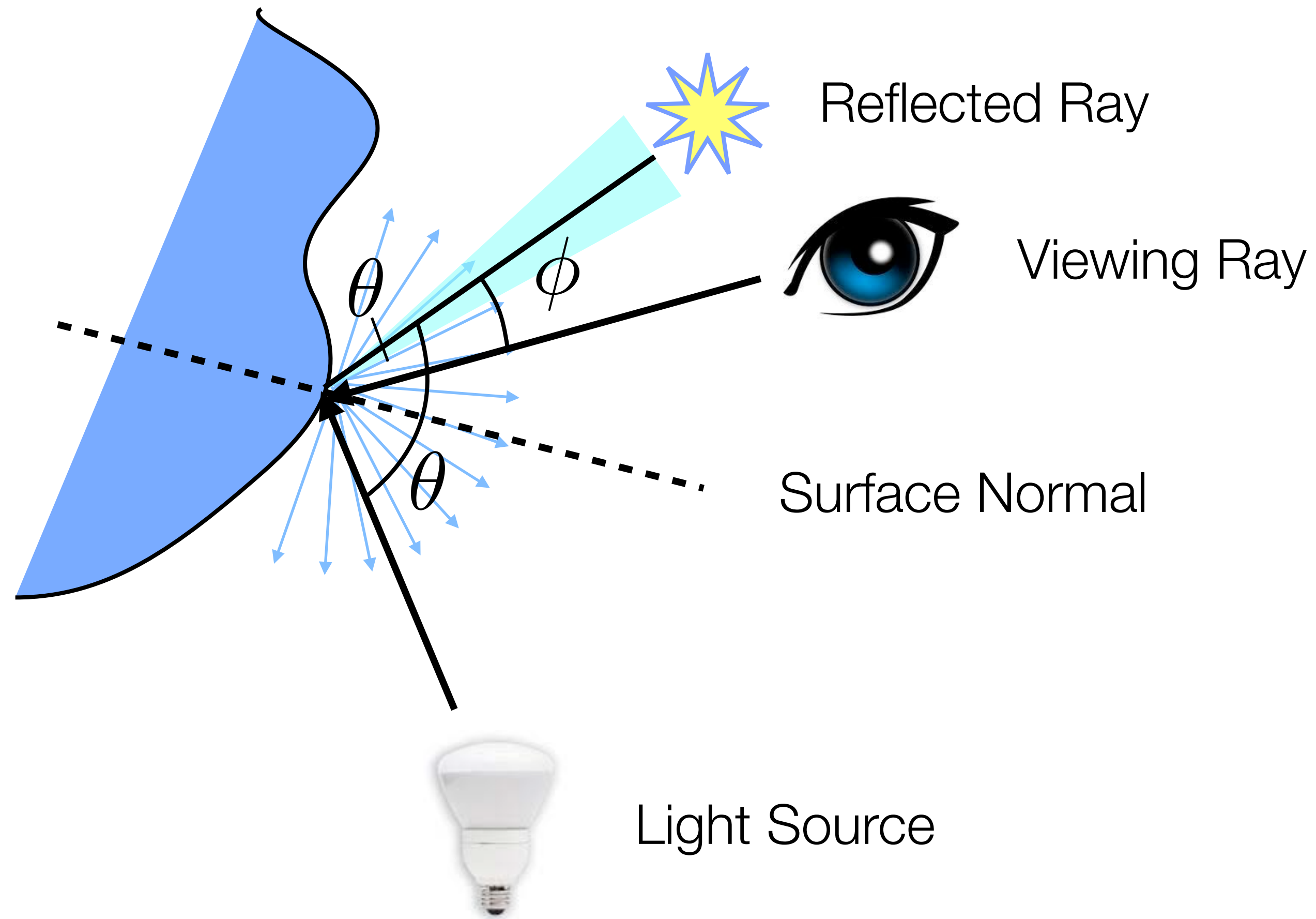


2.2

Phong Illumination Model

- Includes ambient, diffuse and specular reflection

$$I = k_a i_a + k_d i_d \cos \theta + k_s i_s \cos^\alpha \phi$$

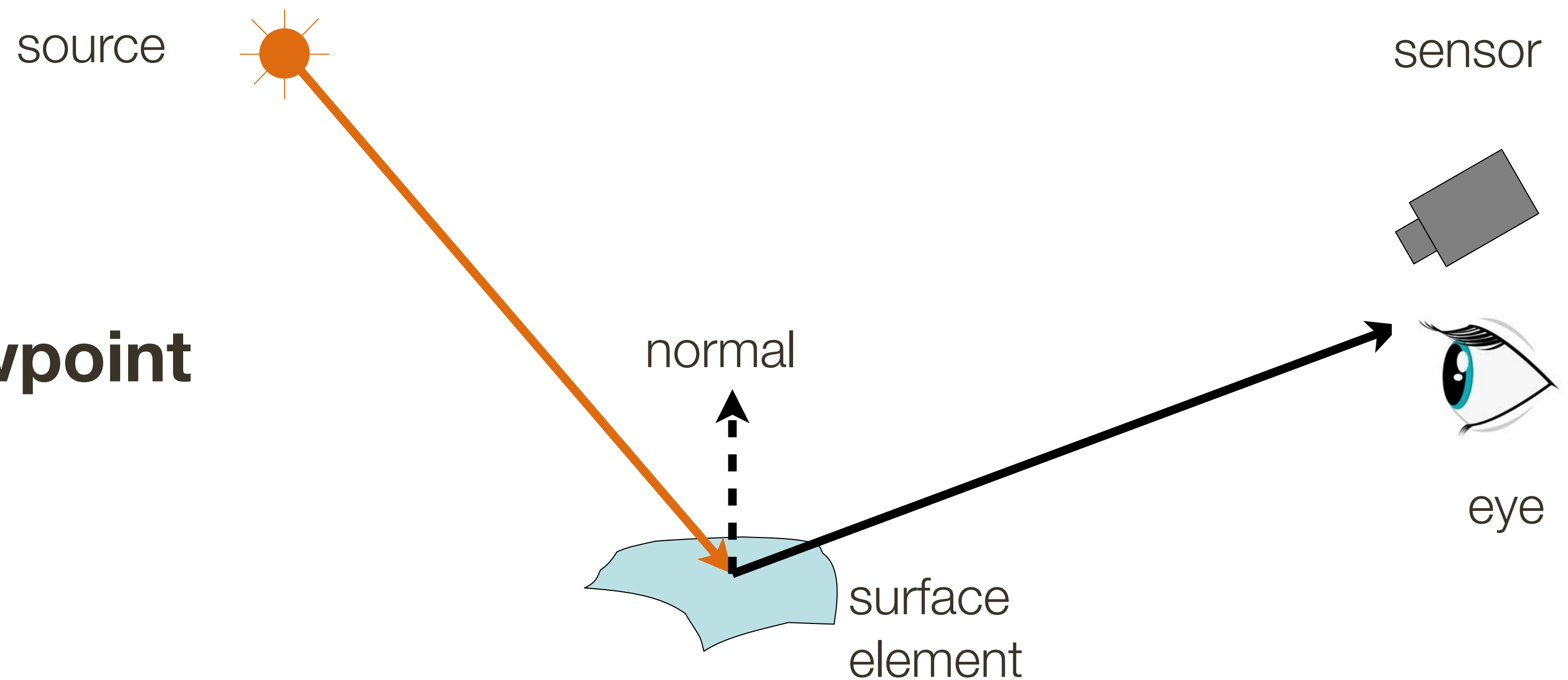


Overview: Image Formation, Cameras and Lenses

Coming back to here...

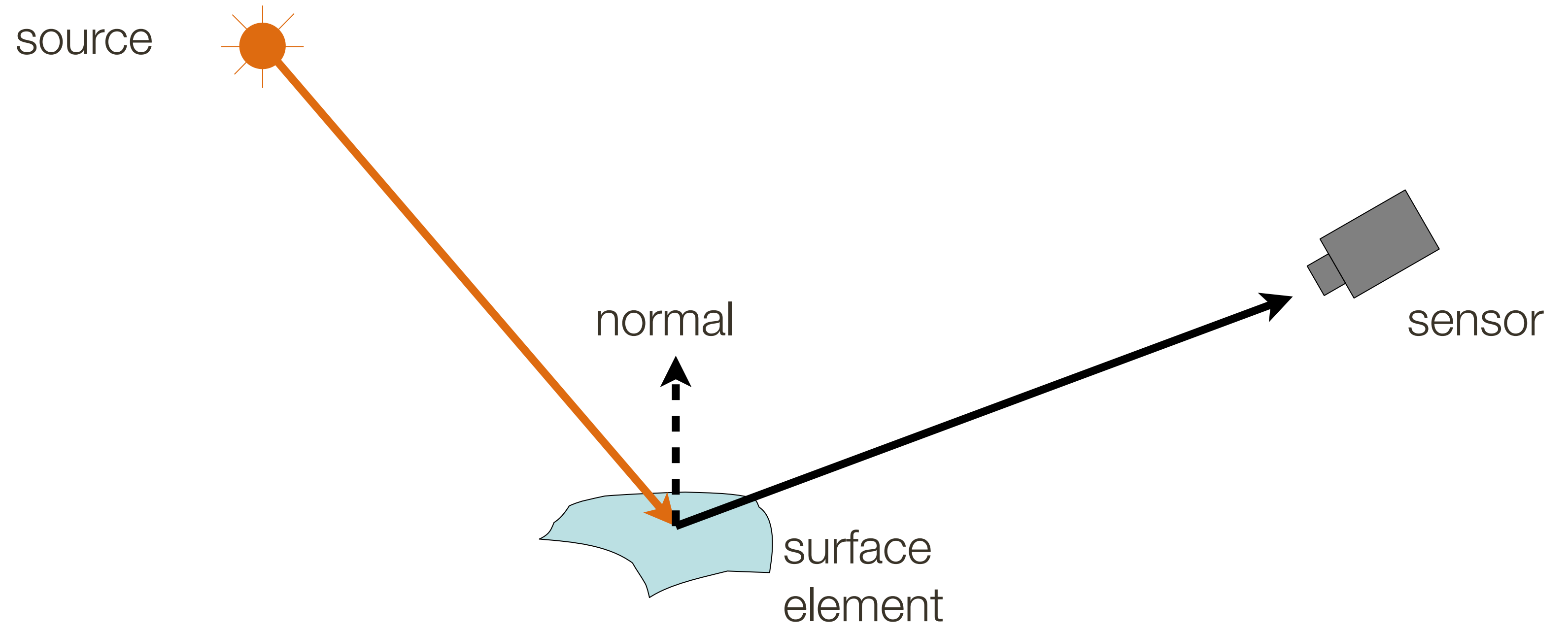
The **image formation process** that produces a particular image depends on

- **Lighting** condition
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- **Surface** properties
- Camera **optics** and **viewpoint**

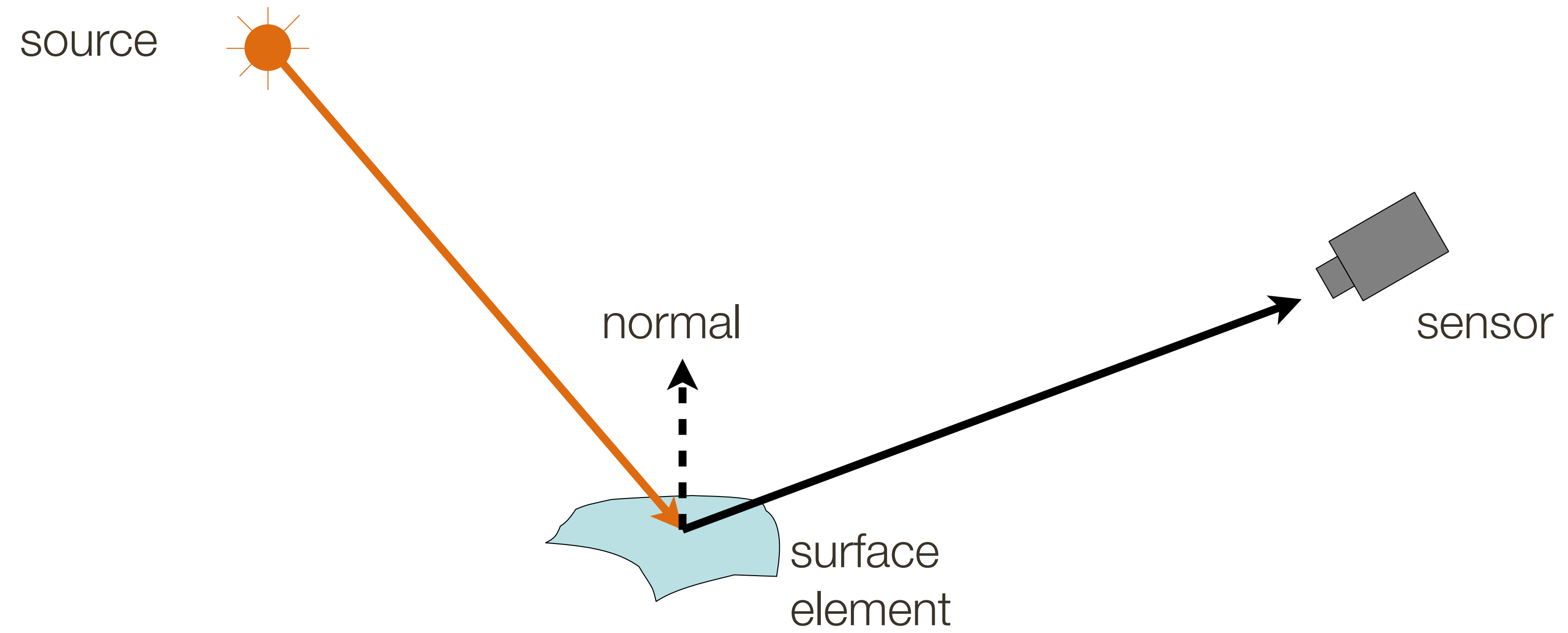


Sensor (or eye) **captures amount of light** reflected from the object

(small) Graphics Review

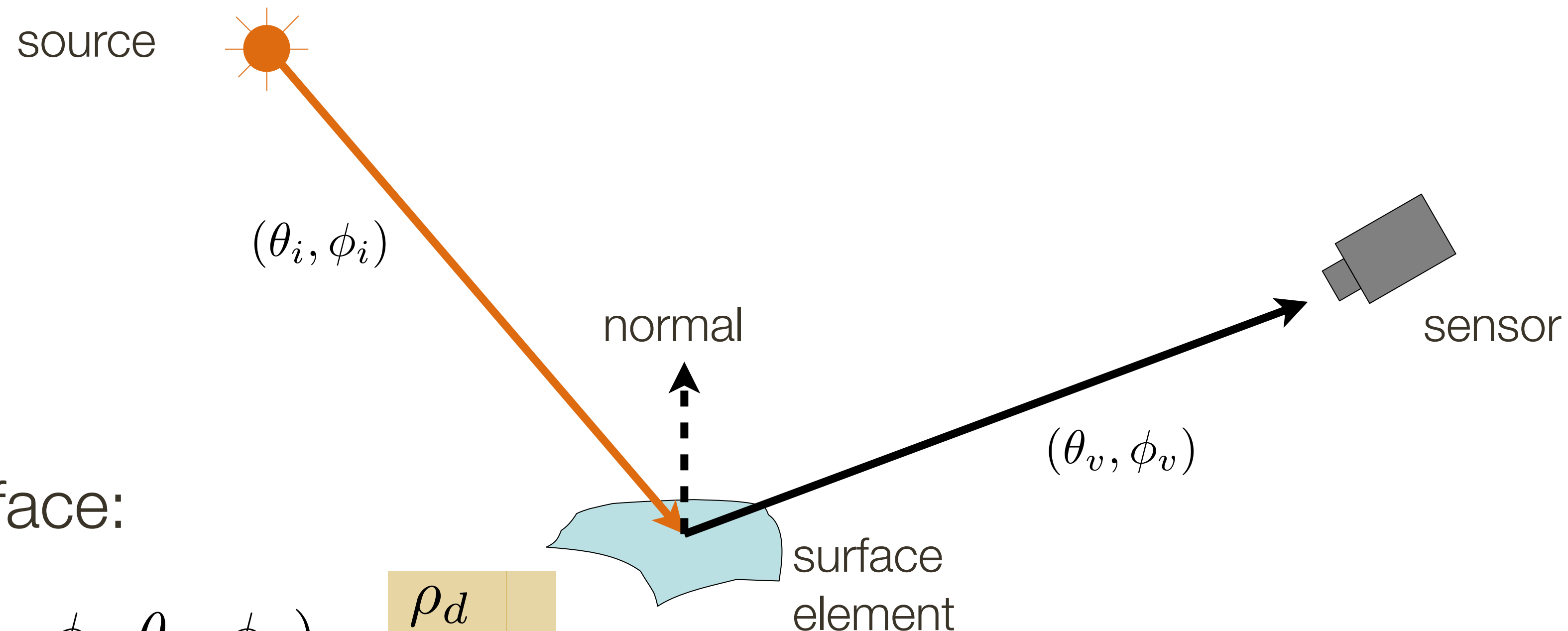


(small) **Graphics** Review



(small) Graphics Review

Surface reflection depends on both the **viewing** (θ_v, ϕ_v) and **illumination** (θ_i, ϕ_i) direction, with Bidirectional Reflection Distribution Function: **BRDF** $(\theta_i, \phi_i, \theta_v, \phi_v)$



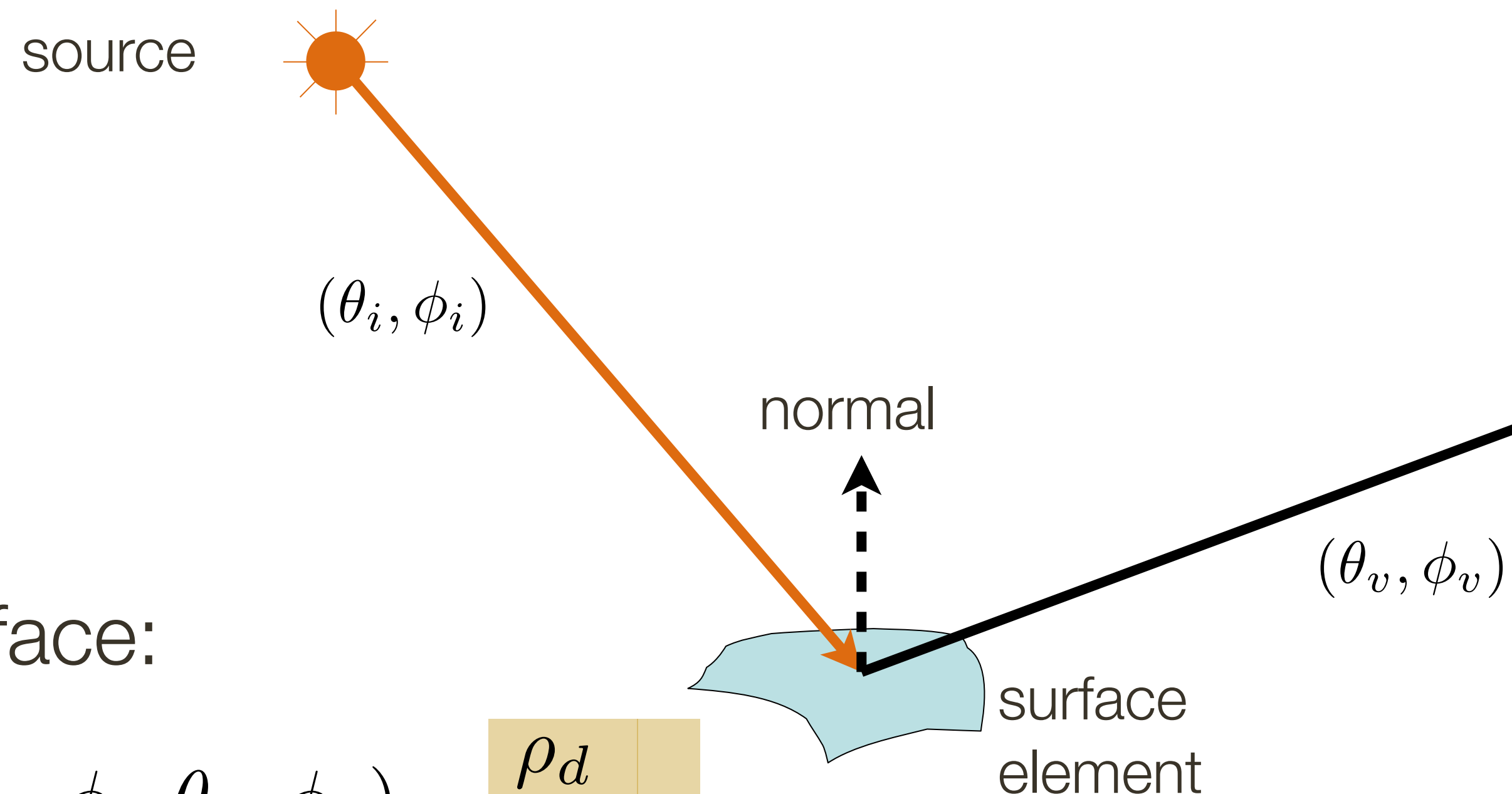
Lambertian surface:

$$\mathbf{BRDF}(\theta_i, \phi_i, \theta_v, \phi_v) = \frac{\rho_d}{\pi}$$

constant, called **albedo**

(small) Graphics Review

Surface reflection depends on both the **viewing** (θ_v, ϕ_v) and **illumination** (θ_i, ϕ_i) direction, with Bidirectional Reflection Distribution Function: **BRDF** $(\theta_i, \phi_i, \theta_v, \phi_v)$



Lambertian surface:

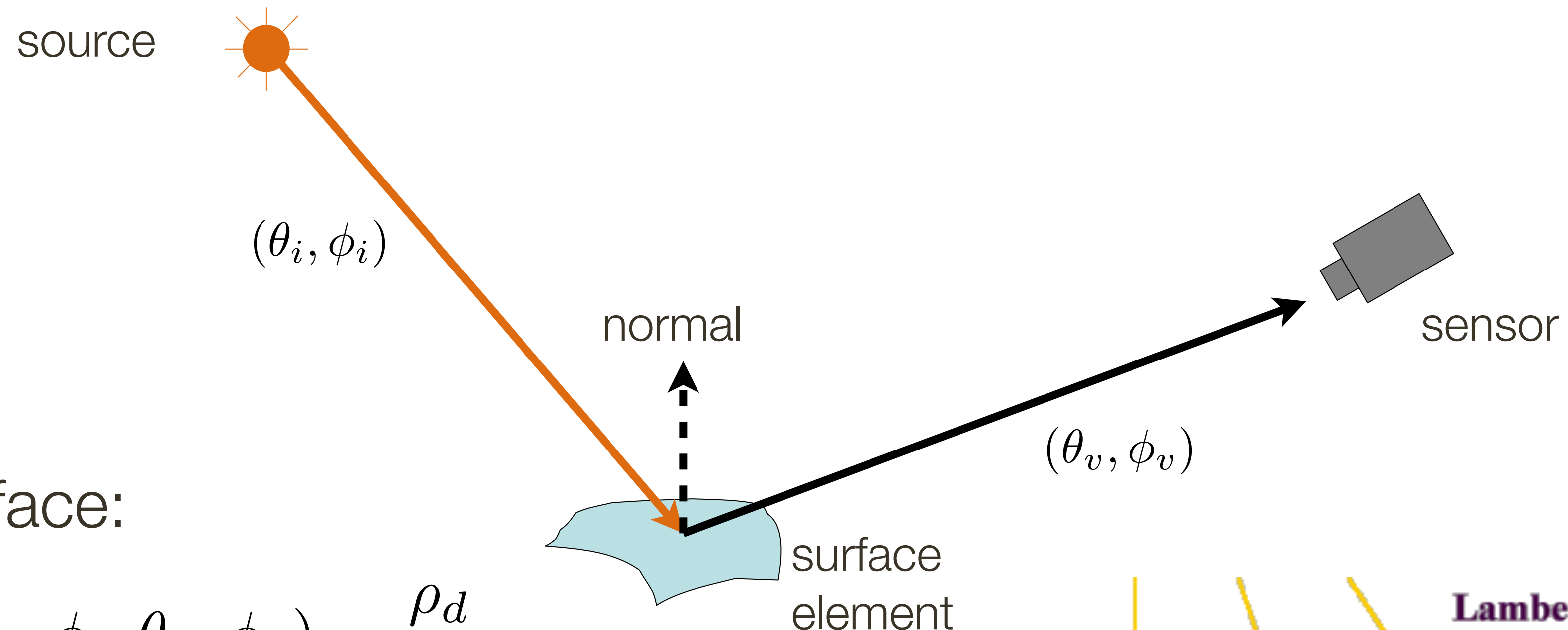
$$\text{BRDF}(\theta_i, \phi_i, \theta_v, \phi_v) = \frac{\rho_d}{\pi}$$

constant, called **albedo**

Surface type	Typical value
Fresh asphalt	0.03 – 0.04
Open ocean	0.06
Conifer forest (summer)	0.08 – 0.15
Worn asphalt	0.12
Deciduous trees	0.15 – 0.18
Sand	0.15 – 0.45
Tundra	0.18 – 0.25
Agricultural crops	0.18 – 0.25
Bare soil	0.17
Green grass	0.20 – 0.25
Desert sand	0.30 – 0.40
Snow	0.40 – 0.90
Ocean ice	0.50 – 0.70
Fresh snow	0.80 – 0.90

(small) Graphics Review

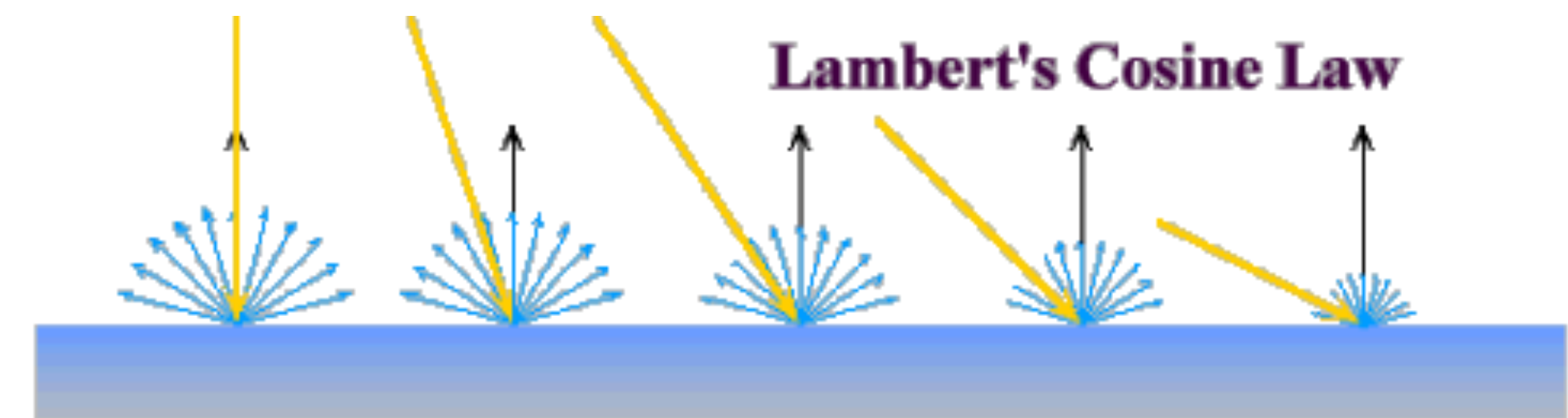
Surface reflection depends on both the **viewing** (θ_v, ϕ_v) and **illumination** (θ_i, ϕ_i) direction, with Bidirectional Reflection Distribution Function: **BRDF** $(\theta_i, \phi_i, \theta_v, \phi_v)$



Lambertian surface:

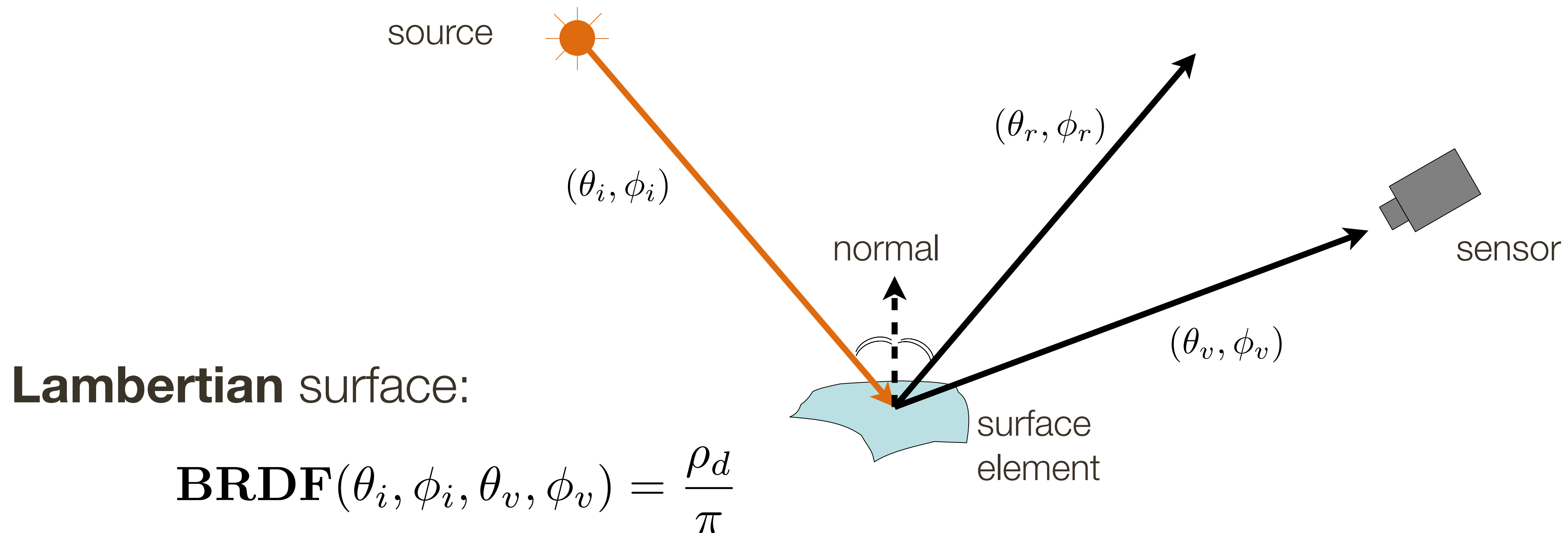
$$\text{BRDF}(\theta_i, \phi_i, \theta_v, \phi_v) = \frac{\rho_d}{\pi}$$

$$L = \frac{\rho_d}{\pi} I(\vec{i} \cdot \vec{n})$$



(small) Graphics Review

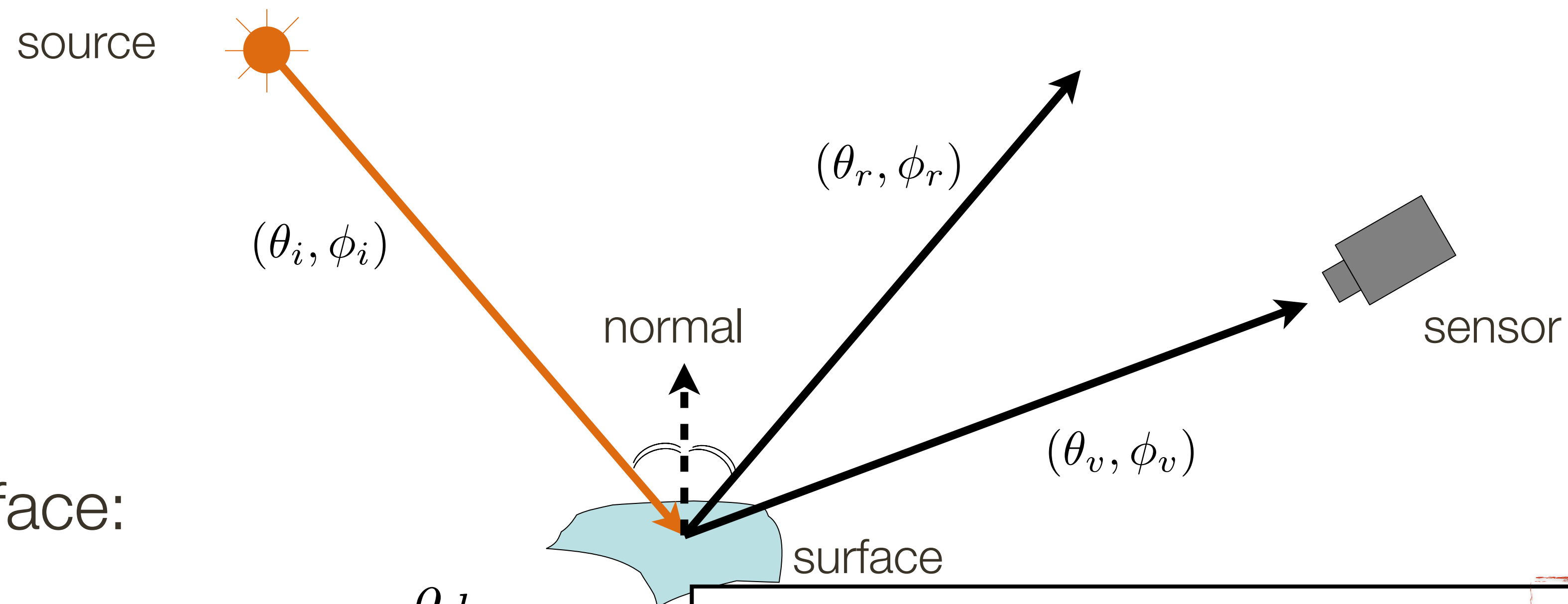
Surface reflection depends on both the **viewing** (θ_v, ϕ_v) and **illumination** (θ_i, ϕ_i) direction, with Bidirectional Reflection Distribution Function: **BRDF** $(\theta_i, \phi_i, \theta_v, \phi_v)$



Mirror surface: all incident light reflected in one directions $(\theta_v, \phi_v) = (\theta_r, \phi_r)$

(small) Graphics Review

Surface reflection depends on both the **viewing** (θ_v, ϕ_v) and **illumination** (θ_i, ϕ_i) direction, with Bidirectional Reflection Distribution Function: **BRDF** $(\theta_i, \phi_i, \theta_v, \phi_v)$



Lambertian surface:

$$\text{BRDF}(\theta_i, \phi_i, \theta_v, \phi_v) = \frac{\rho_d}{\pi}$$

Recall...

$$I = k_a i_a + k_d i_d \cos \theta + k_s i_s \cos^\alpha \phi$$

Mirror surface: all incident light reflected in one directions $(\theta_v, \phi_v) = (\theta_r, \phi_r)$

Reflectance in Vision



Reflectance in Graphics

Cameras

Old school **film** camera



Digital CCD/CMOS camera



Let's say we have a **sensor** ...

Digital CCD/CMOS camera



digital sensor
(CCD or
CMOS)

... and the **object** we would like to photograph

What would an image taken like this look like?

real-world
object



digital sensor
(CCD or
CMOS)



Bare-sensor imaging

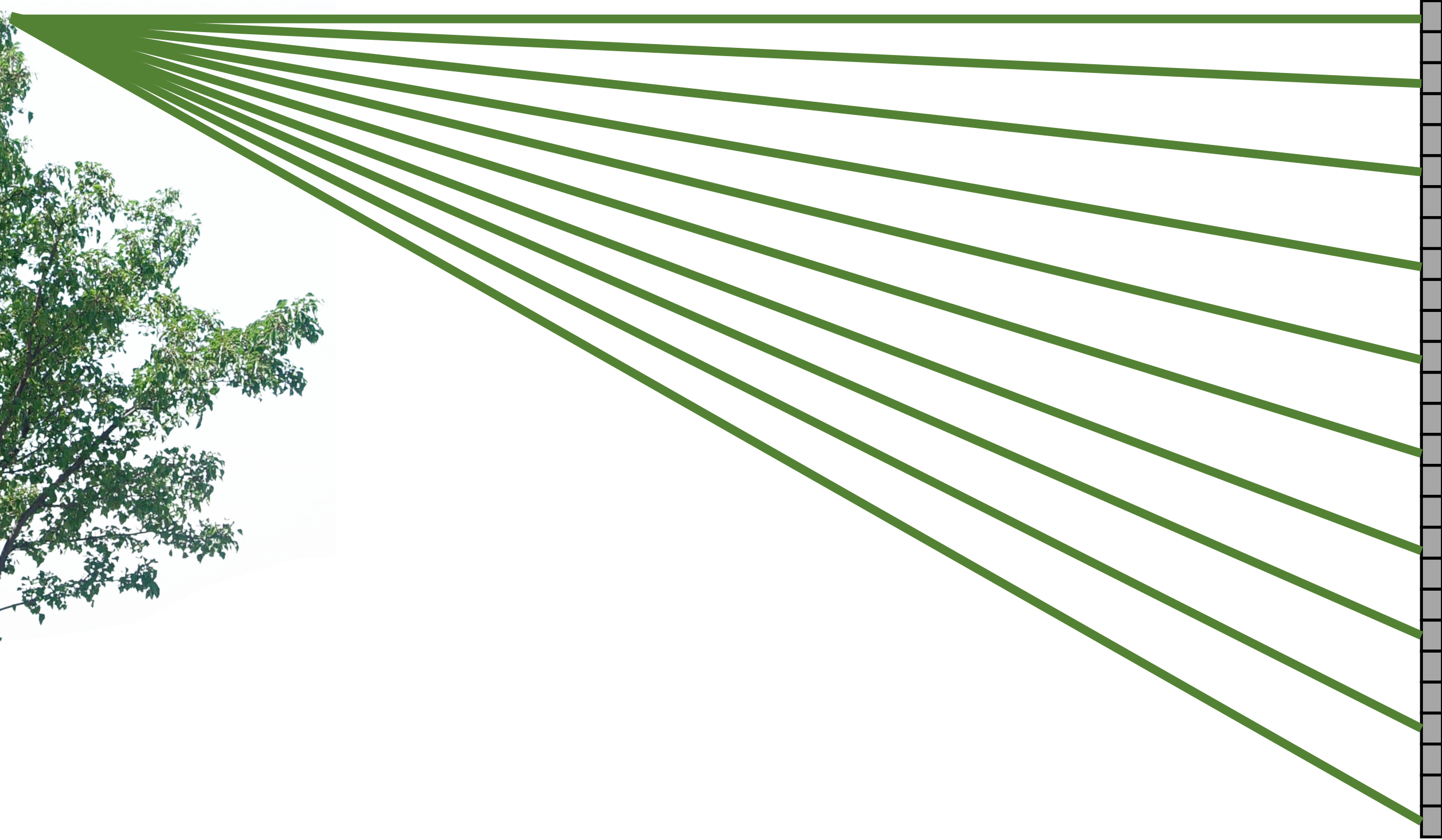
real-world
object



digital sensor
(CCD or
CMOS)

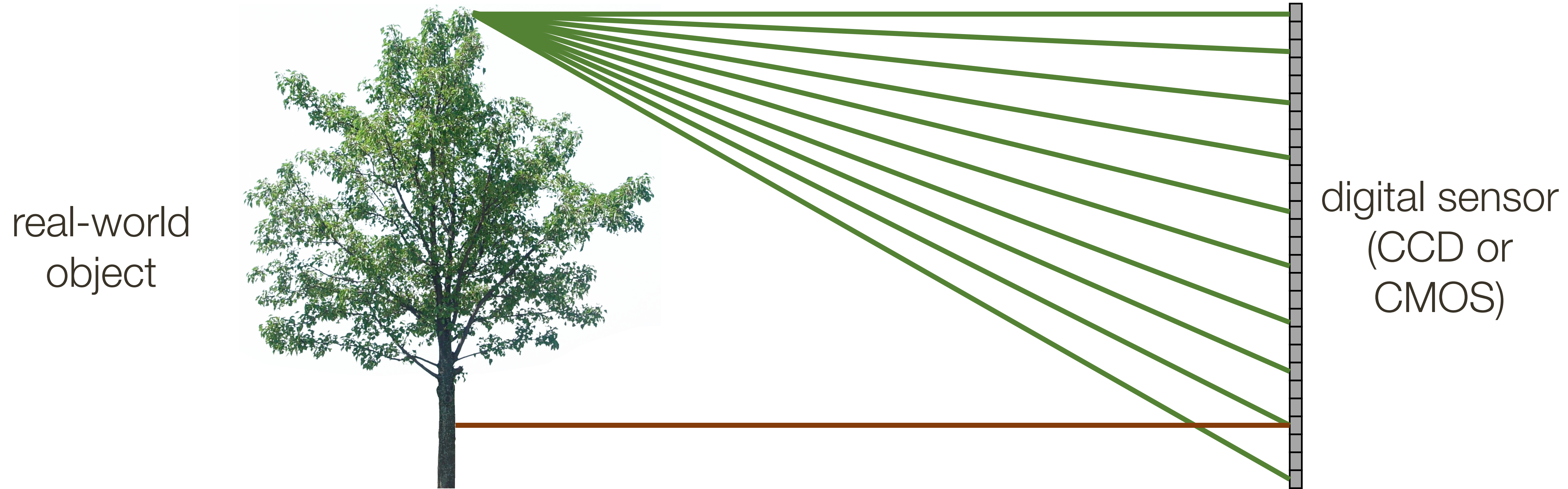
Bare-sensor imaging

real-world
object

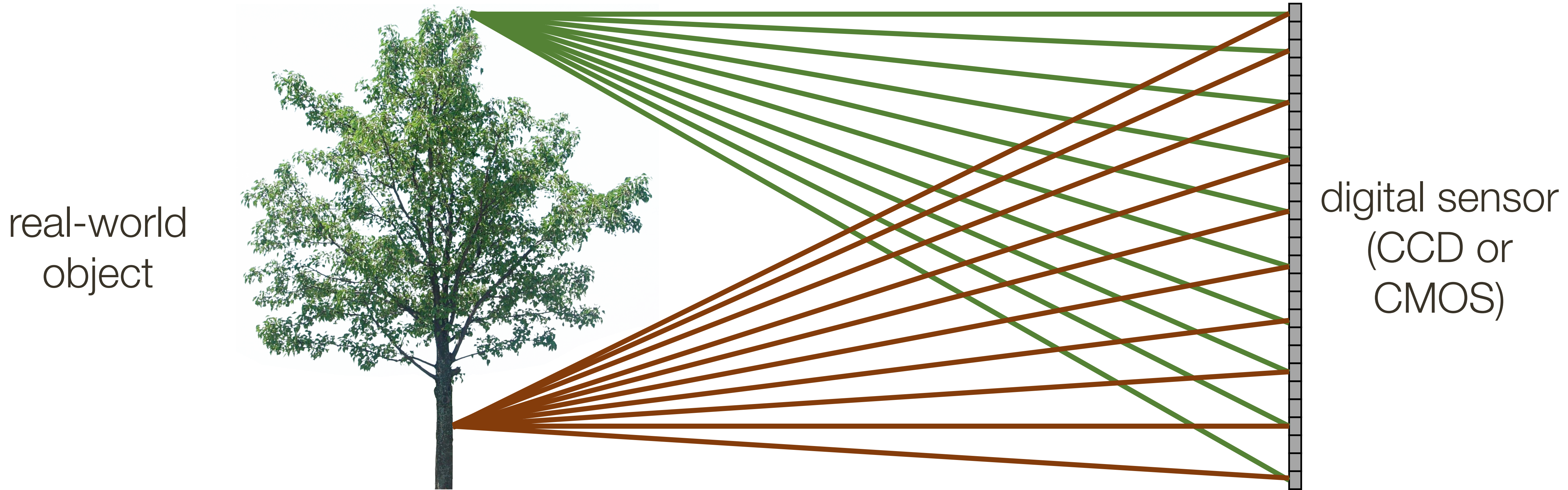


digital sensor
(CCD or
CMOS)

Bare-sensor imaging



Bare-sensor imaging



All scene points contribute to all sensor pixels

Bare-sensor imaging



All scene points contribute to all sensor pixels

Pinhole Camera

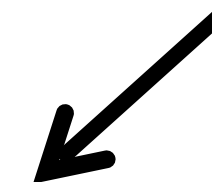
real-world
object



barrier (diaphragm)



pinhole
(aperture)



digital sensor
(CCD or
CMOS)



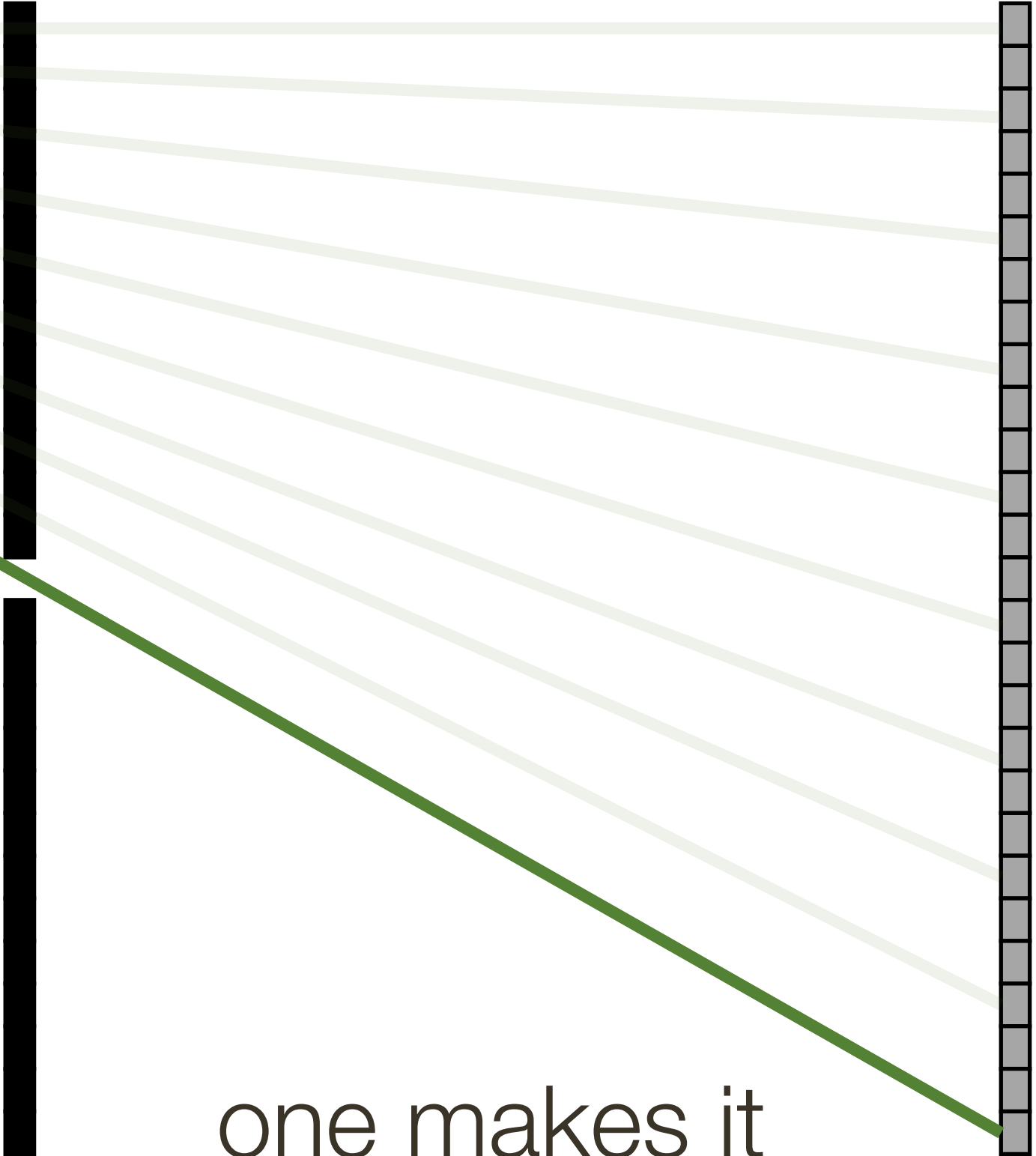
What would an image taken like this look like?

Pinhole Camera

real-world object



most rays are blocked

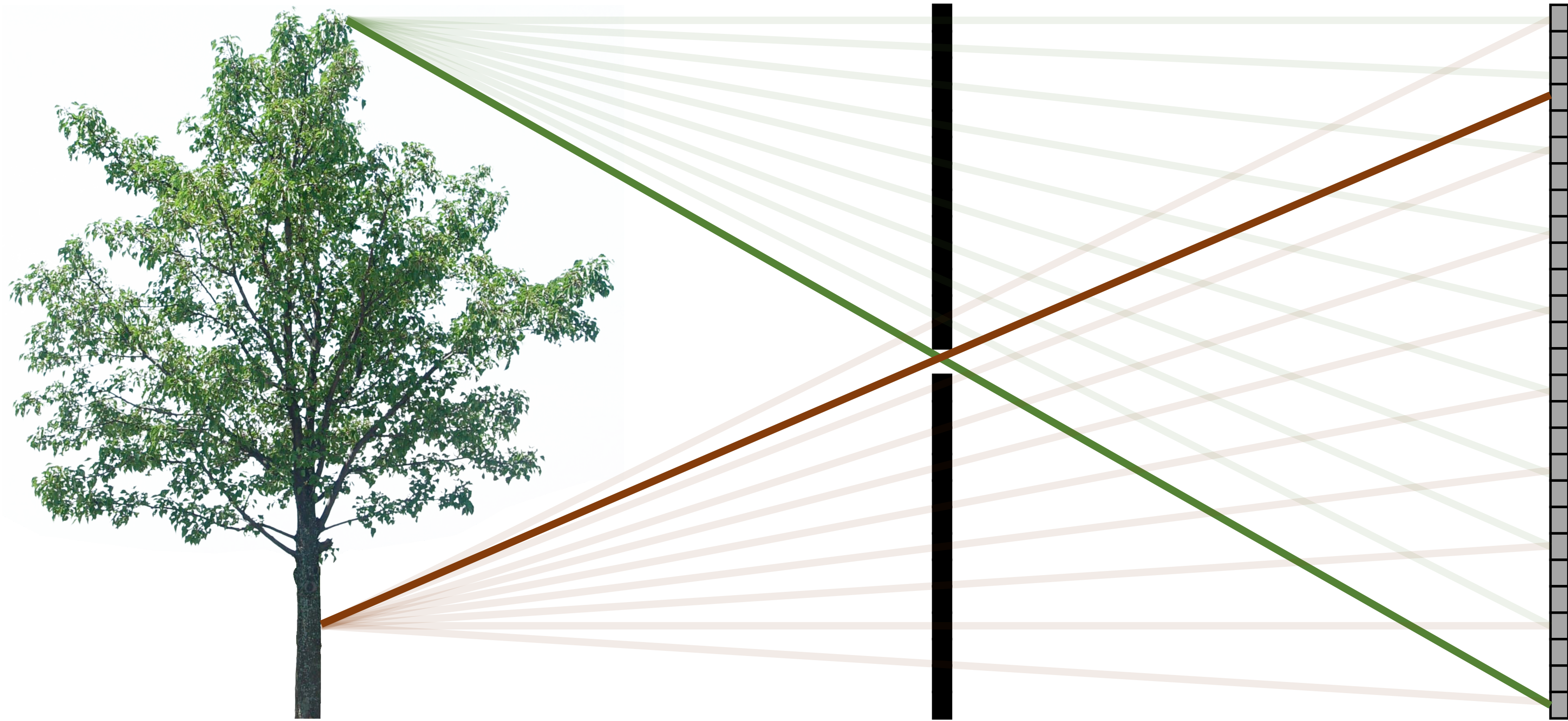


one makes it through

digital sensor (CCD or CMOS)

Pinhole Camera

real-world
object



digital sensor
(CCD or
CMOS)

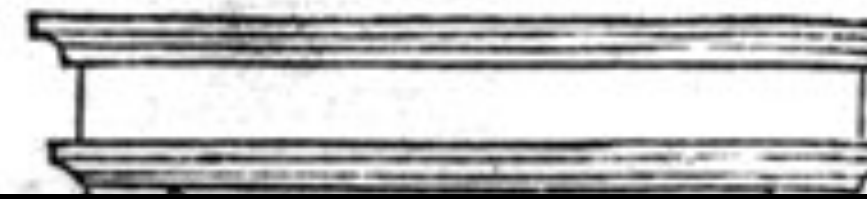
Each scene point contributes to only one sensor pixel

Camera Obscura (latin for “dark chamber”)



illum in tabula per radios Solis, quam in cælo contin-
git: hoc est, si in cælo superior pars deliquiū patiatur, in
radiis apparebit inferior deficere, vt ratio exigat optica.

*Solis deliquium Anno Christi
1544. Die 24. Januarij
Louanij*



principles behind the pinhole camera or camera obscura were first mentioned by Chinese philosopher Mozi (Mo-Ti) (470 to 390 BCE)



Sic nos exactè Anno .1544. Louanii eclipsim Solis
obseruauimus, inuenimusq; deficere paulò plus q̄ dex-

Reinerus Gemma-Frisius observed an eclipse of the sun at Louvain on January 24, 1544. He used this illustration in his book, “De Radio Astronomica et Geometrica,” 1545. It is thought to be the first published illustration of a camera obscura.

Credit: John H., Hammond, “Th Camera Obscure, A Chronicle”

First **Photograph** on Record

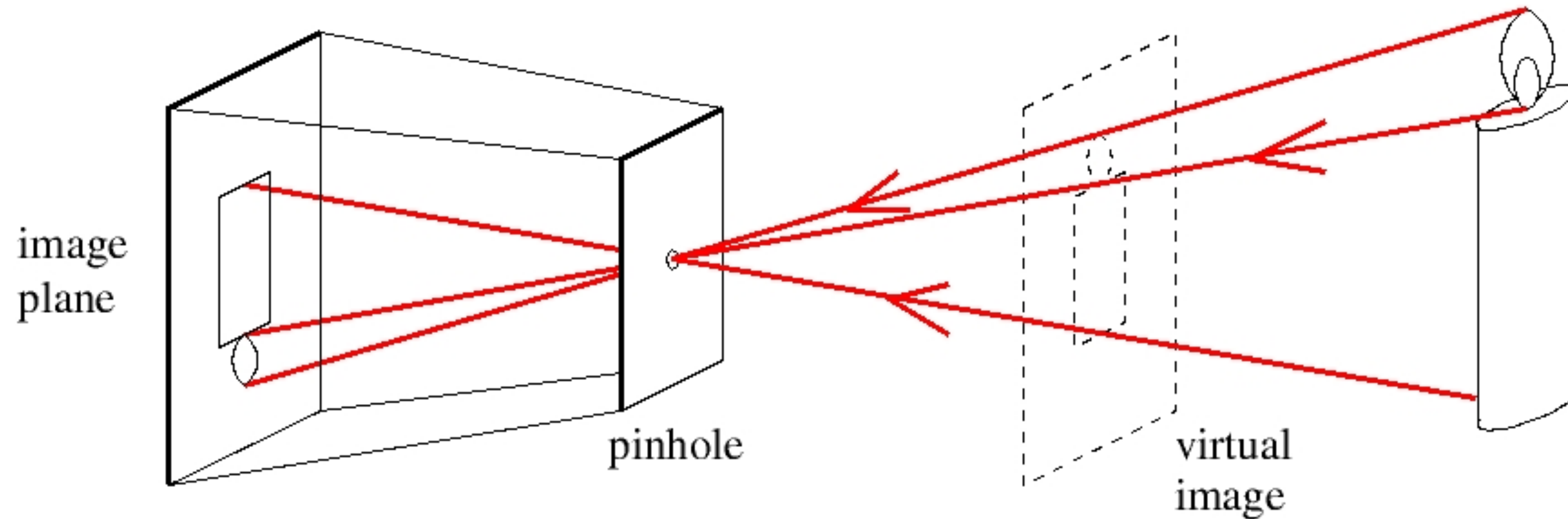
La table servie



Credit: Nicéphore Niepce, 1822

Pinhole Camera

A pinhole camera is a box with a small hole (**aperture**) in it



Forsyth & Ponce (2nd ed.) Figure 1.2

Image Formation



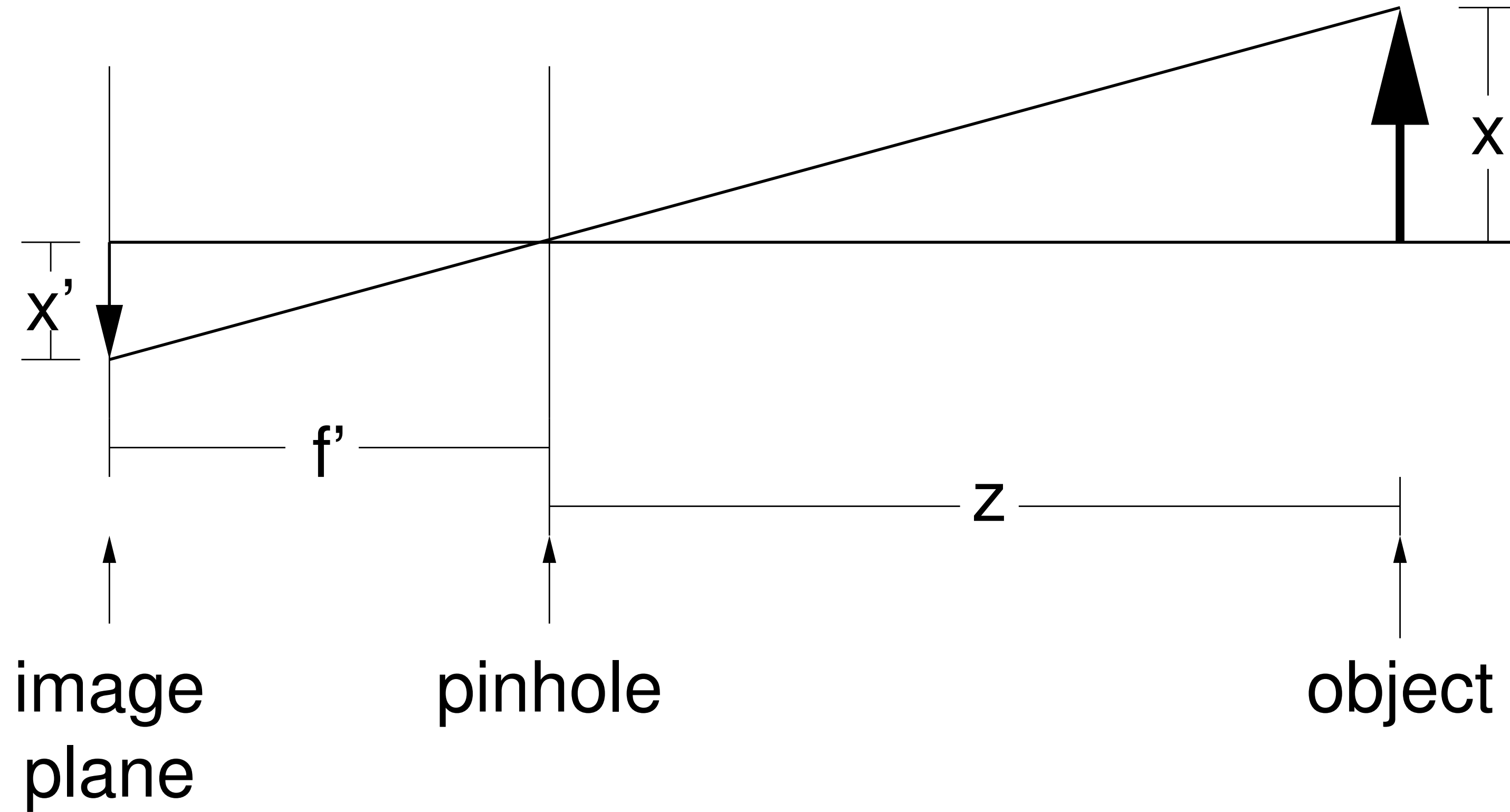
Forsyth & Ponce (2nd ed.) Figure 1.1

Accidental Pinhole Camera



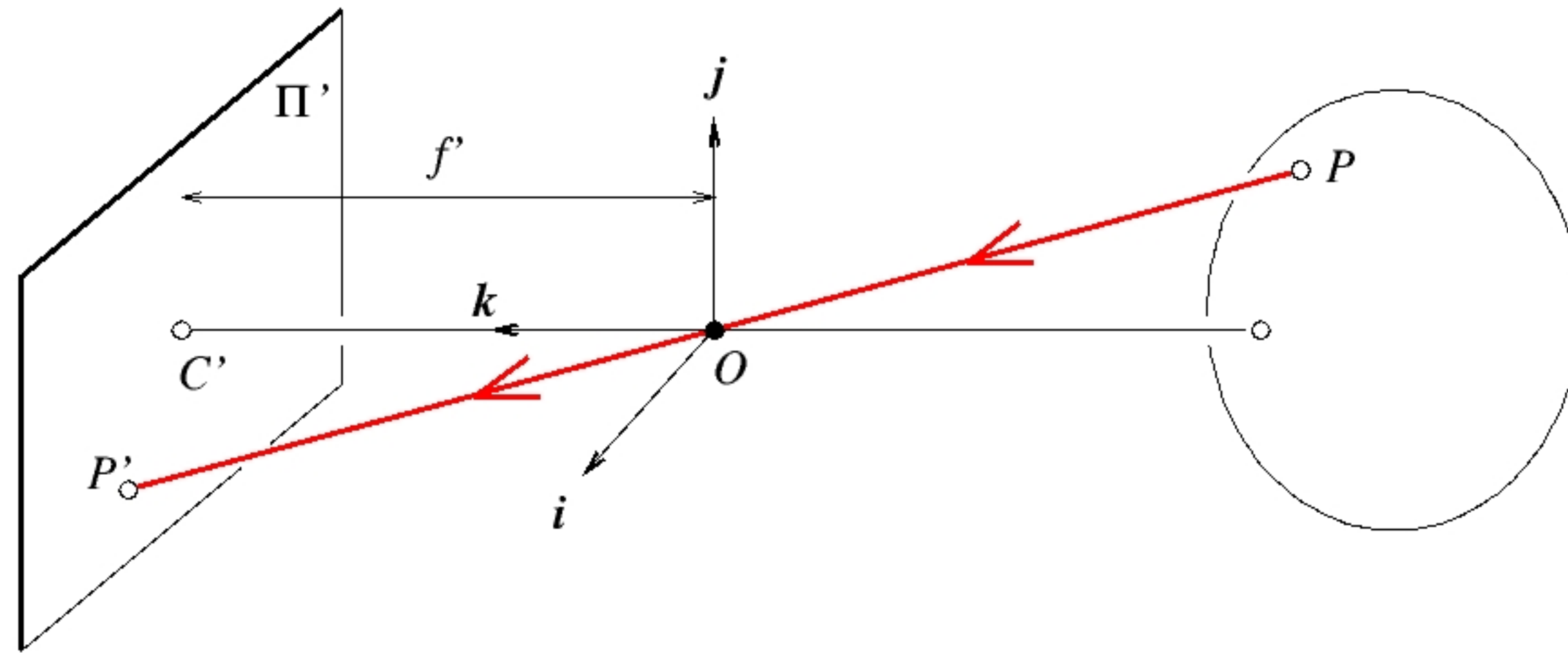
Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

Pinhole Camera



2.3

Perspective Projection



3D object point

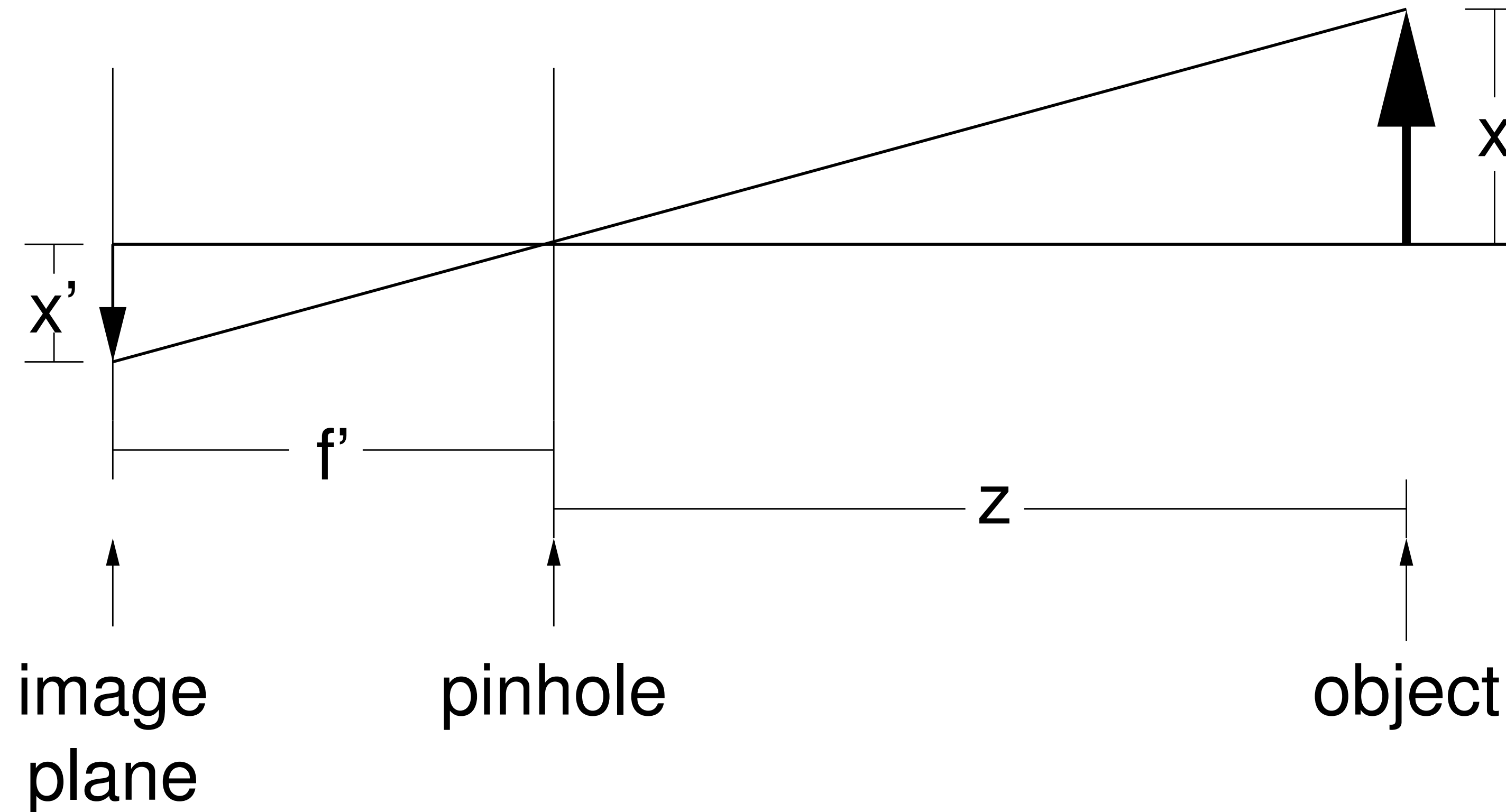
Forsyth & Ponce (1st ed.) Figure 1.4

$P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ projects to 2D image point $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$ where

$$\begin{aligned} x' &= f' \frac{x}{z} \\ y' &= f' \frac{y}{z} \end{aligned}$$

Pinhole Camera

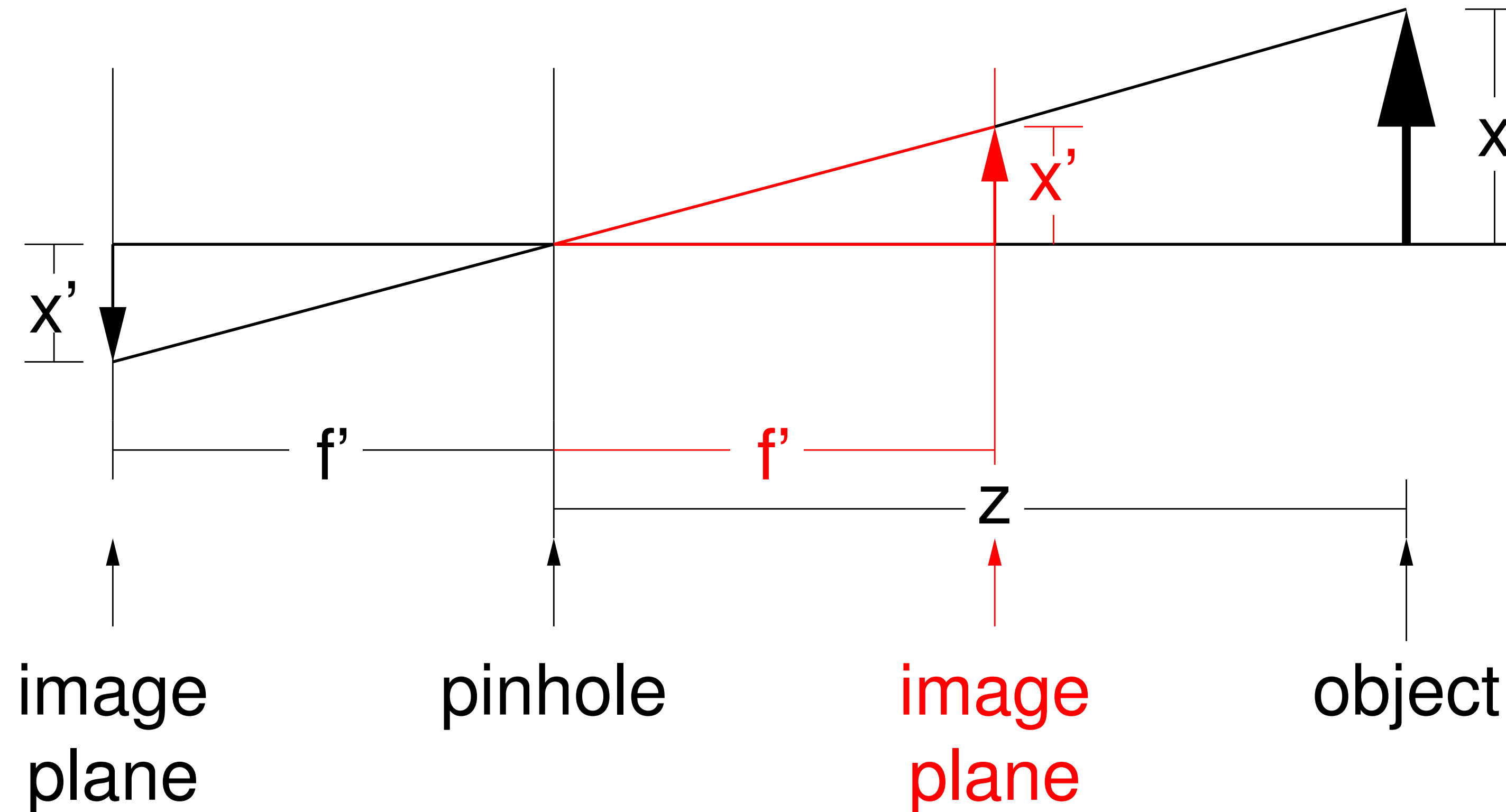
f' is the **focal length** of the camera



Note: In a pinhole camera we can adjust the focal length, all this will do is change the **size** of the resulting image

Pinhole Camera

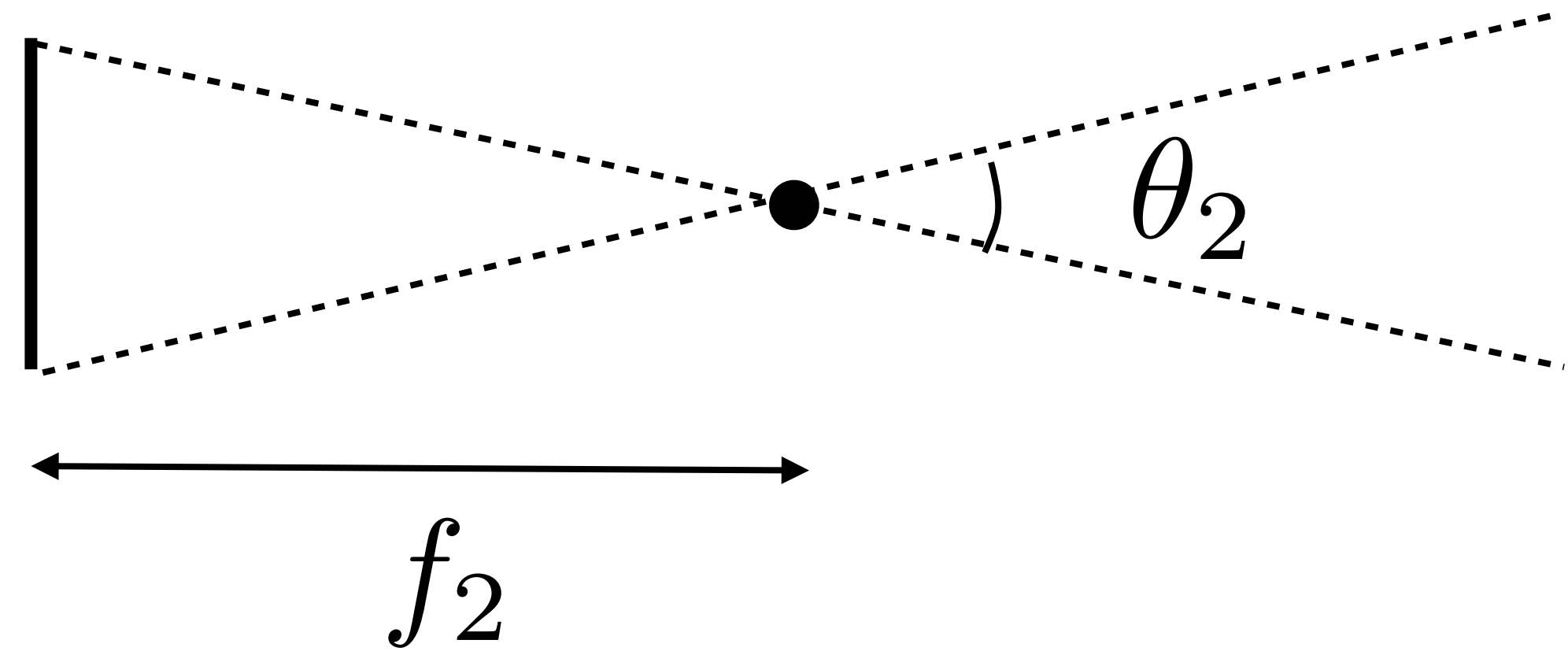
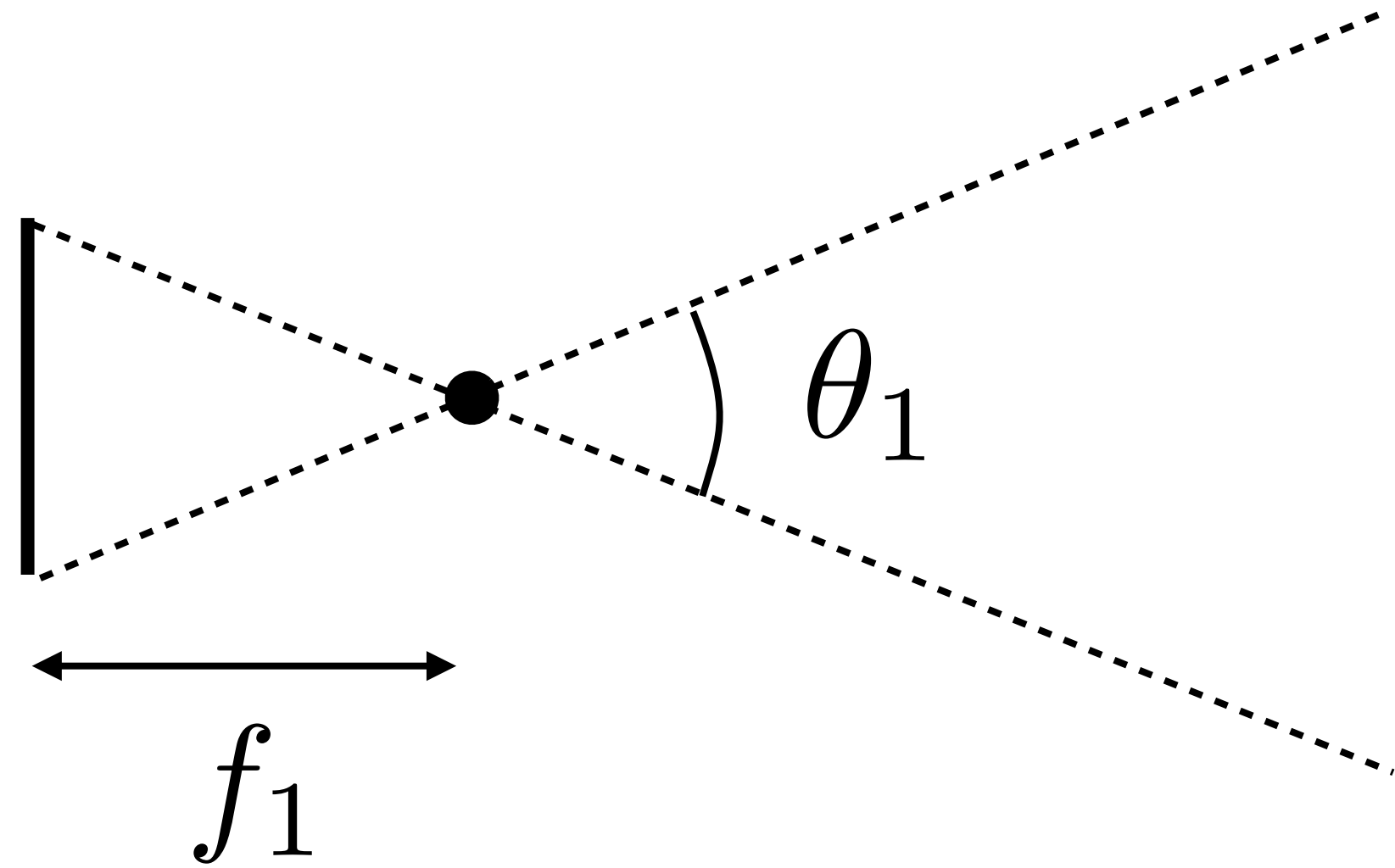
It is convenient to think of the **image plane** being in front of the pinhole



What happens if object moves towards the camera? Away from the camera?

Focal Length

- For a fixed sensor size, focal length determines the field of view (fov)



2.5

Q: What is the field of view of a **full-frame (35mm) camera** with a **50mm lens**? 100mm lens?

Sensor size

Focal length

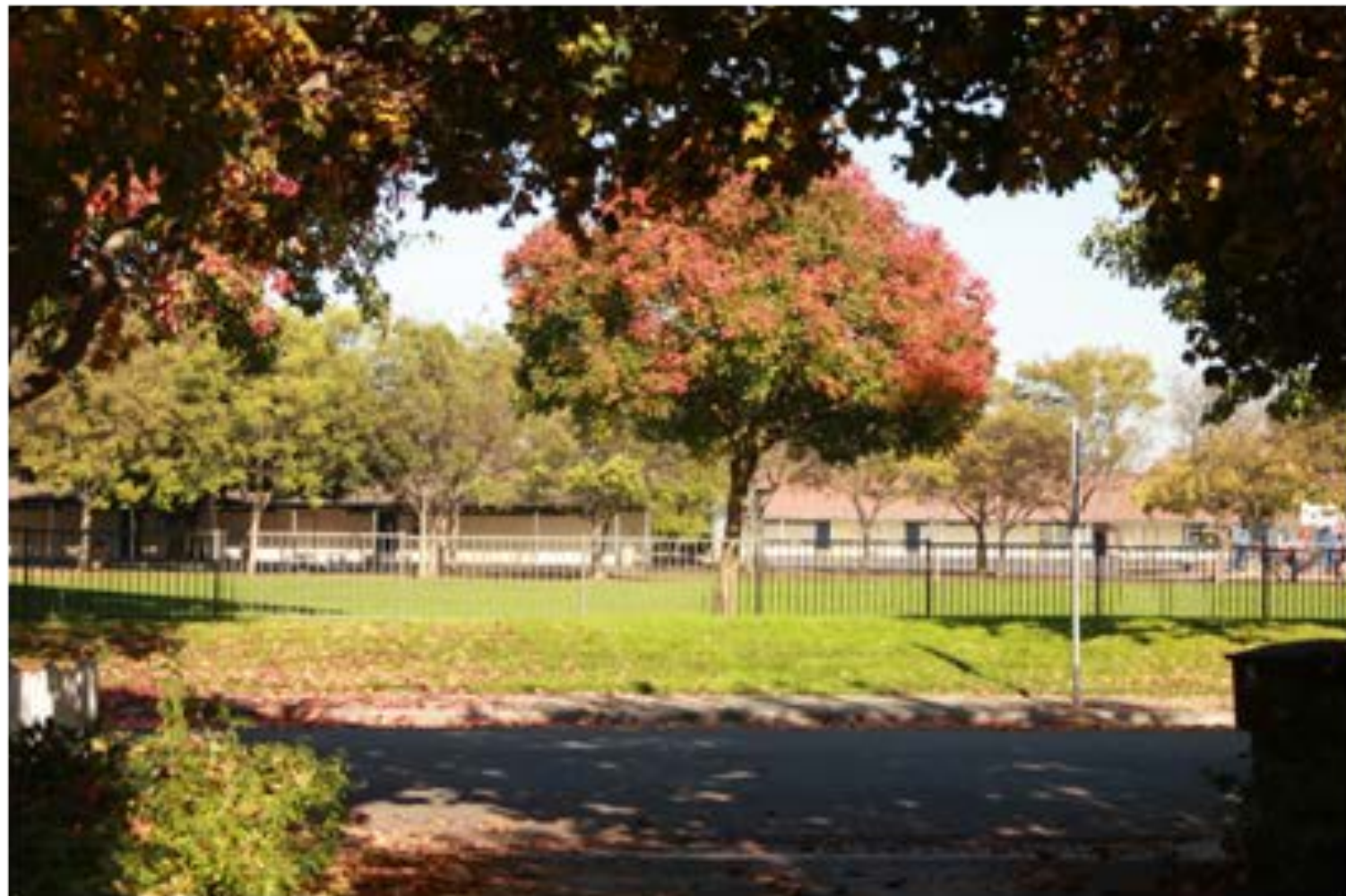
Focal Length



28 mm



35 mm



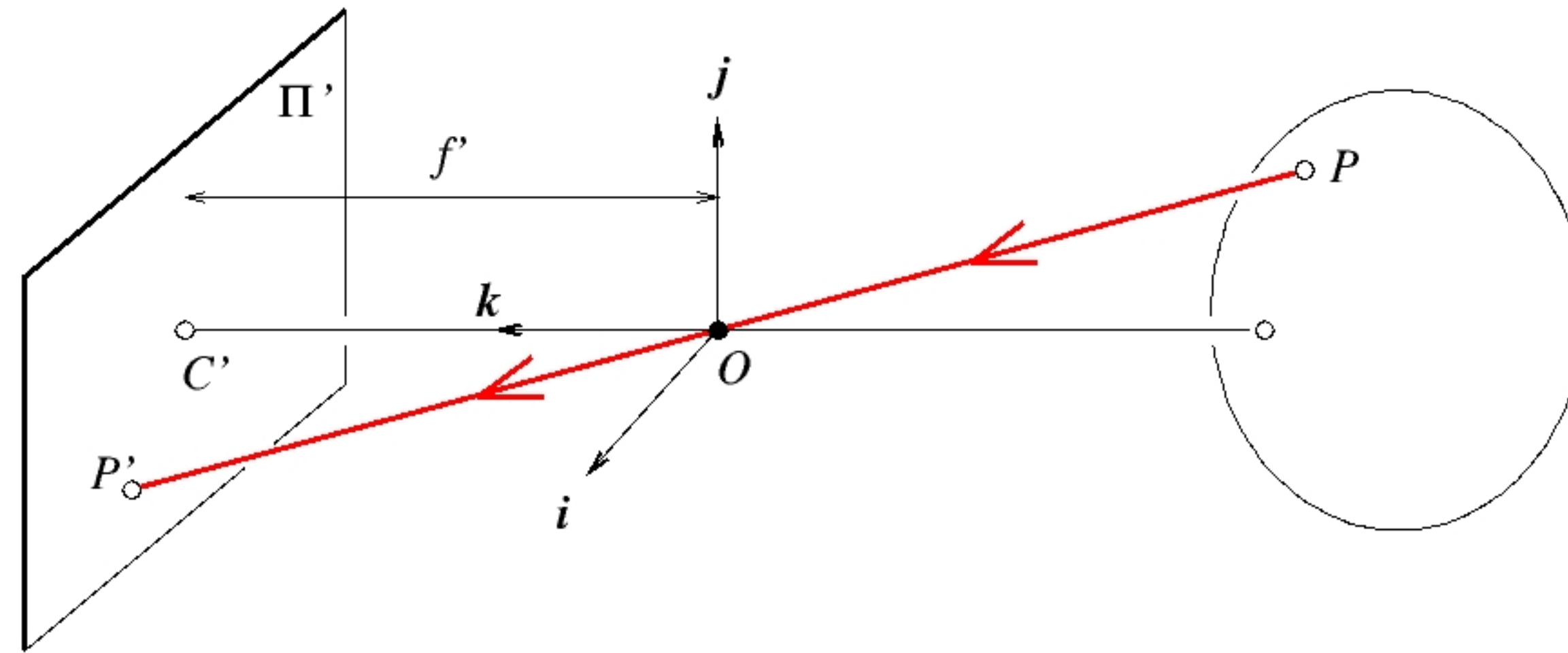
50 mm



70 mm

Perspective Projection: Matrix Form

Camera Matrix



$$\mathbf{C} = \begin{bmatrix} f' & 0 & 0 & 0 \\ 0 & f' & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

3D object point

Forsyth & Ponce (1st ed.) Figure 1.4

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

projects to 2D image point

$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$

where

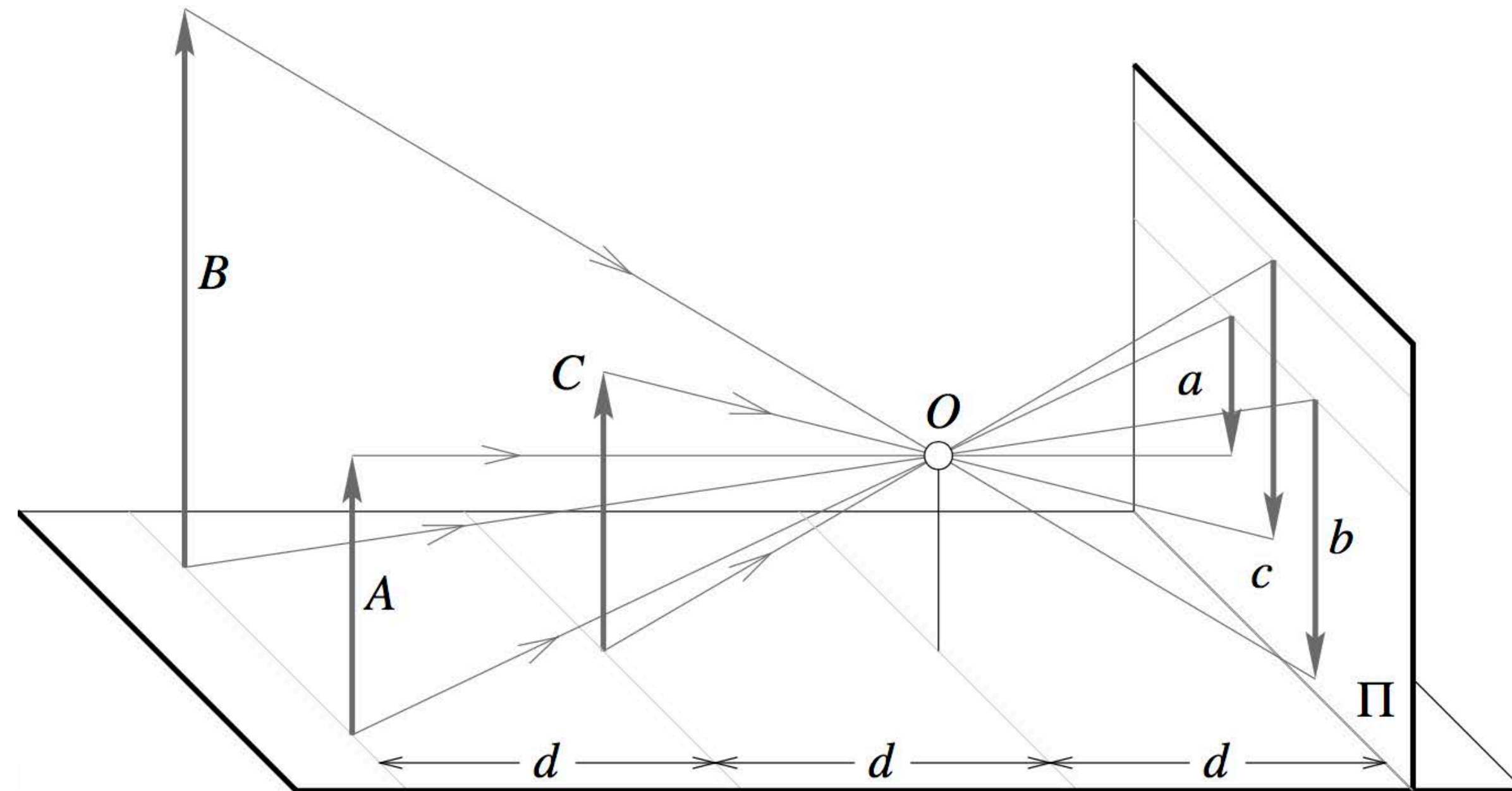
$$sP' = \mathbf{C}P$$

(s is a scale factor)



Perspective Effects

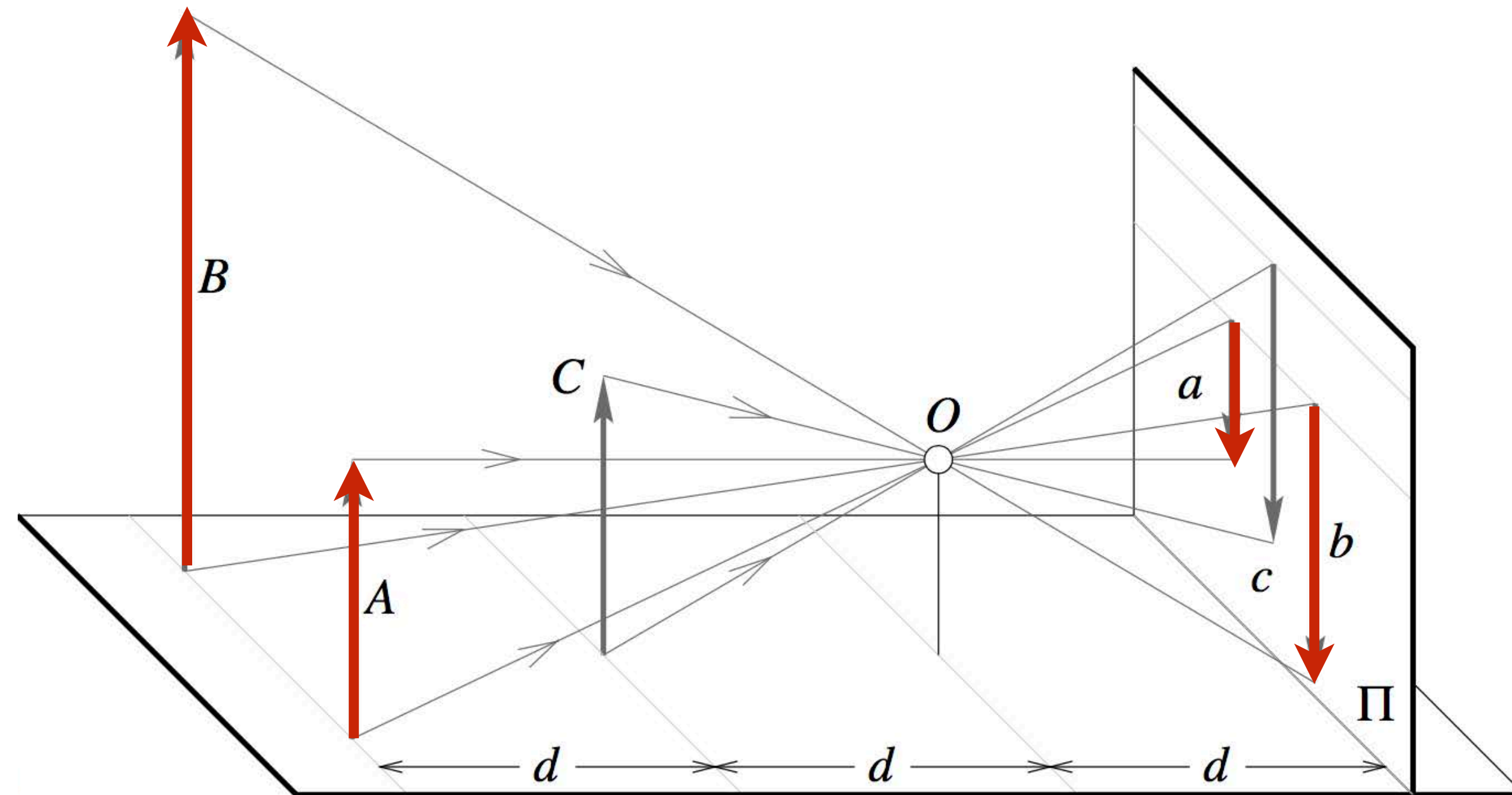
Far objects appear **smaller** than close ones



Forsyth & Ponce (2nd ed.) Figure 1.3a

Perspective Effects

Far objects appear **smaller** than close ones

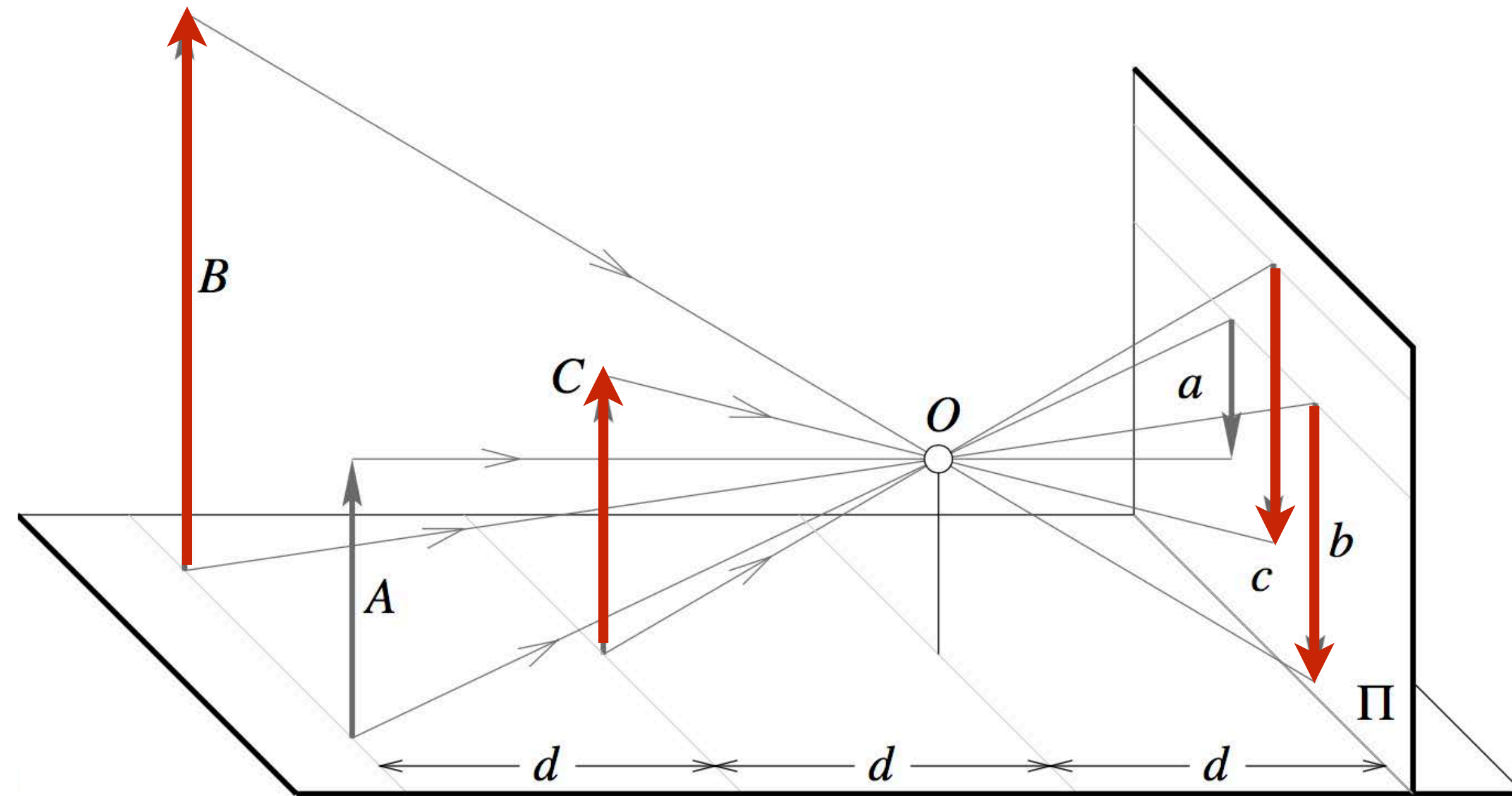


Forsyth & Ponce (2nd ed.) Figure 1.3a

Size is **inversely** proportions to distance

Perspective Effects

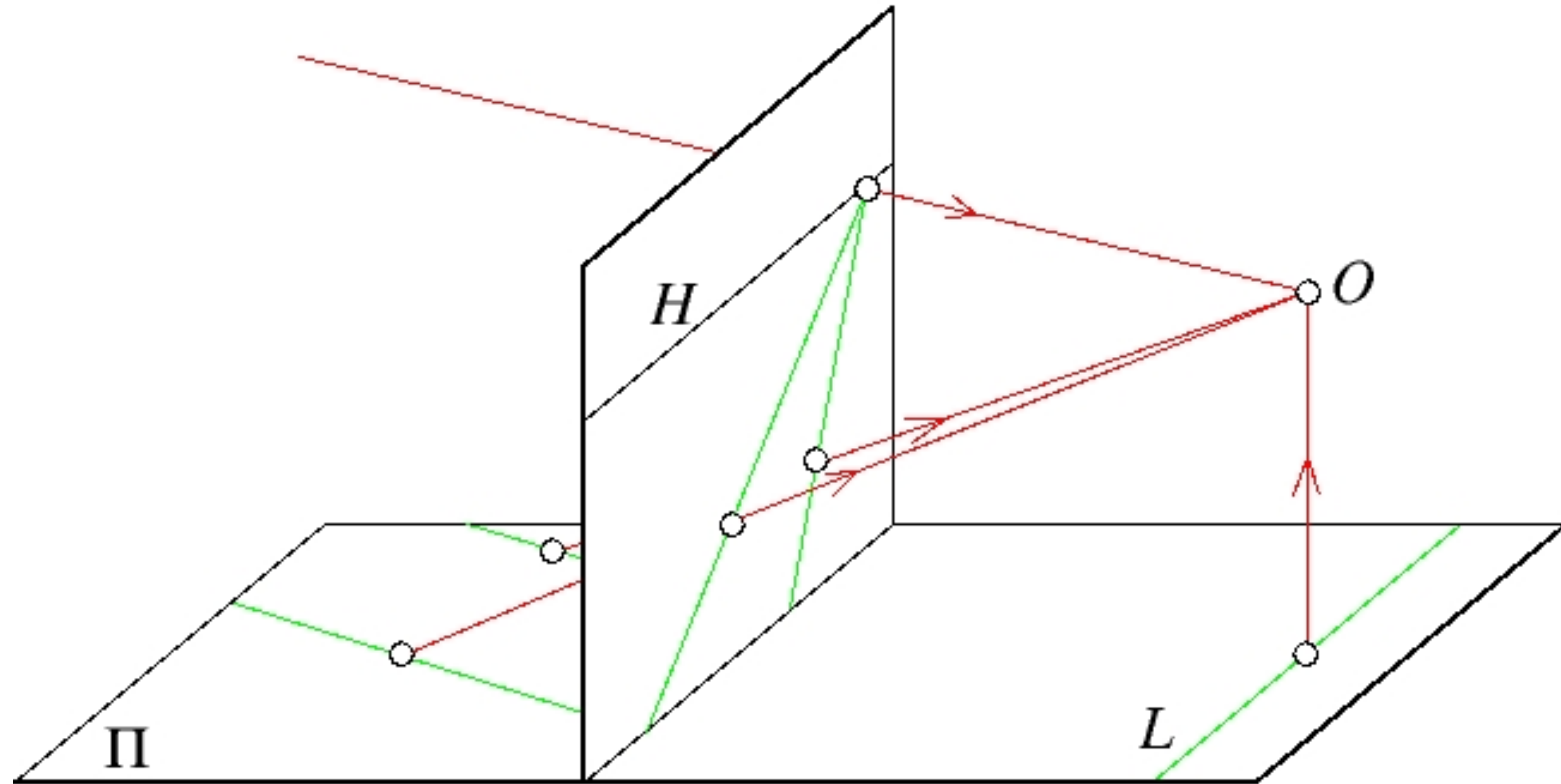
Far objects appear **smaller** than close ones



Forsyth & Ponce (2nd ed.) Figure 1.3a

Perspective Effects

Parallel lines meet at a point (**vanishing point**)



Forsyth & Ponce (1st ed.) Figure 1.3b

Vanishing Points

Each set of parallel lines meet at a different point

— the point is called **vanishing point**

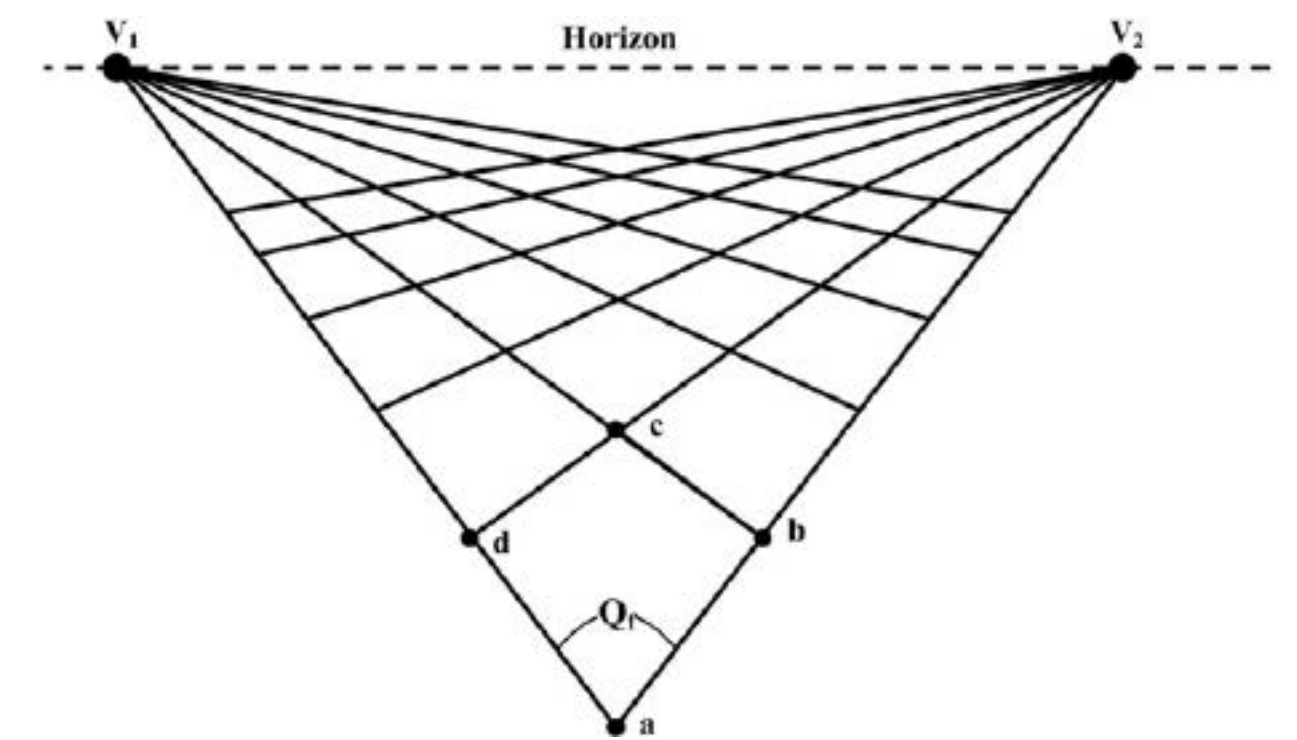
Vanishing Points

Each set of parallel lines meets at a different point

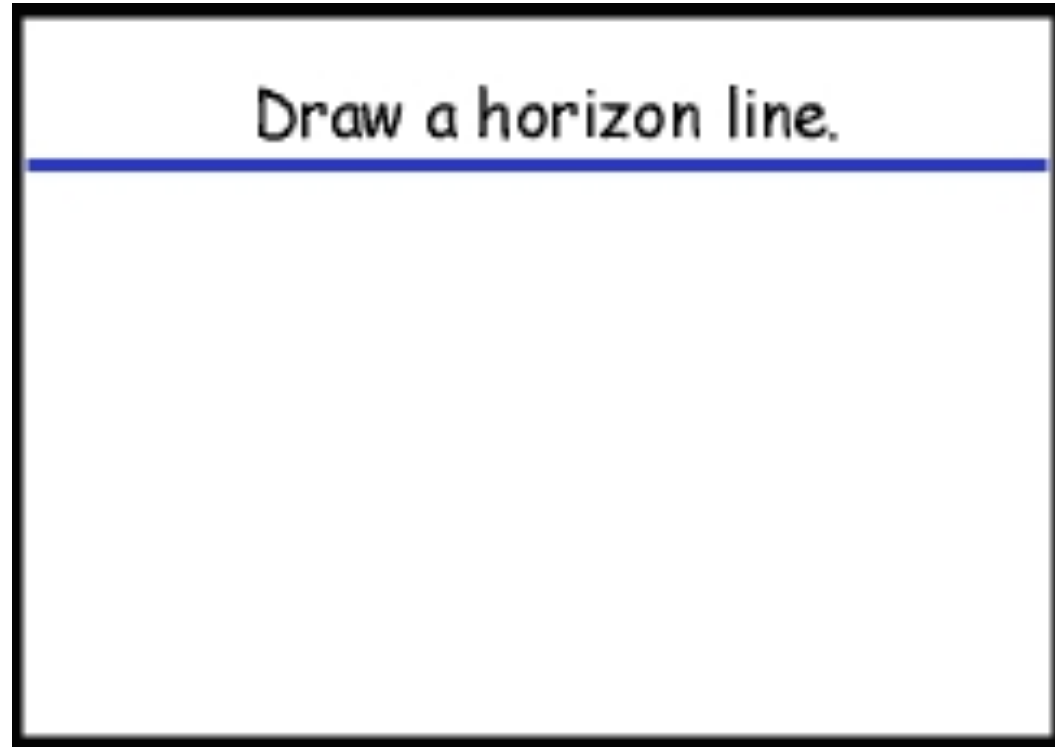
— the point is called the **vanishing point**

Sets of parallel lines on the same plane lead to **collinear** vanishing points

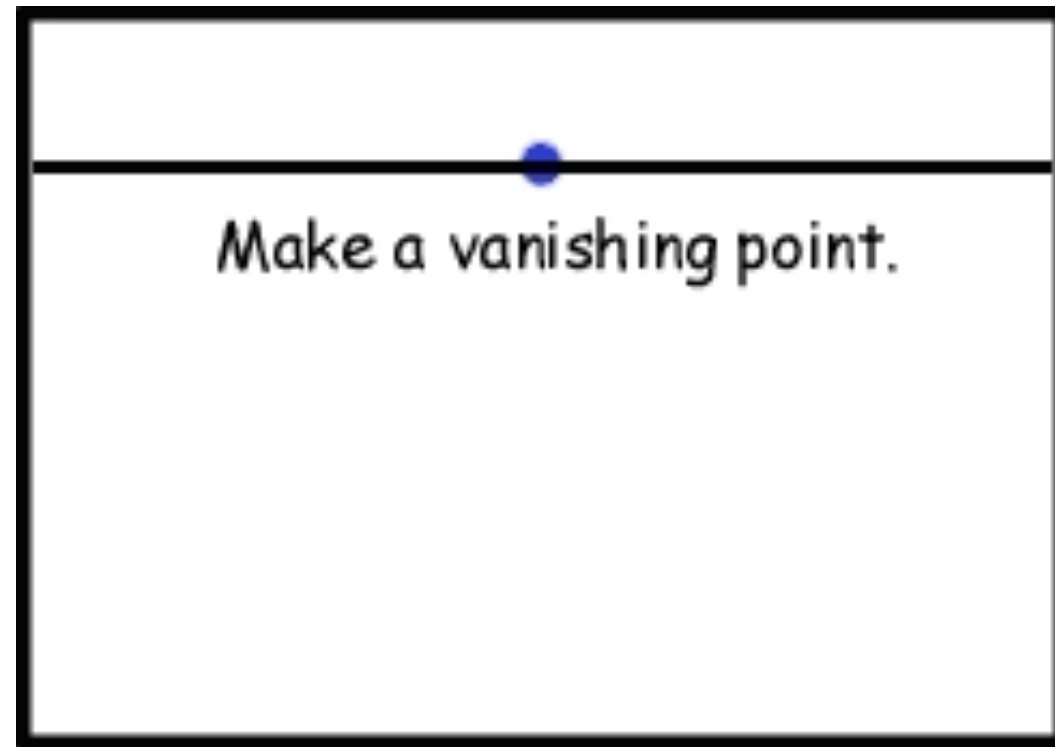
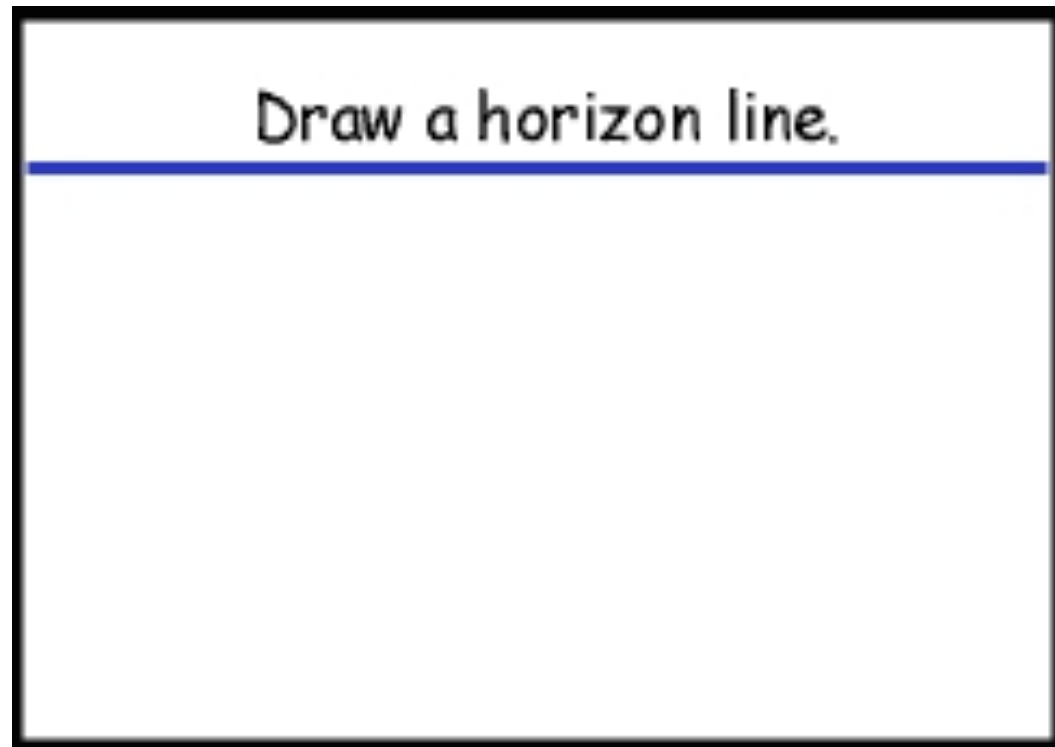
— the line is called a **horizon** for that plane



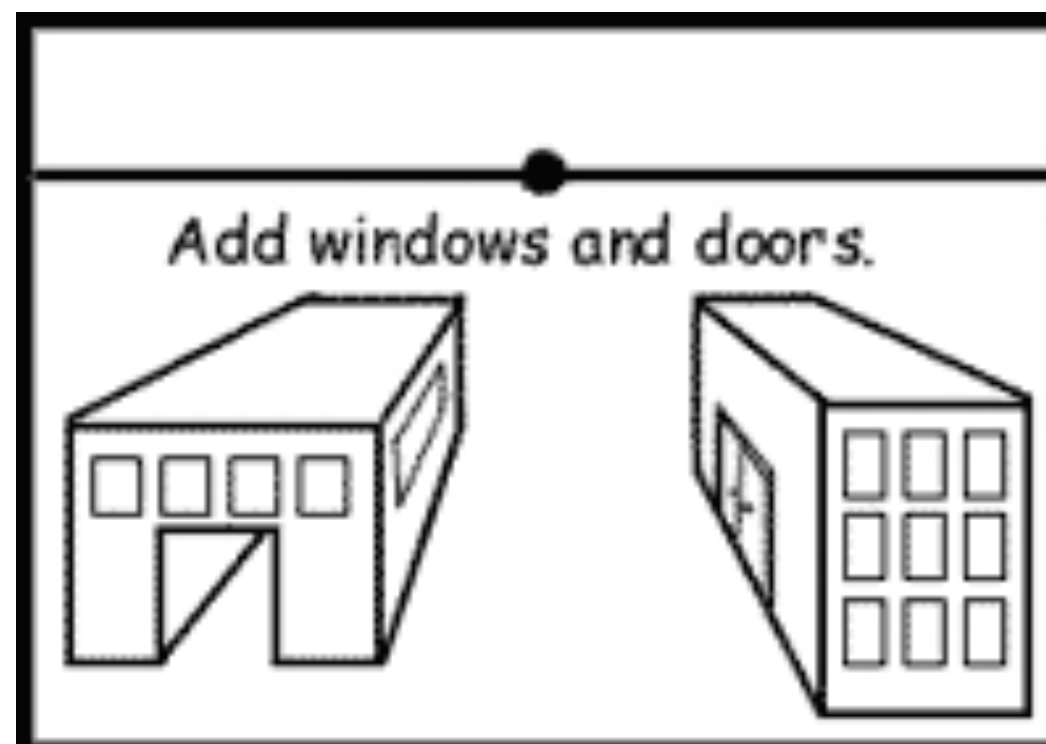
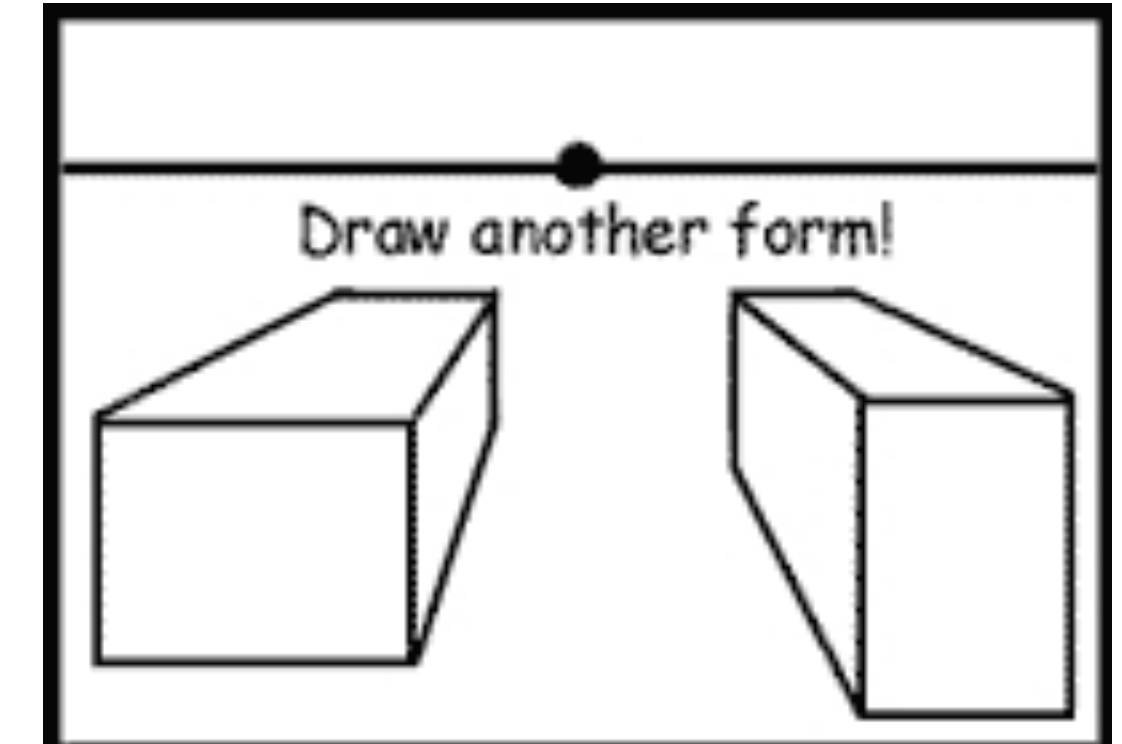
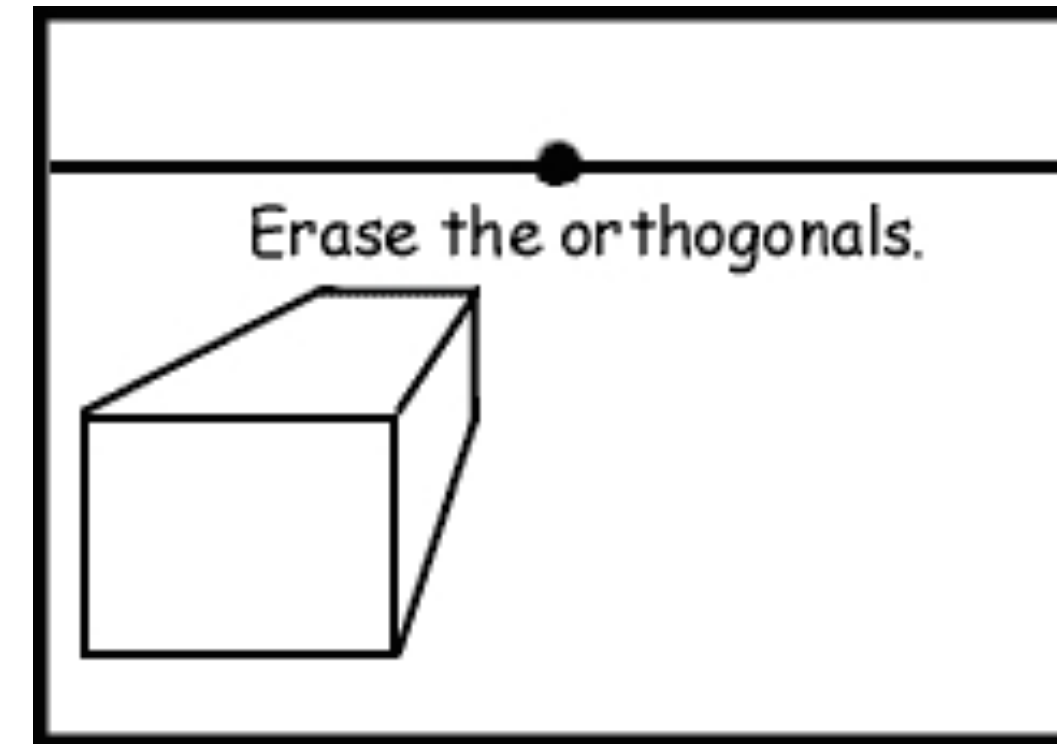
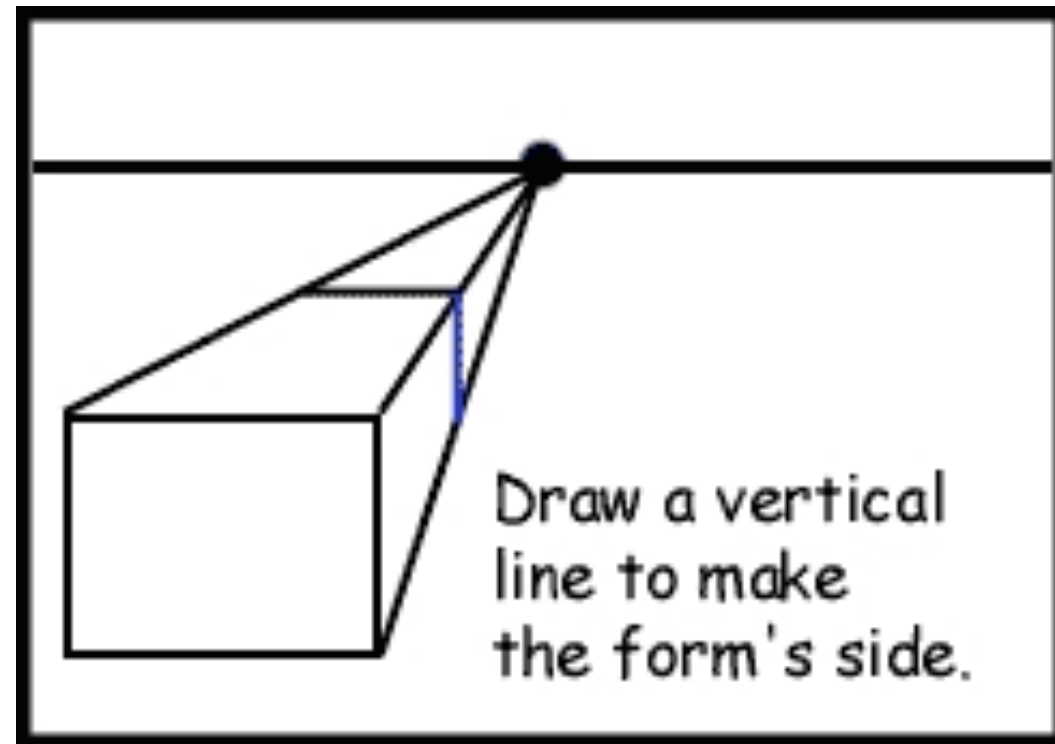
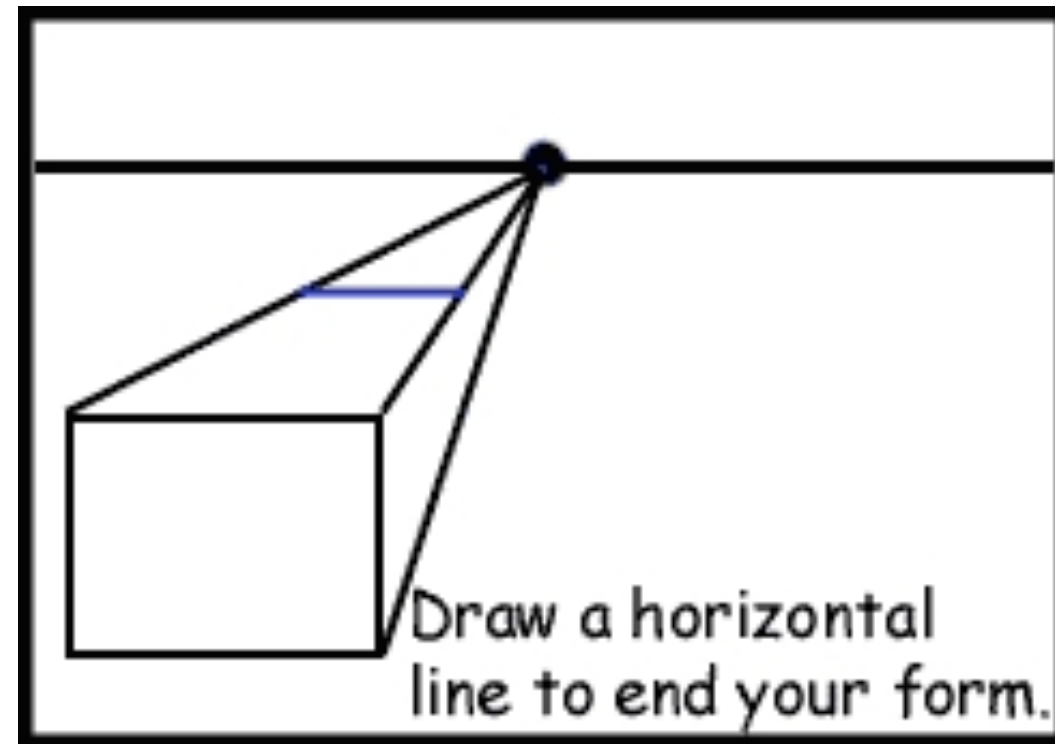
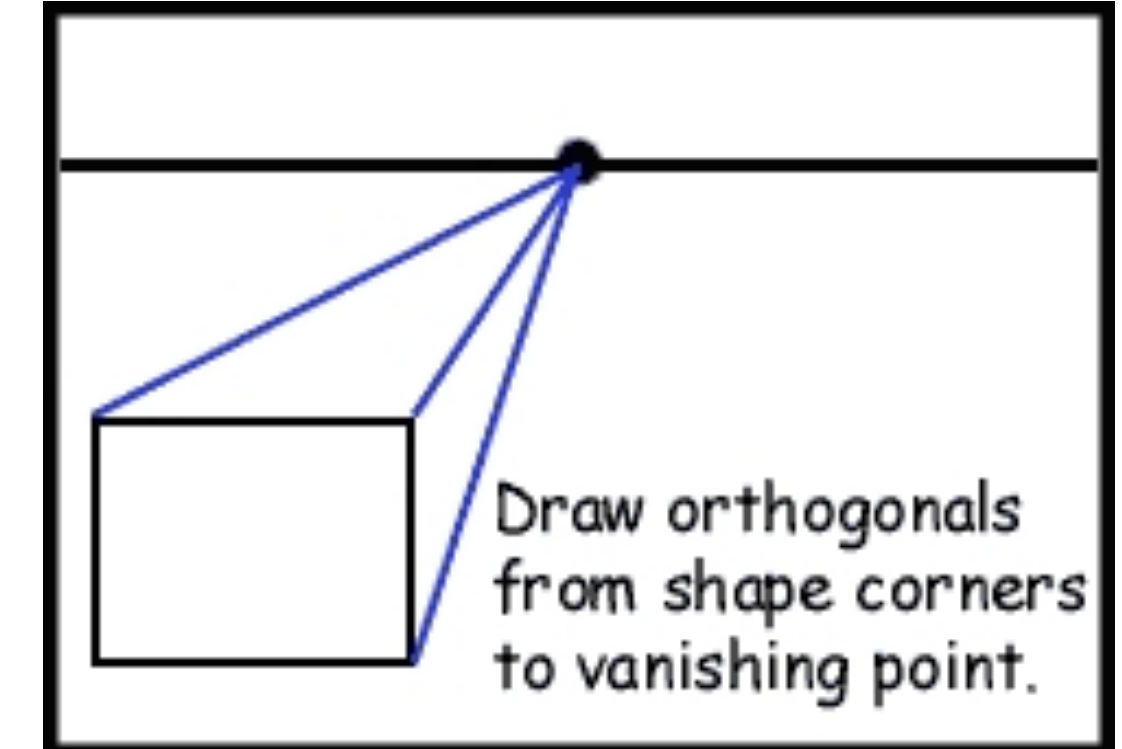
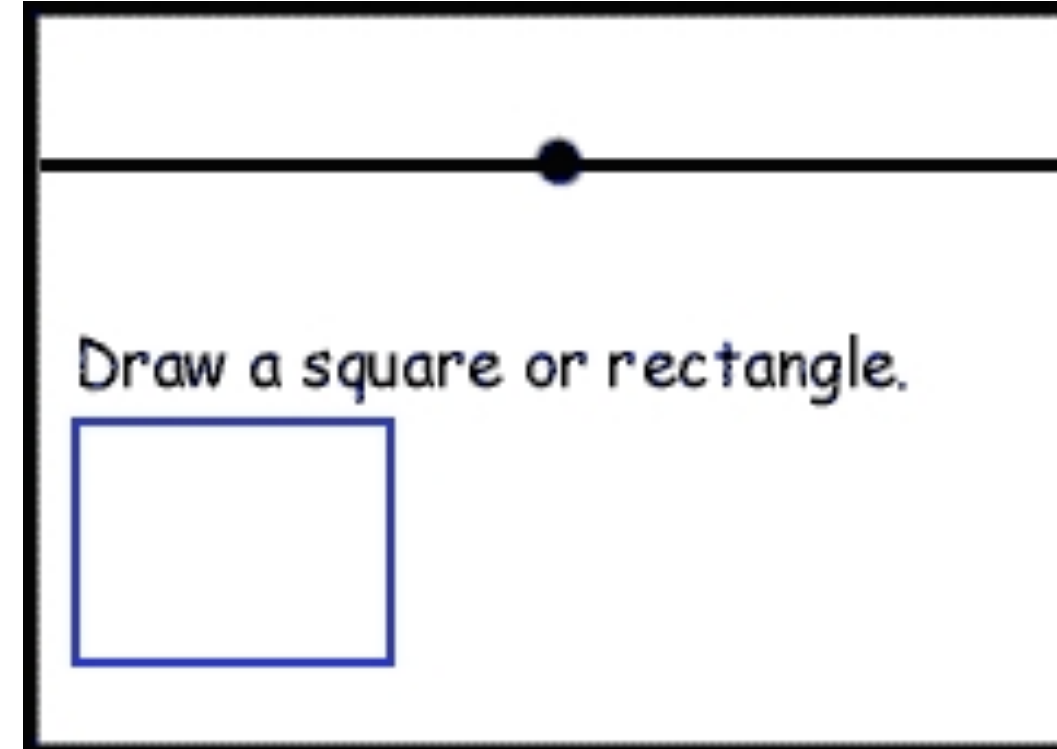
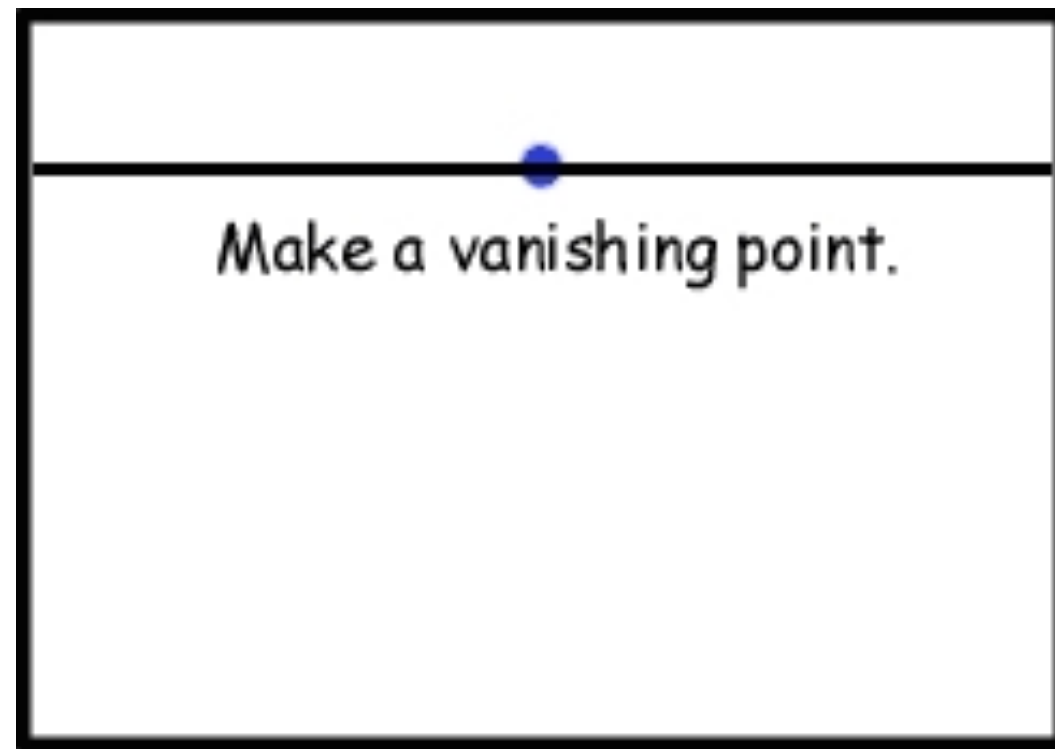
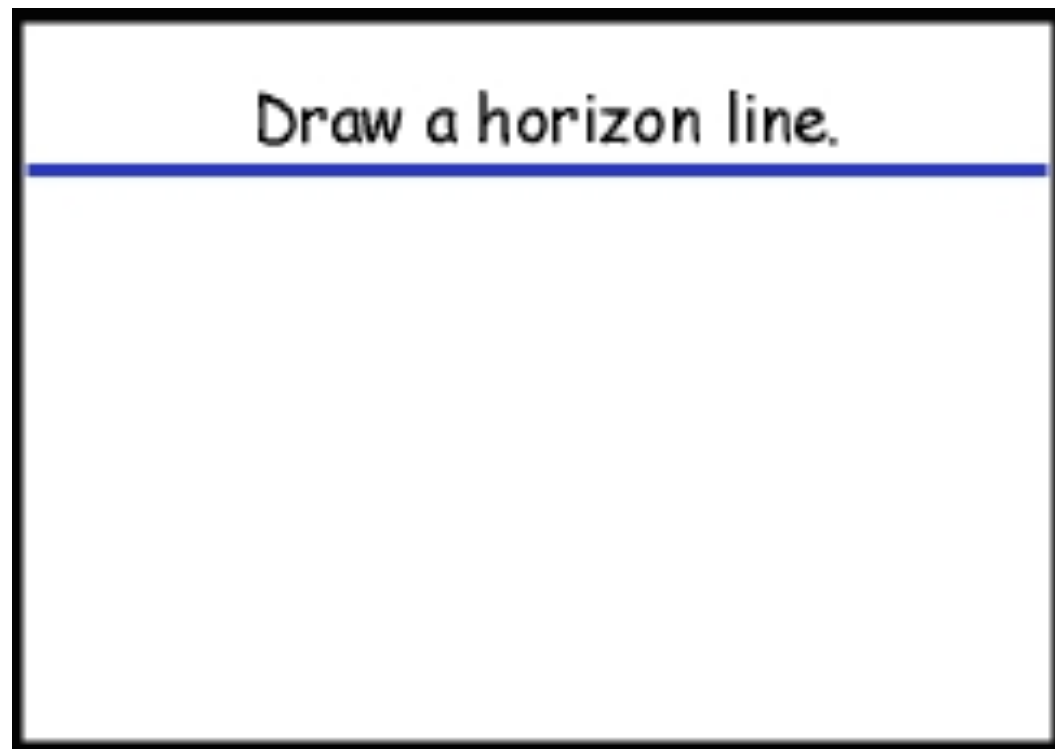
Vanishing Points



Vanishing Points



Vanishing Points



Vanishing Points

Each set of parallel lines meets at a different point

— the point is called the **vanishing point**

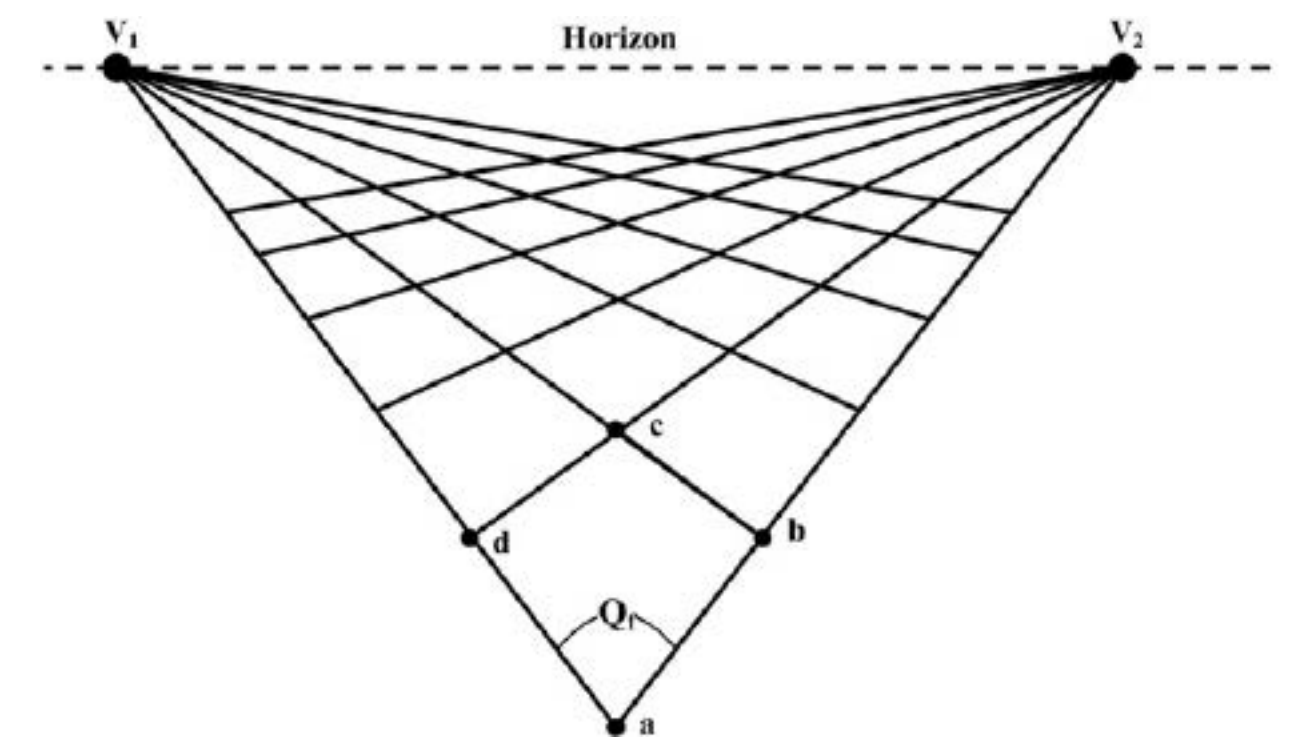
Sets of parallel lines on the same plane lead to **collinear** vanishing points

— the line is called a **horizon** for that plane

A good way to **spot fake images**

— scale and perspective do not work

— vanishing points behave badly



Spotting fake images with **Vanishing** Points



Generated Image

Shadow Errors

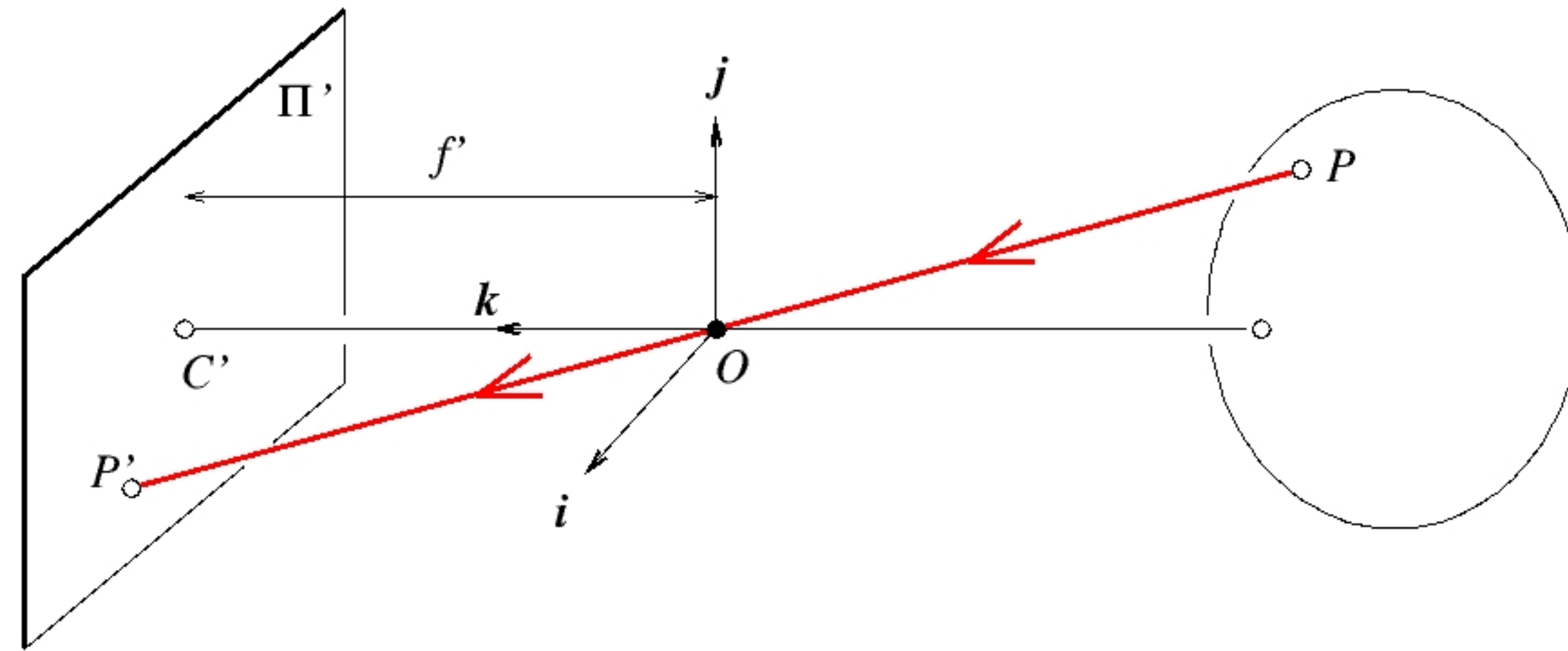
Detected Shadow Errors

Vanishing Point Errors

Detected Perspective Errors

Perspective Projection: Matrix Form

Camera Matrix



$$\mathbf{C} = \begin{bmatrix} f' & 0 & 0 & 0 \\ 0 & f' & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

3D object point

Forsyth & Ponce (1st ed.) Figure 1.4

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

projects to 2D image point

$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$

where

$$sP' = \mathbf{C}P$$

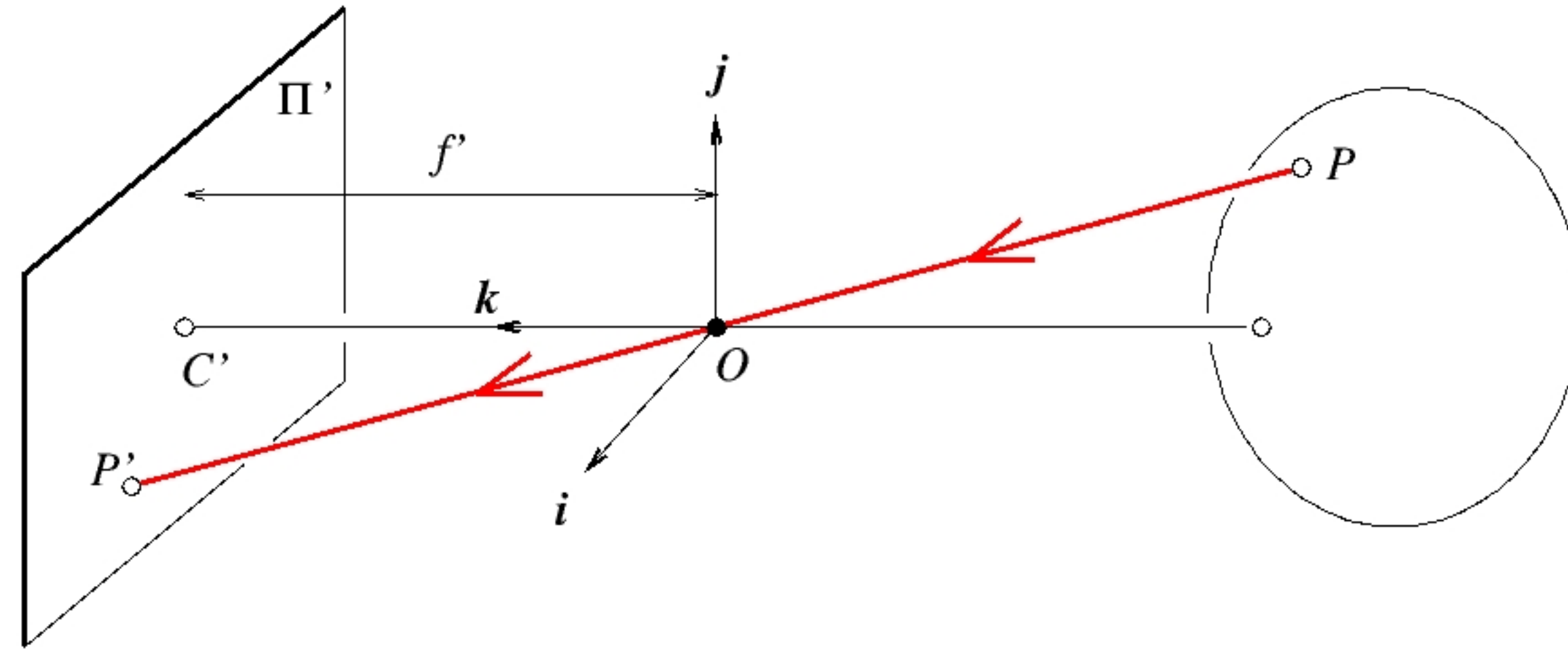
(s is a scale factor)



2.4

Aside: Camera Matrix

Camera Matrix



$$\mathbf{C} = \begin{bmatrix} f' & 0 & 0 & 0 \\ 0 & f' & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

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$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$ projects to 2D image point $P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$ where $P' = \mathbf{C}P$

Aside: Camera Matrix

Camera Matrix

$$\mathbf{C} = \begin{bmatrix} f' & 0 & 0 & 0 \\ 0 & f' & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

Pixels are squared / lens is perfectly symmetric

Sensor and pinhole perfectly aligned

Coordinate system centered at the pinhole

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \text{ projects to 2D image point } P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \text{ where } P' = \mathbf{C}P$$

Aside: Camera Matrix

Camera Matrix

$$\mathbf{C} = \begin{bmatrix} f'_x & 0 & 0 & 0 \\ 0 & f'_y & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

~~Pixels are squared / lens is perfectly symmetric~~

Sensor and pinhole perfectly aligned

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$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \text{ projects to 2D image point } P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \text{ where } P' = \mathbf{C}P$$

Aside: Camera Matrix

Camera Matrix

$$\mathbf{C} = \begin{bmatrix} f'_x & 0 & 0 & c_x \\ 0 & f'_y & 0 & c_y \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

~~Pixels are squared / lens is perfectly symmetric~~

~~Sensor and pinhole perfectly aligned~~

Coordinate system centered at the pinhole

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \text{ projects to 2D image point } P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \text{ where } P' = \mathbf{C}P$$

Aside: Camera Matrix

Camera Matrix

$$\mathbf{C} = \begin{bmatrix} f'_x & 0 & 0 & c_x \\ 0 & f'_y & 0 & c_y \\ 0 & 0 & 1 & 0 \end{bmatrix} \mathbb{R}_{4 \times 4}$$

~~Pixels are squared / lens is perfectly symmetric~~

~~Sensor and pinhole perfectly aligned~~

~~Coordinate system centered at the pinhole~~

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \text{ projects to 2D image point } P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \text{ where } P' = \mathbf{C}P$$

Aside: Camera Matrix

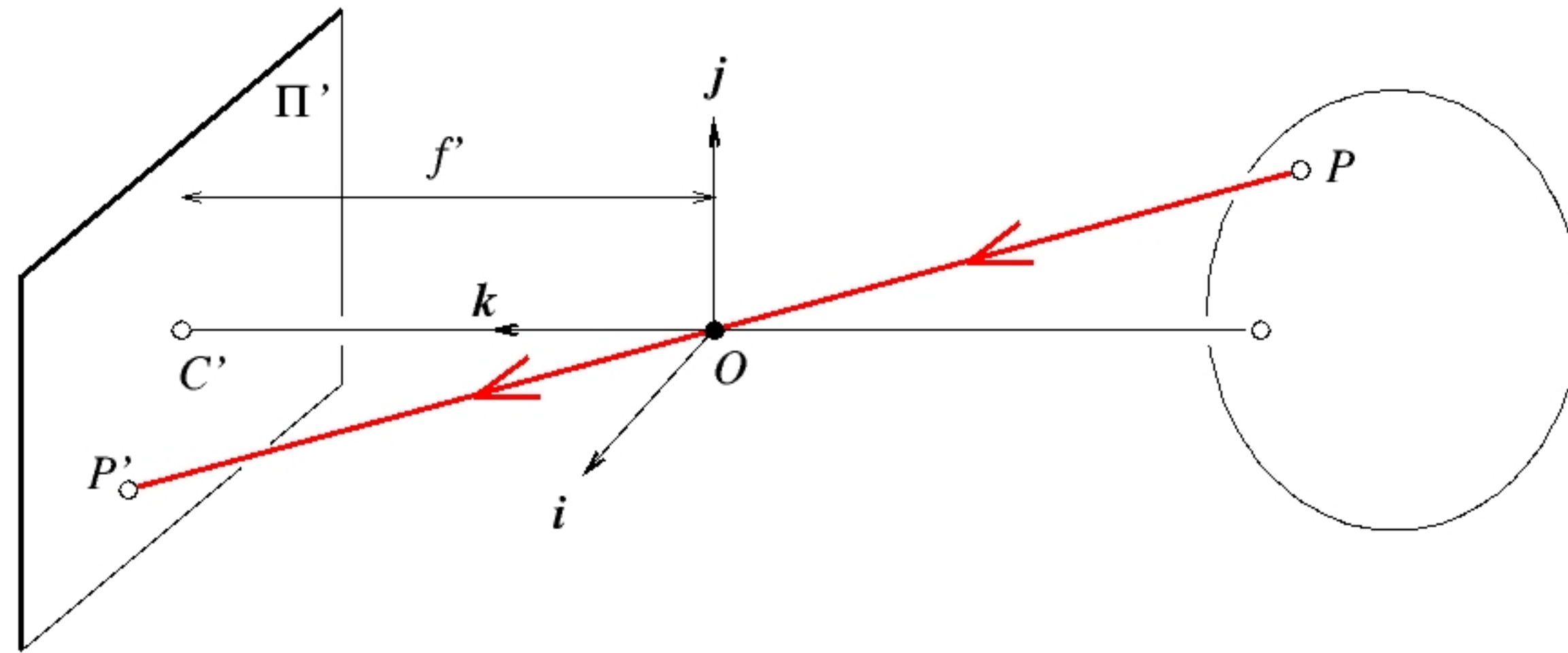
Camera Matrix

$$\mathbf{C} = \begin{bmatrix} f'_x & 0 & 0 & c_x \\ 0 & f'_y & 0 & c_y \\ 0 & 0 & 1 & 0 \end{bmatrix} \mathbb{R}_{4 \times 4}$$

Camera calibration is the process of estimating the parameters of the camera matrix based on a set of 3D-2D correspondences (usually requires a pattern whose structure and size are known)

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \text{ projects to 2D image point } P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \text{ where } P' = \mathbf{C}P$$

Perspective Projection



3D object point

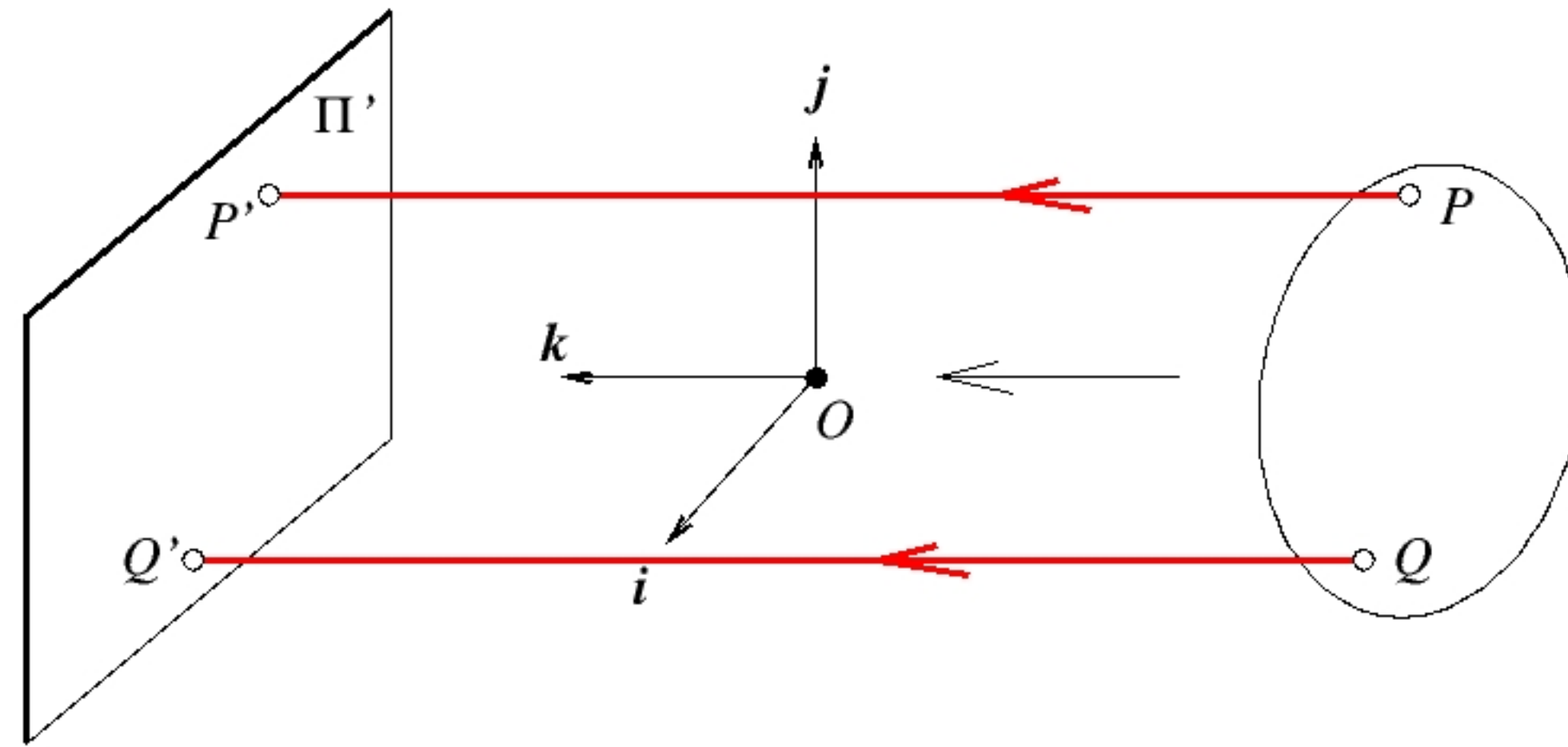
Forsyth & Ponce (1st ed.) Figure 1.4

$P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ projects to 2D image point $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$ where

$$\begin{aligned} x' &= f' \frac{x}{z} \\ y' &= f' \frac{y}{z} \end{aligned}$$

Note: this assumes world coordinate frame at the optical center (pinhole) and aligned with the image plane, image coordinate frame aligned with the camera coordinate frame

Orthographic Projection



Forsyth & Ponce (1st ed.) Figure 1.6

3D object point $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ projects to 2D image point $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$

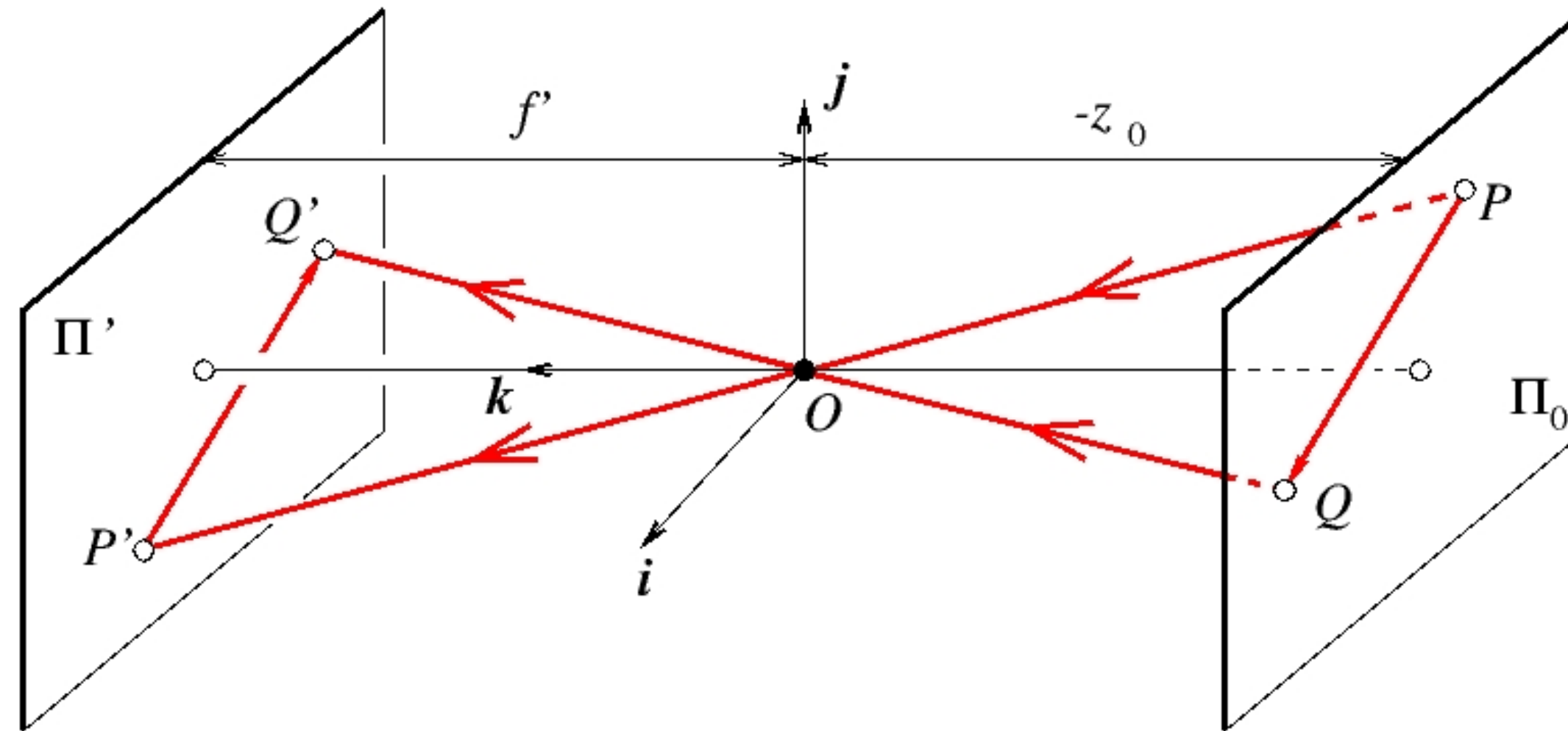
where

$$\begin{array}{l} x' = x \\ y' = y \end{array}$$

Weak Perspective



3.1



Forsyth & Ponce (1st ed.) Figure 1.5

3D object point $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ in Π_0 projects to 2D image point $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$

where $\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} mx \\ my \end{bmatrix}$ and $m = \frac{f'}{z_0}$

Summary of **Projection Equations**

3D object point $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ projects to 2D image point $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$ where

Perspective

$$\begin{aligned} x' &= f' \frac{x}{z} \\ y' &= f' \frac{y}{z} \end{aligned}$$

Weak Perspective

$$\begin{aligned} x' &= m x \\ y' &= m y \end{aligned} \quad m = \frac{f'}{z_0}$$

Orthographic

$$\begin{aligned} x' &= x \\ y' &= y \end{aligned}$$

Projection Models: Pros and Cons

Weak perspective (including orthographic) has simpler mathematics

- accurate when object is small and/or distant
- useful for recognition

Perspective is more accurate for real scenes

When **maximum accuracy** is required, it is necessary to model additional details of a particular camera

- use perspective projection with additional parameters (e.g., lens distortion)

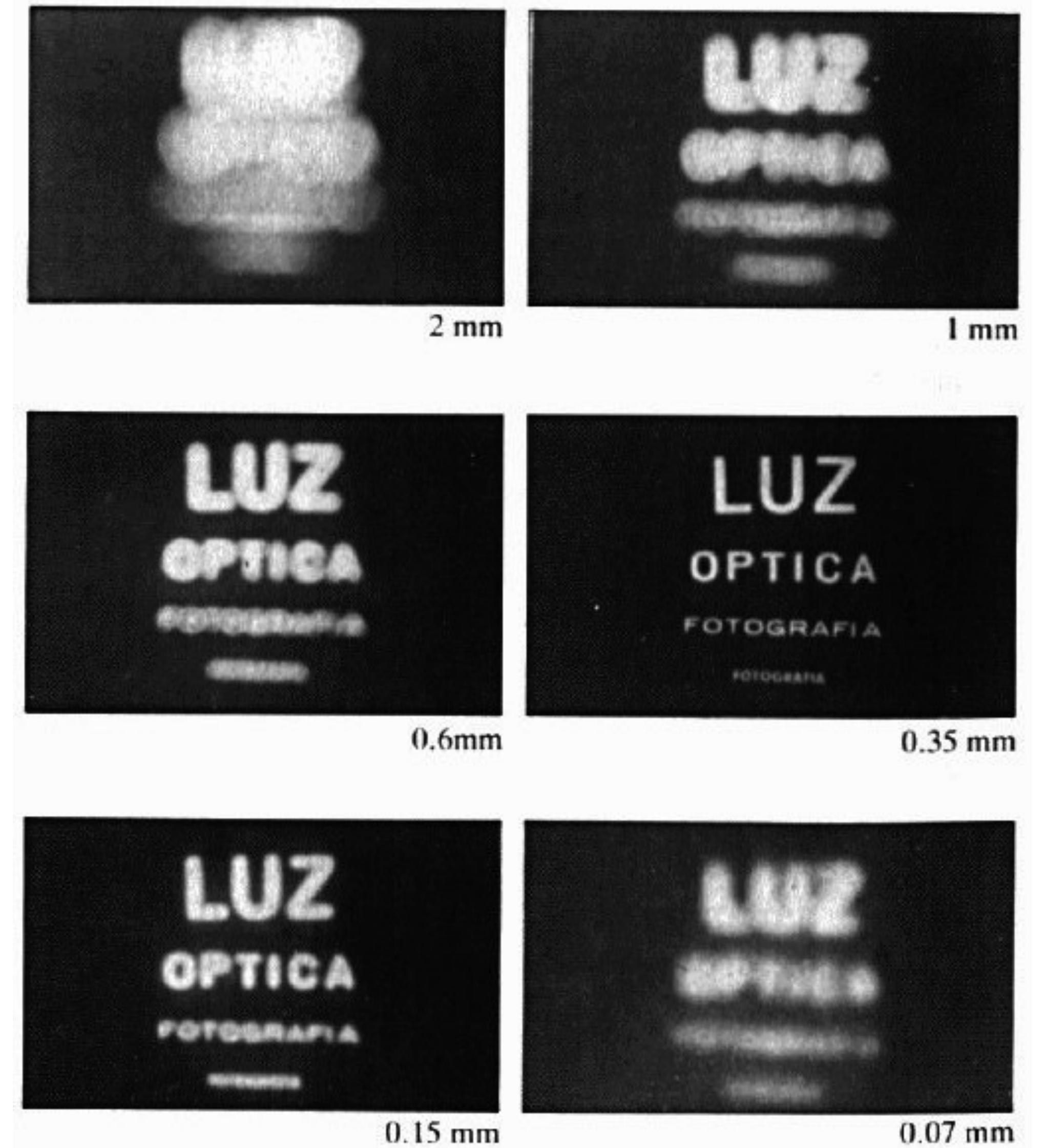
Projection Illusion



Our brains also know this perspective model very well!

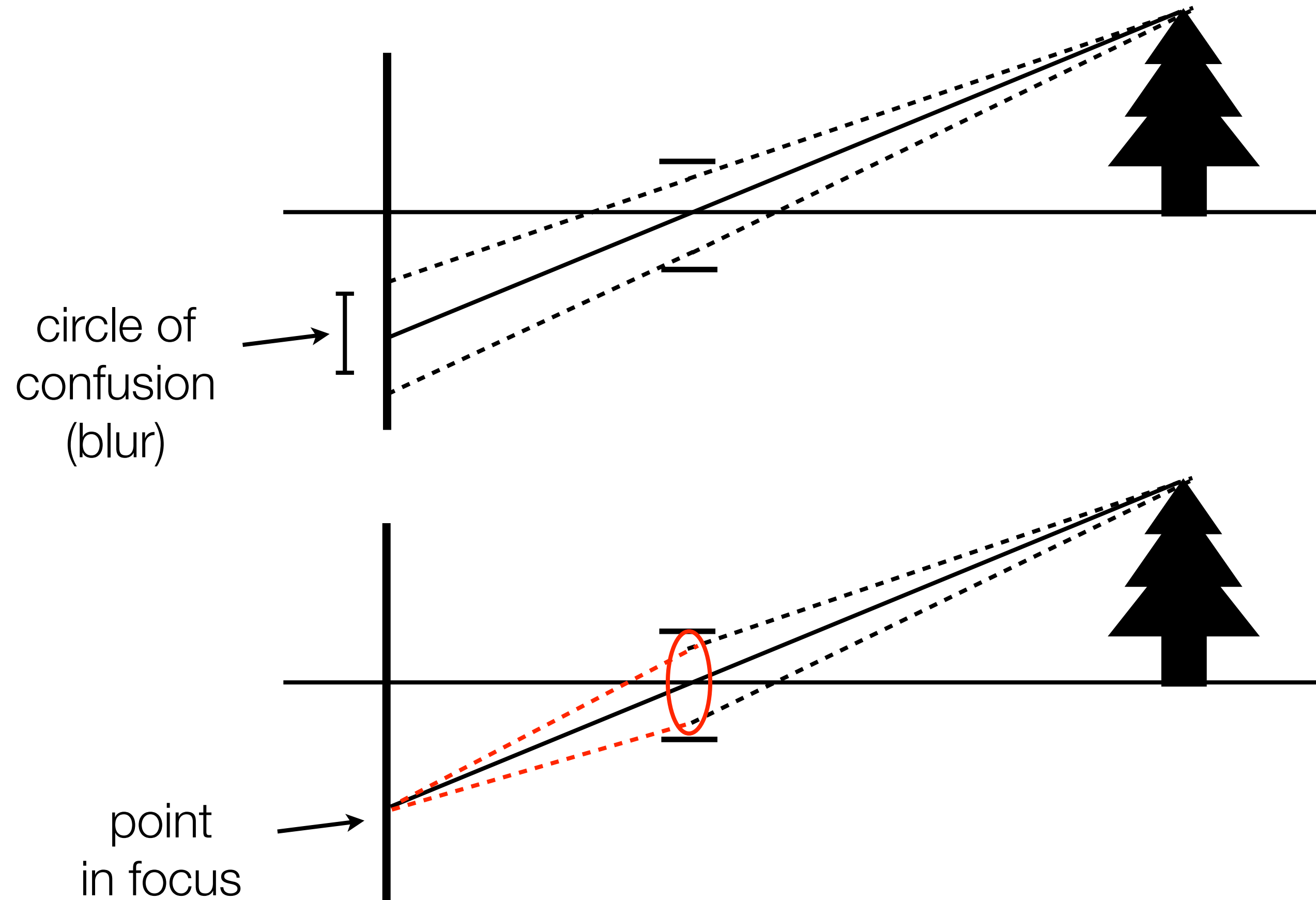
Why **Not** a Pinhole Camera?

- If pinhole is **too big** then many directions are averaged, blurring the image
- If pinhole is **too small** then diffraction becomes a factor, also blurring the image
- Generally, pinhole cameras are **dark**, because only a very small set of rays from a particular scene point hits the image plane
- Pinhole cameras are **slow**, because only a very small amount of light from a particular scene point hits the image plane per unit time



Reason for **Lenses**

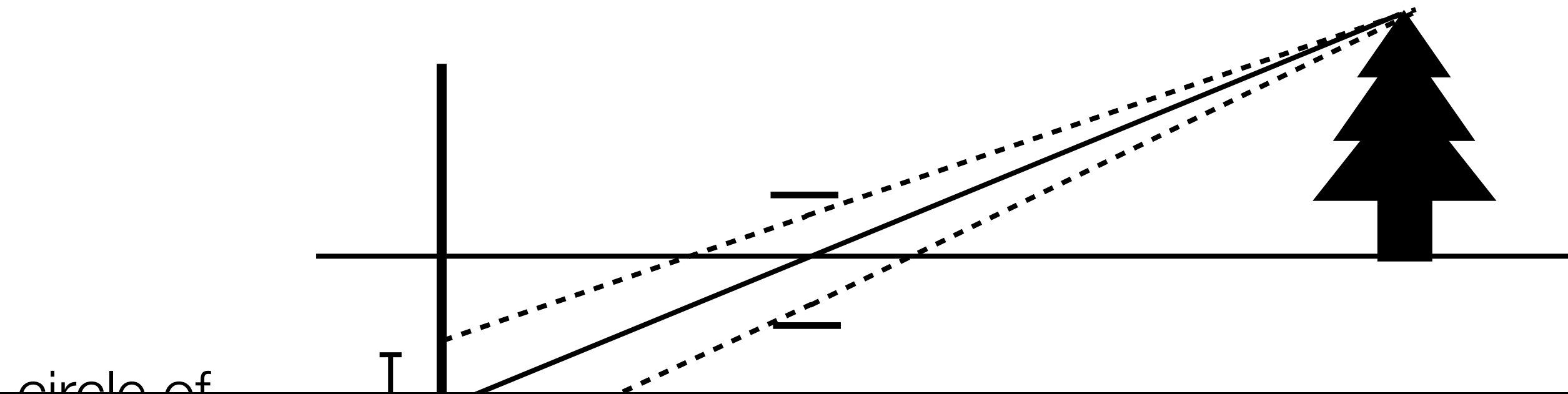
A real camera must have a finite aperture to get enough light, but this causes blur in the image



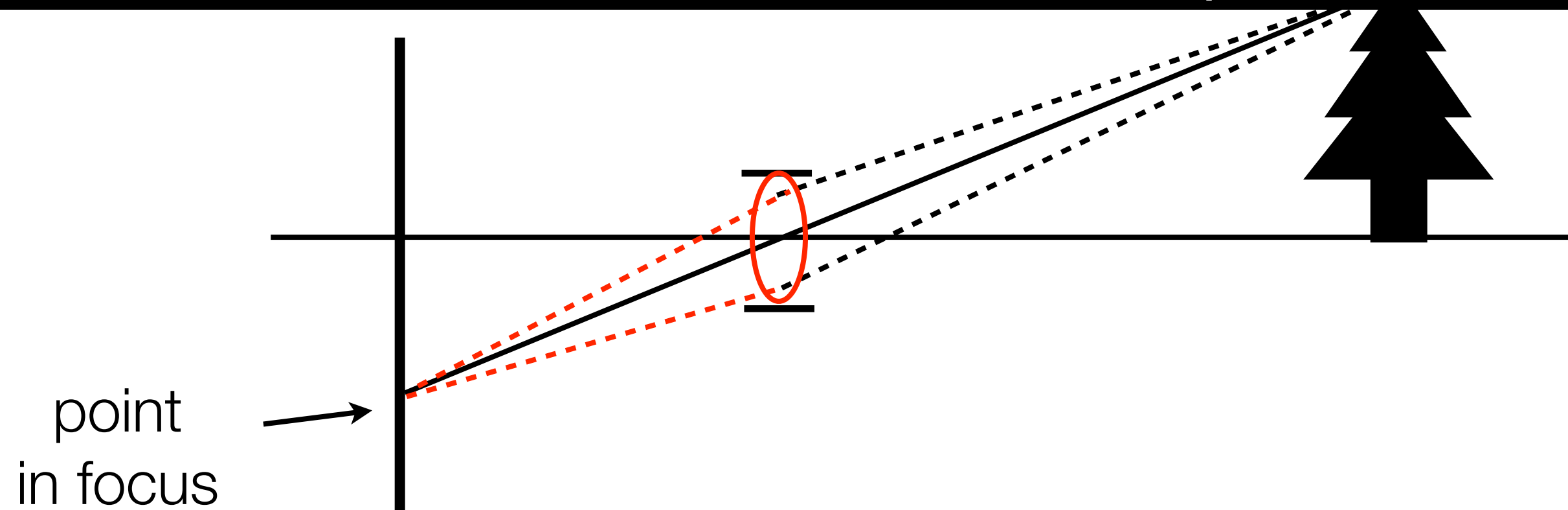
Solution: use a **lens** to focus light onto the image plane

Reason for **Lenses**

A real camera must have a finite aperture to get enough light, but this causes blur in the image

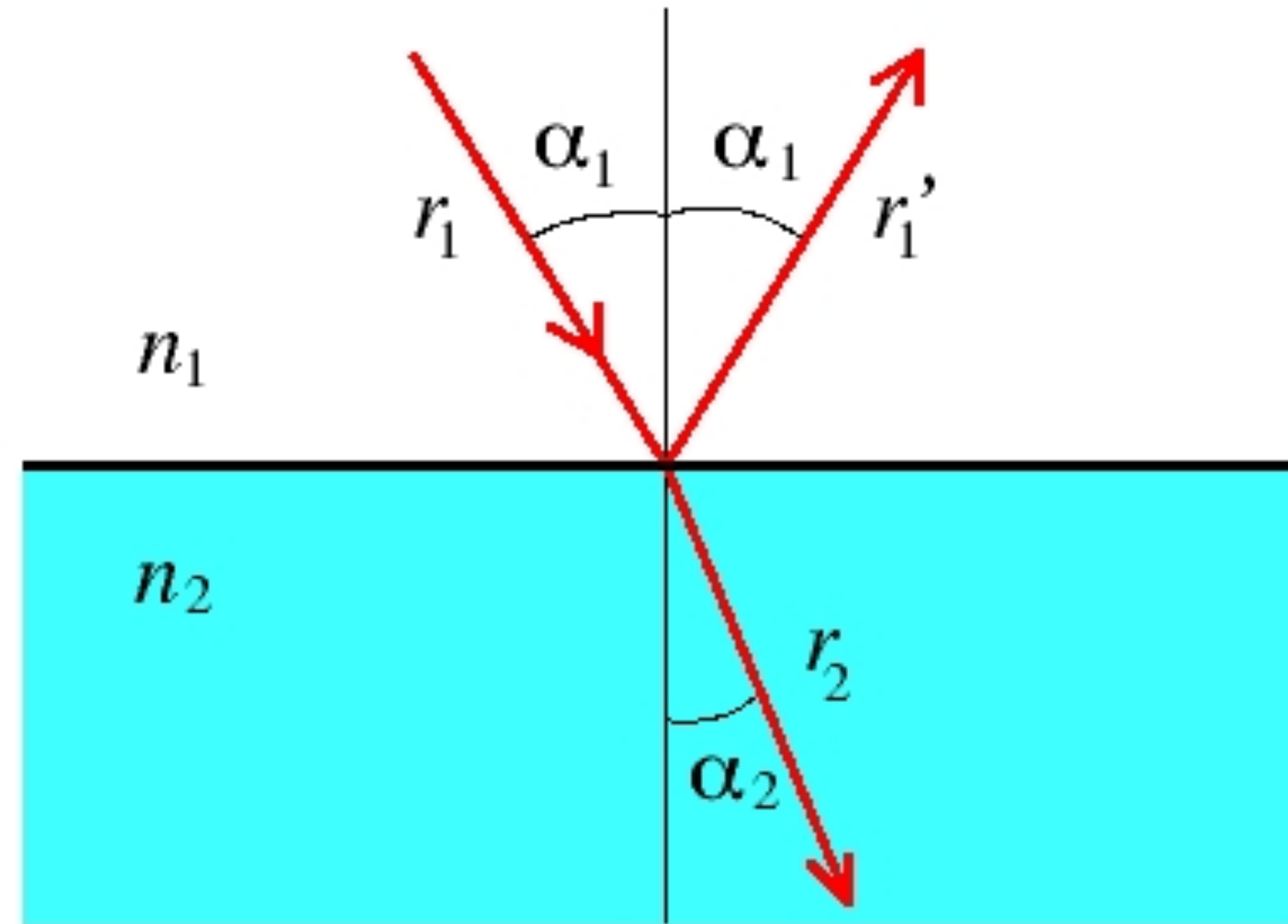


The role of a lens is to **capture more light** while preserving, as much as possible, the abstraction of an ideal pinhole camera.



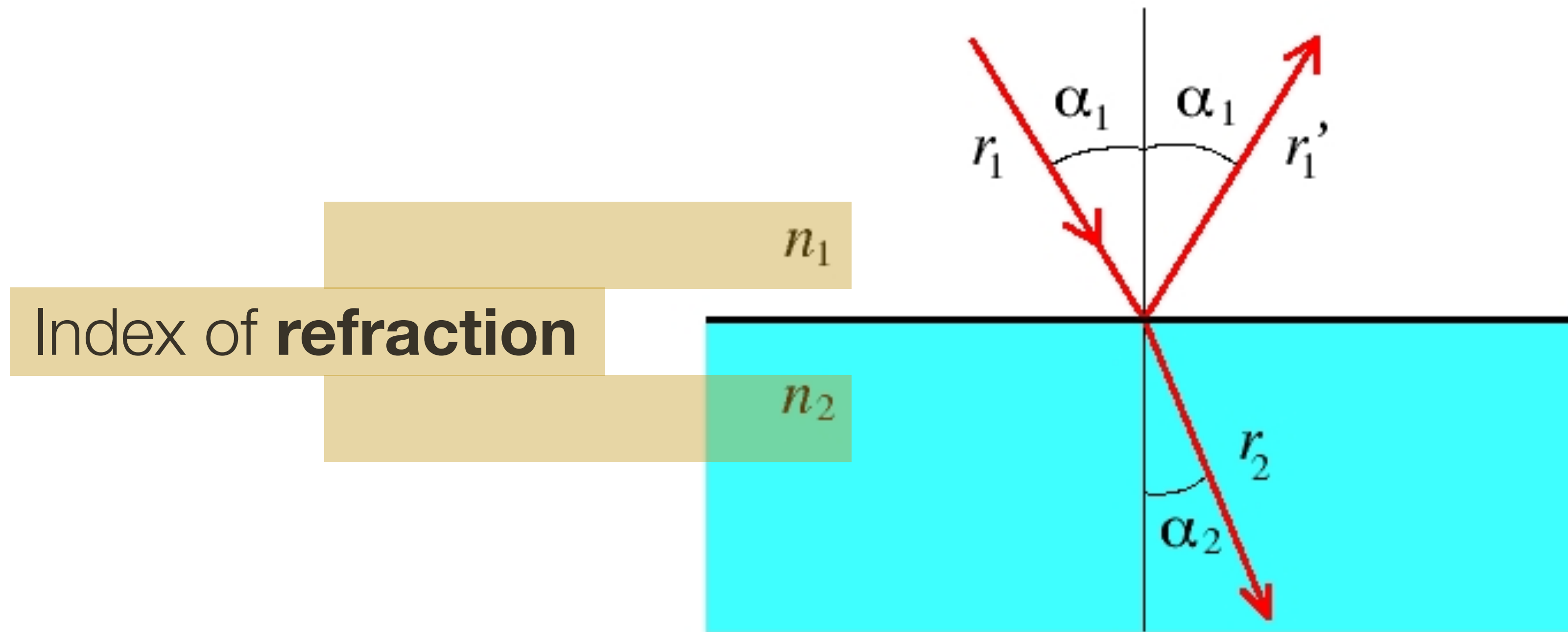
Solution: use a **lens** to focus light onto the image plane

Snell's Law



$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

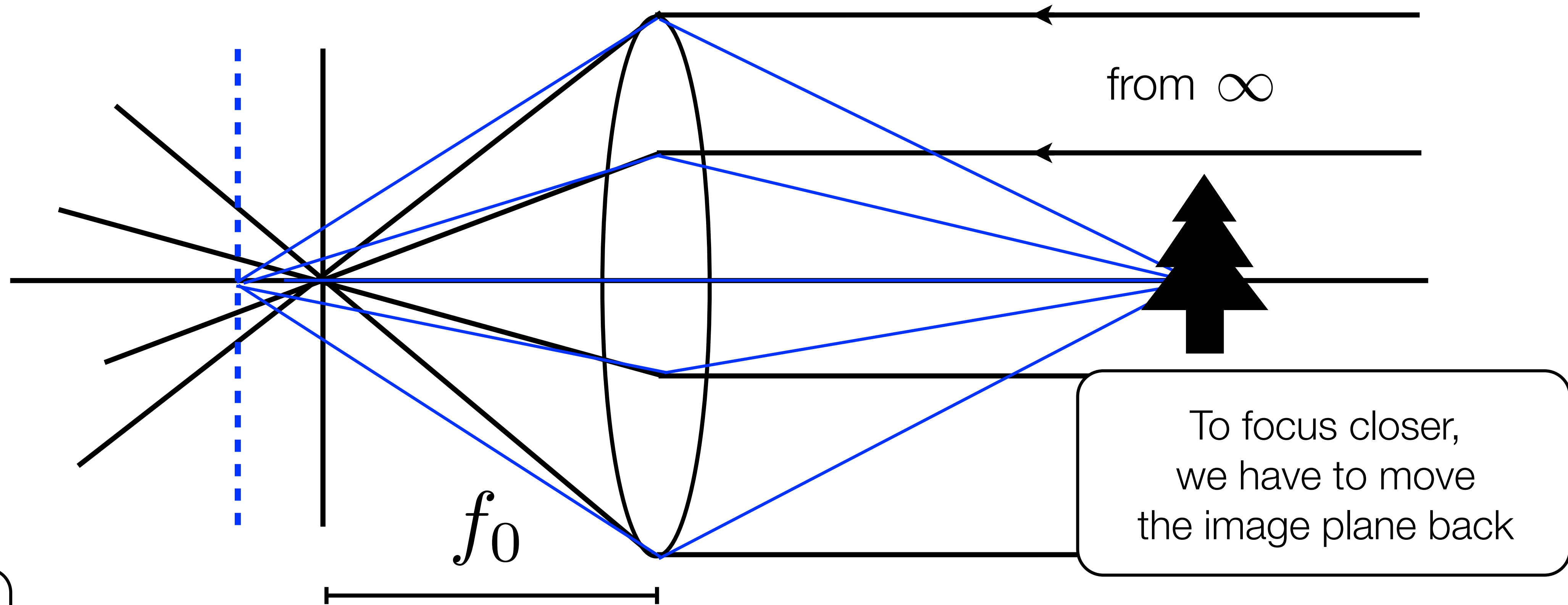
Snell's Law



$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

Lens Basics

- A lens focuses rays from infinity at the focal length of the lens
- Points passing through the centre of the lens are not bent



2.6

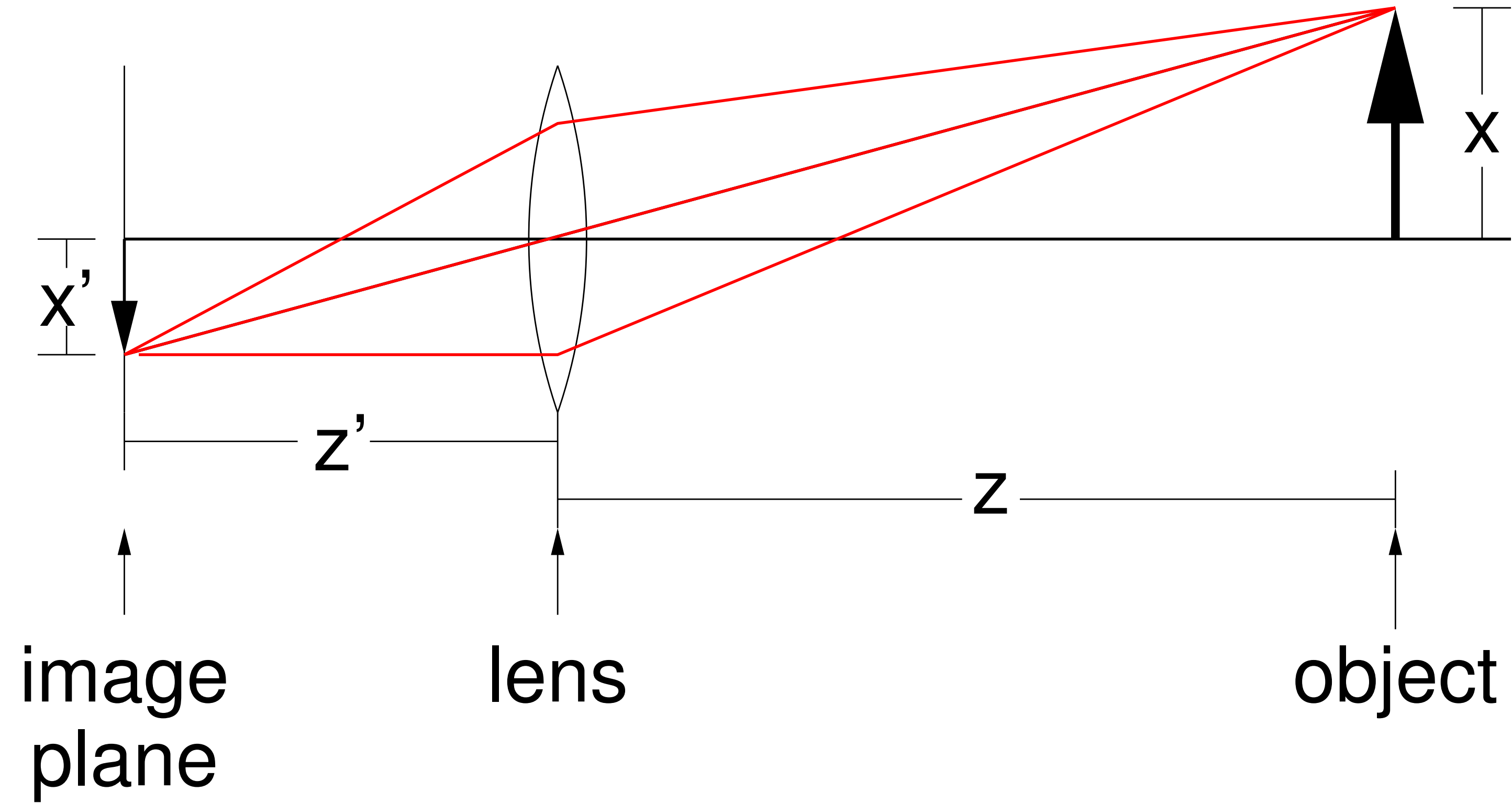
- We can use these 2 properties to find the **thin** lens equation

Lens Basics

- A 50mm lens is focussed at infinity. It now moves to focus on something 5m away. How far does the lens move?

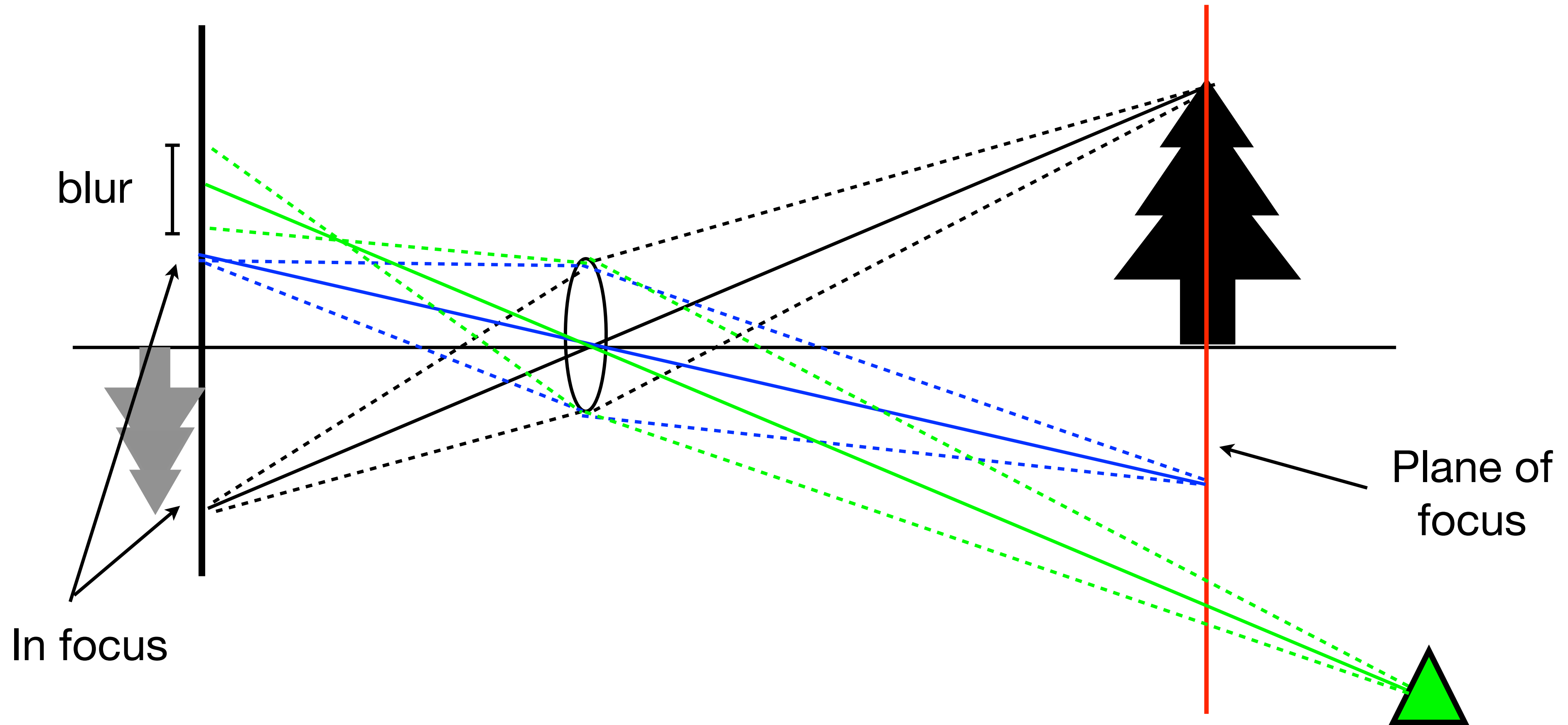


Pinhole Model **with Lens**



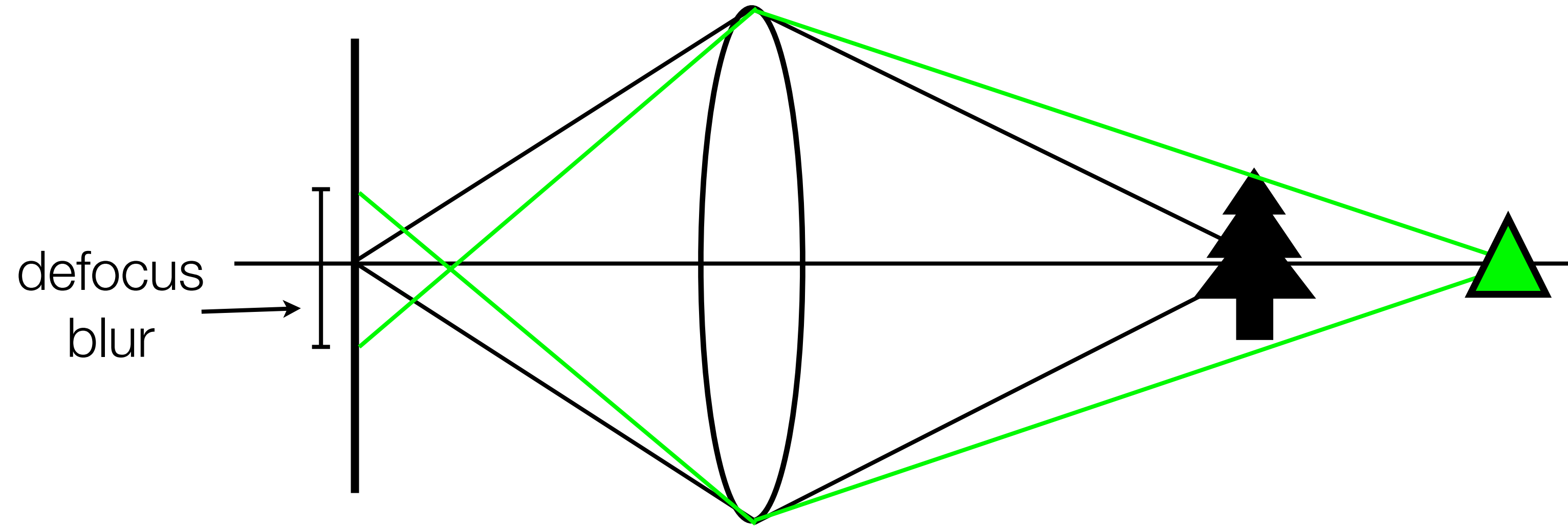
Lens Basics

- Lenses focus all rays from a plane in the world

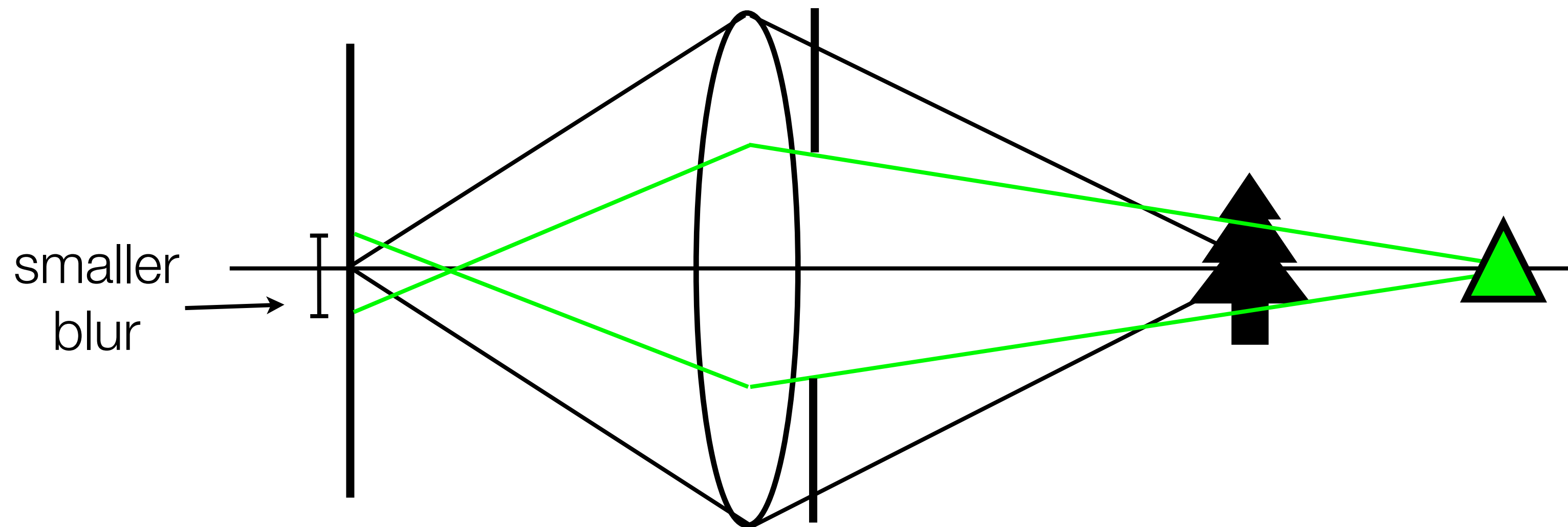


- Objects off the plane are blurred depending on distance

Effect of Aperture Size



Smaller aperture \Rightarrow smaller blur, larger **depth of field**



Depth of Field

- Photographers use large apertures to give small depth of field



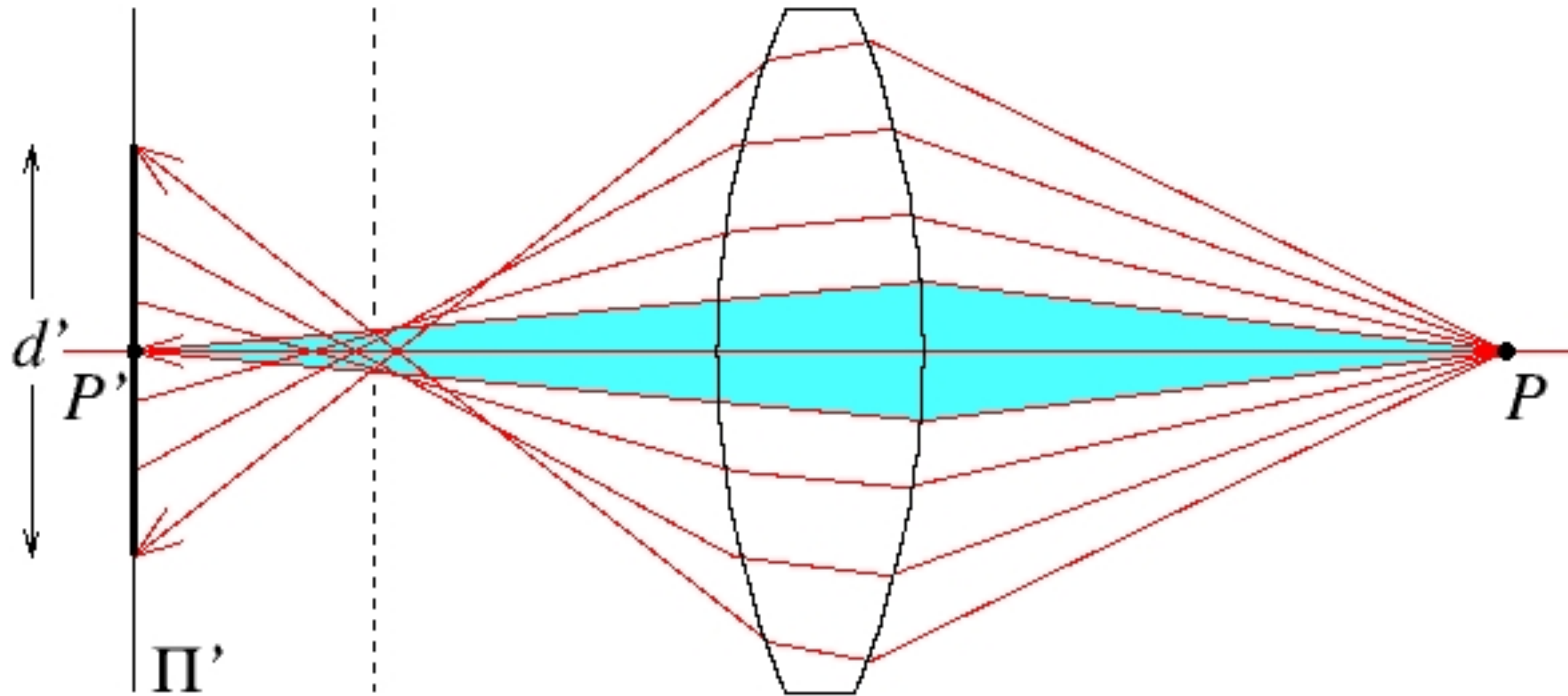
Aperture size = f/N , \Rightarrow large N = small aperture

Real Lenses



- Real Lenses have multiple stages of positive and negative elements with differing refractive indices
- This can help deal with issues such as chromatic aberration (different colours bent by different amounts), vignetting (light fall off at image edge) and sharp imaging across the zoom range

Spherical Aberration



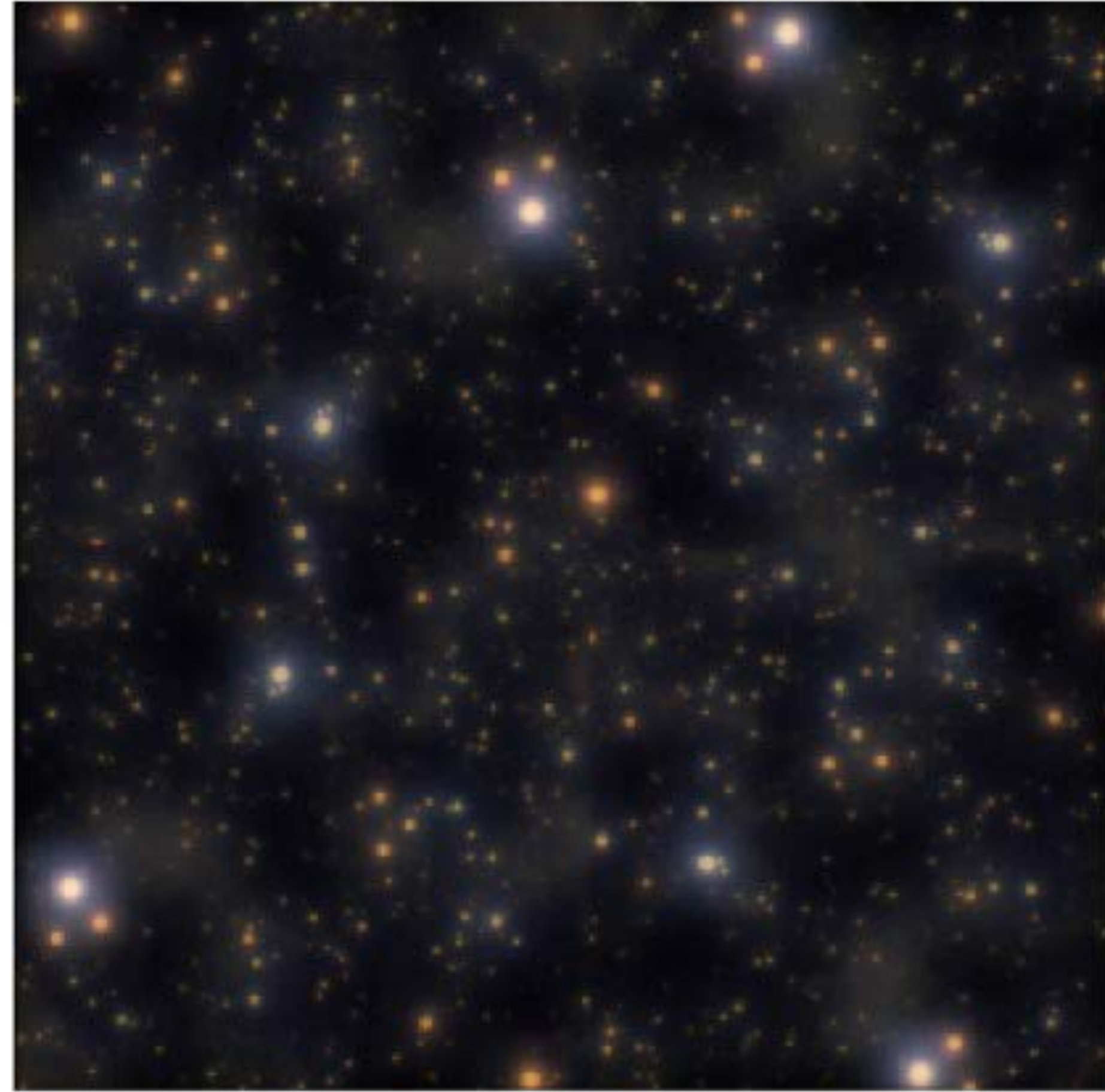
Forsyth & Ponce (1st ed.) Figure 1.12a

Spherical **Aberration**

Un-aberrated image

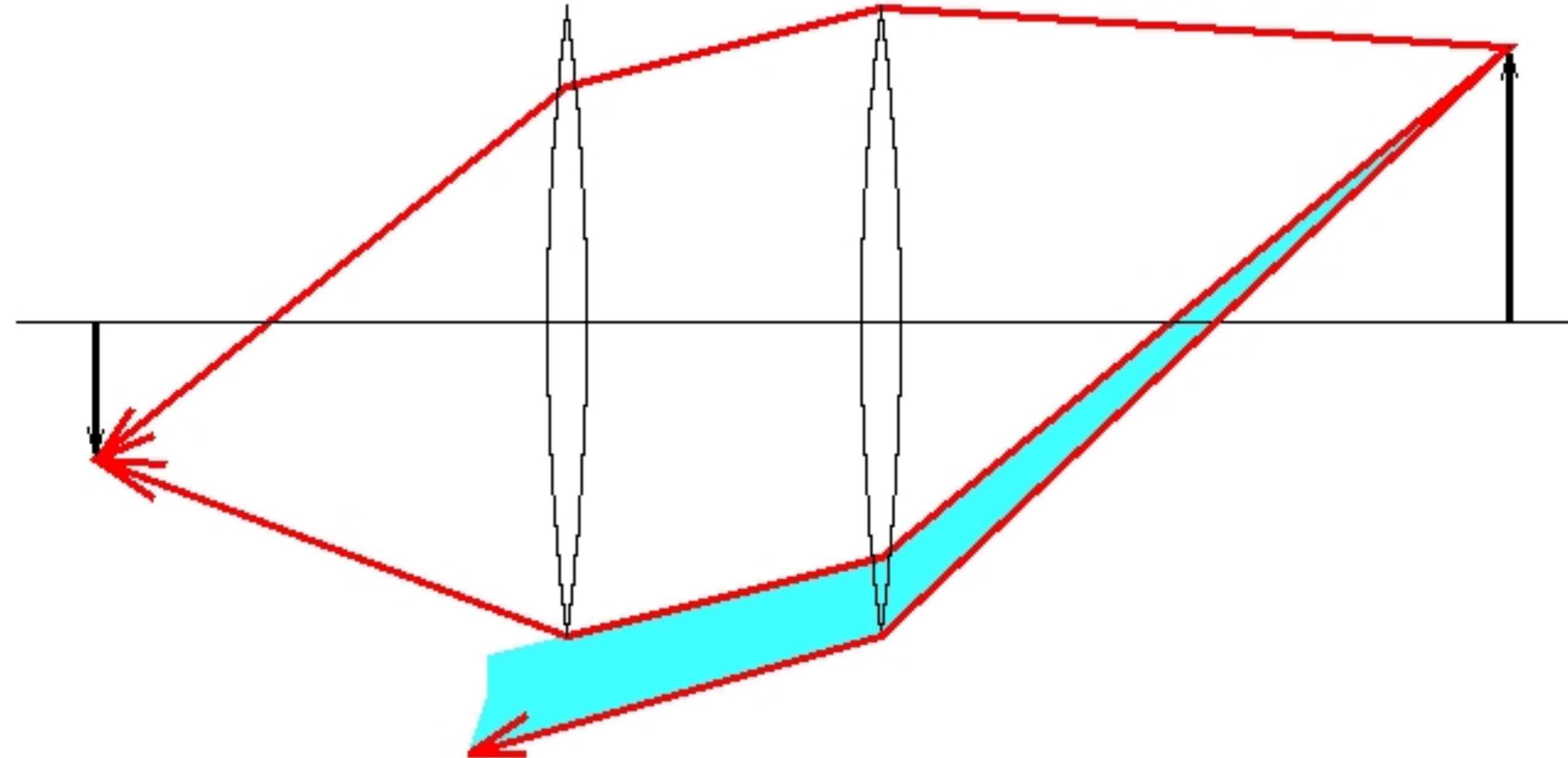


Image from lens with Spherical Aberration



Vignetting

Vignetting in a two-lens system



Forsyth & Ponce (2nd ed.) Figure 1.12

The shaded part of the beam **never reaches** the second lens

Vignetting



Chromatic **Aberration**

- Index of **refraction depends on wavelength**, λ , of light
- Light of different colours follows different paths
- Therefore, not all colours can be in equal focus

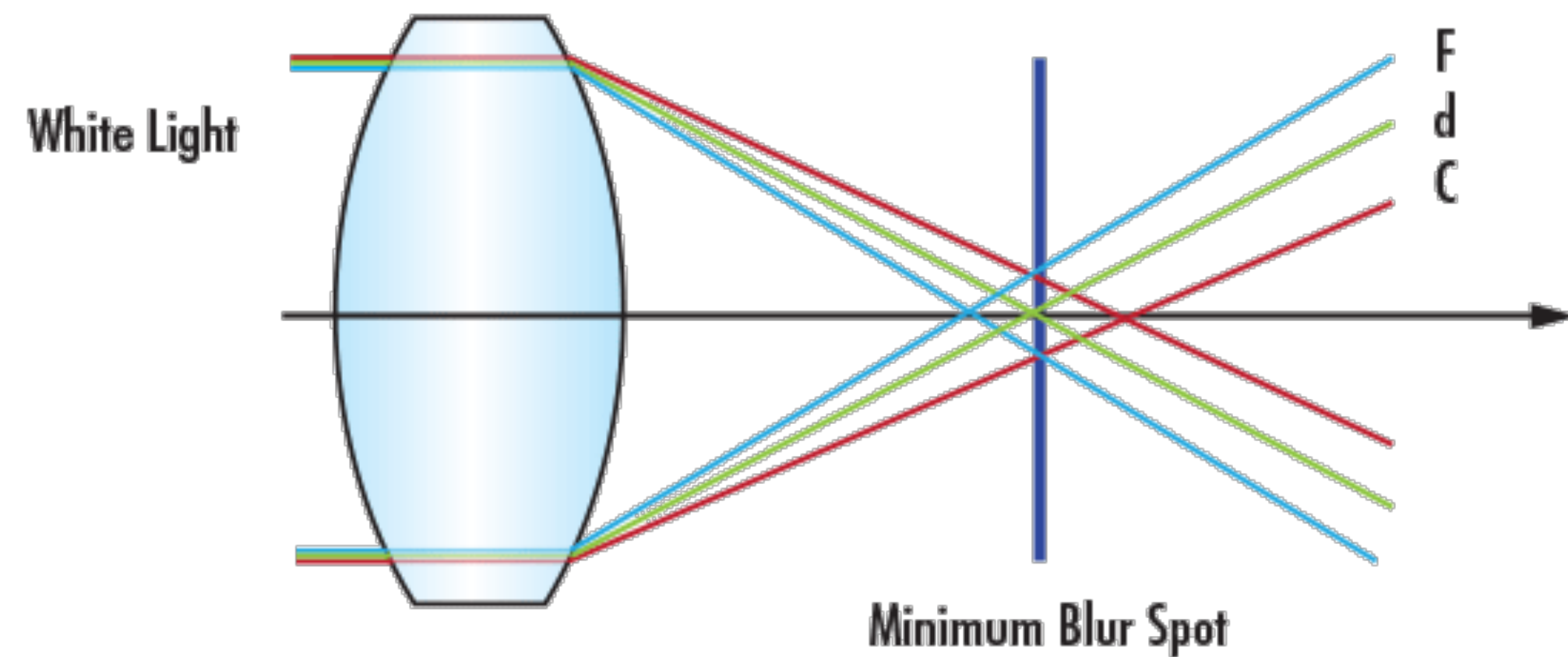
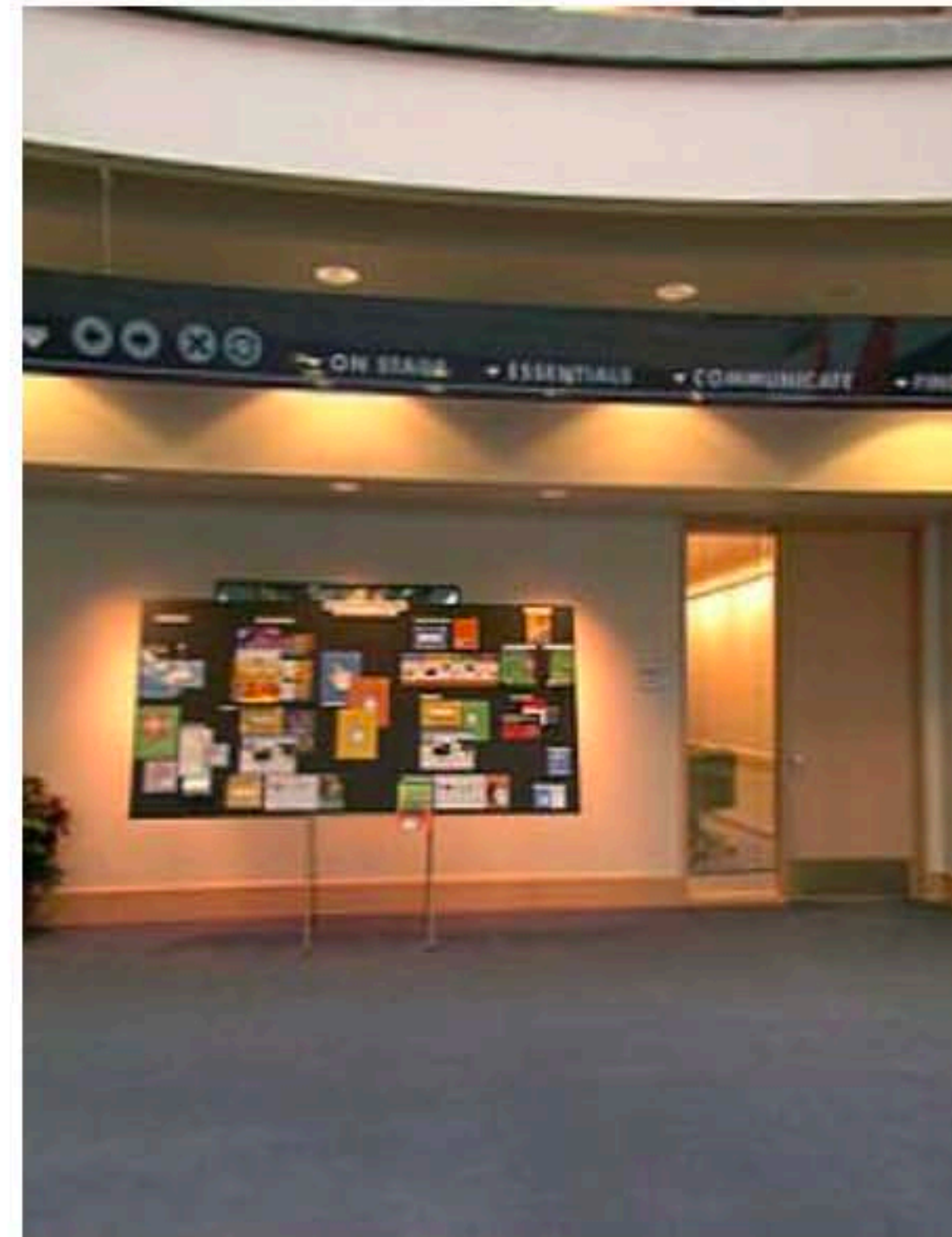


Image Credit: Trevor Darrell

Lens Distortion

Fish-eye Lens



Szeliski (1st ed.) Figure 2.13

Lines in the world are no longer lines on the image, they are curves!

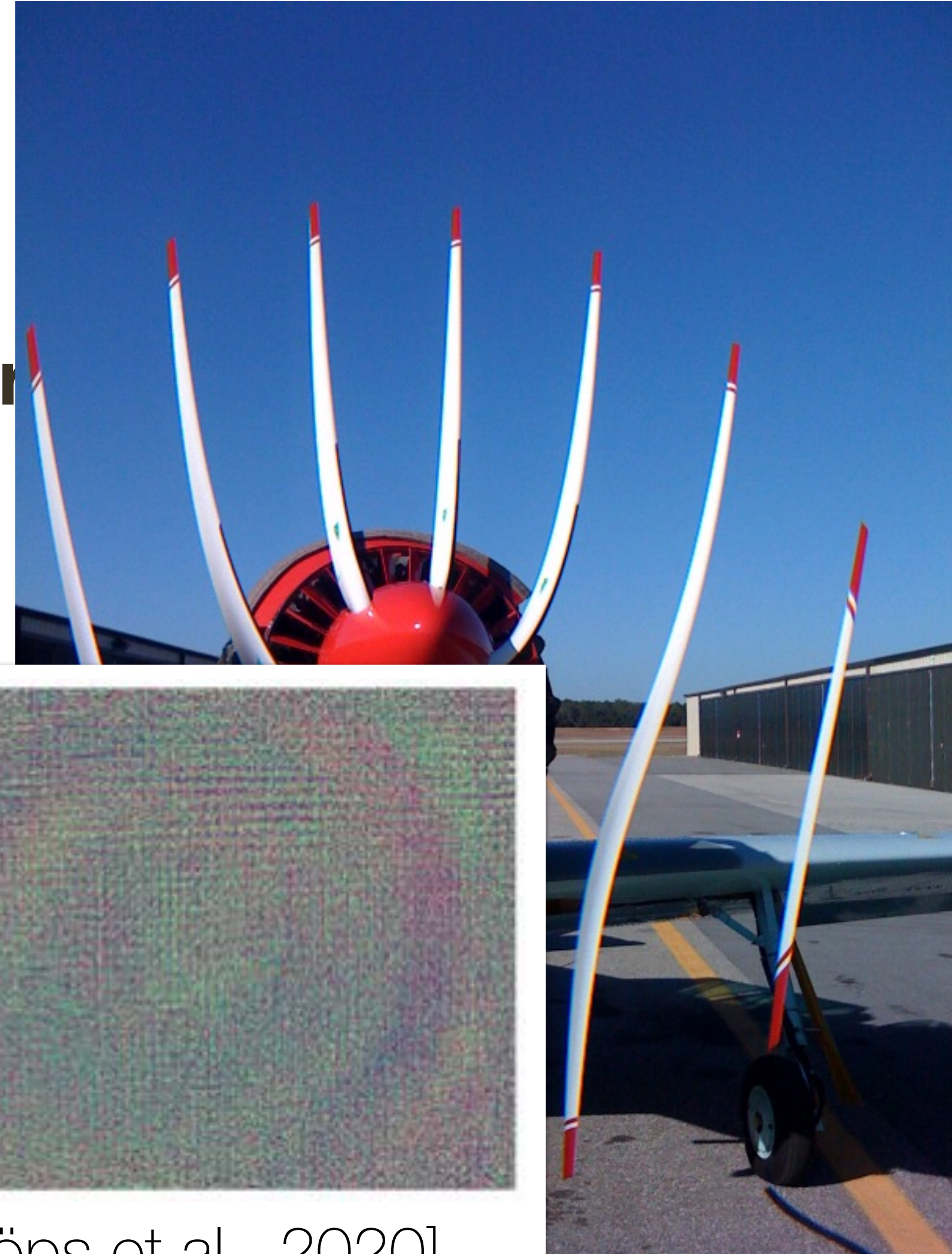
Other (Possibly Significant) **Lens Effects**

Scattering at the lens surface

- Some light is reflected at each lens surface

There are other **geometric phenomena/distortions**

- pincushion distortion
- barrel distortion



Parametric calibration errors

[Schöps et al., 2020]

Image from [Schöps et al., 2019]. Reproduced for educational purposes.

<https://www.flickr.com/photos/nragdale/3192314056/>

Lecture **Summary**

- We discussed a “physics-based” approach to image formation. Basic abstraction is the **pinhole camera**.
- **Lenses overcome limitations** of the pinhole model while trying to preserve it as a useful abstraction
- Projection equations: **perspective**, weak perspective, orthographic
- Thin lens equation
- Some “aberrations and **distortions**” persist (e.g. spherical aberration, vignetting)