

THE UNIVERSITY OF BRITISH COLUMBIA

CPSC 425: Computer Vision



Lecture 19: Classification (part2)

Menu for Today

Topics:

- Scene Classification
- Bag of Words Representation

Redings:

- Today's Lecture: Forsyth & Ponce (2nd ed.) 16.1.3, 16.1.4, 16.1.9
- **Next** Lecture:

Reminders:

- Quiz 4 is due today

Decision Tree Boosting

Forsyth & Ponce (2nd ed.) 17.1–17.2



Lecture 18: Re-cap (Image Classification)

Classify images containing single **objects**, the same techniques can be applied to classify natural **scenes** (e.g. beach, forest, harbour, library).



(assume given set of discrete labels) {dog, cat, truck, plane, ...}





Lecture 18: Image Classification

Representation of Images

- Image pixels directly
- Bag of Words

Classification Algorithms

- Bayes' Classifier
- Nearest Neighbor Classifier
- SVM Classifier

Lecture 18: Re-cap (Vector Space Model)

Many algorithms for image classification accumulate evidence on the basis of **visual words**.

To classify a text document (e.g. as an article on sports, entertainment, business, politics) we might find patterns in the occurrences of certain words.

Dictionary Learning: Learn Visual Words using clustering

Encode: build Bags-of-Words (BOW) vectors for each image

> **Classify**: Train data using BOWs



Input: large collection of images (they don't even need to be training images)



Dictionary Learning: Learn Visual Words using clustering

Encode: build Bags-of-Words (BOW) vectors for each image

> **Classify**: Train data using BOWs



Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)



Output: dictionary of visual words



Input: large collection of images (they don't even need to be training images)

Input: training images, dictionary



airplane	1	14	-	X	1	+	2	-1		-
automobile					-	The				*>
bird	S	ſ	12			4	1	N.	12	4
cat	a sta		4	50		<u>E</u>		Å.	A.S.	20
deer	6	48	X	M	Ĩ	Y	Y	1	-	
dog	1	1	-		(A)	(a)		N?	A	The second
frog	2	19						3K)		5
horse	- Mar	T.	A	2	1	107AB	1	24	6	N.
ship	-		ditte	-	144		2	12	and in	
truck			1						013	ALL.

Encode: \rightarrow build Bags-of-Words (BOW) vectors \rightarrow for each image

Classify: Train data using BOWs

Dictionary Learning: Learn Visual Words using clustering

Output: dictionary of visual words

Output: histogram representation for each training image

airplane automobile bird deer dog frog horse ship truck











Input: histogram representation for each training image + labels



Encode: **Output:** histogram representation \rightarrow build Bags-of-Words (BOW) vectors \rightarrow for each training image for each image

> **Classify**: **Output:** parameters if the classifier Train data using BOWs













Input: large collection of images (they don't even need to be training images)

Input: test image, dictionary





Dictionary Learning: Learn Visual Words using clustering

Encode: \rightarrow build Bags-of-Words (BOW) vectors \rightarrow for each image

> **Classify**: Test data using BOWs

Output: dictionary of visual words

Output: histogram representation for test image









Input: large collection of images (they don't even need to be training images)

Dictionary Learning: Learn Visual Words using clustering

Input: test image, dictionary



Input: histogram representation for test image, trained classifier





Output: dictionary of visual words







Input: large collection of images (they don't even need to be training images)



Dictionary Learning: Learn Visual Words using clustering

Encode: build Bags-of-Words (BOW) vectors for each image

> **Classify**: Train data using BOWs

Output: dictionary of visual words







Extracting SIFT Patches



Compute SIFT descriptor

[Lowe'99]

Normalize patch



Detect patches

[Mikojaczyk and Schmid '02] [Mata, Chum, Urban & Pajdla, '02] [Sivic & Zisserman, '03]

Extracting SIFT Patches







Creating **Dictionary**



Creating **Dictionary**





Creating **Dictionary**





Example Visual Dictionary







Source: B. Leibe

Example Visual Dictionary





Source: B. Leibe

Input: large collection of images (they don't even need to be training images)

Input: test image, dictionary





Dictionary Learning: Learn Visual Words using clustering

Encode: \rightarrow build Bags-of-Words (BOW) vectors \rightarrow for each image

> **Classify**: Test data using BOWs

Output: dictionary of visual words

Output: histogram representation for test image









2. Encode: build Bag-of-Words (BOW) vectors for each image



1. Quantization: image features gets associated to a visual word (nearest cluster center)













2. Encode: build Bag-of-Words (BOW) vectors for each image

2. Histogram: count the number of visual word occurrences







2. Encode: build Bag-of-Words (BOW) vectors for each image







frequency

codewords





Input: large collection of images (they don't even need to be training images)

Dictionary Learning: Learn Visual Words using clustering

Input: training images, dictionary

Encode: **Output:** histogram representation \rightarrow build Bags-of-Words (BOW) vectors \rightarrow for each training image for each image

Input: histogram representation for each training image + labels



Output: dictionary of visual words

Classify: Train data using BOWs

Output: parameters if the classifier











3. Classify: Train and text classifier using BOWs



K nearest neighbors





Input: large collection of images (they don't even need to be training images)

Dictionary Learning: Learn Visual Words using clustering

Input: test image, dictionary



Input: histogram representation for test image, trained classifier





Output: dictionary of visual words







Inference **Bag-of-Words** Representation

Algorithm:

Initialize an empty K-bin histogram, where K is the number of codewords Extract local descriptors (e.g. SIFT) from the image For each local descriptor **x**

Map (Quantize) **x** to its closest codeword \rightarrow **c**(**x**) Increment the histogram bin for c(x)Return histogram

vector machine or k-Nearest Neighbor classifier

We can then classify the histogram using a trained classifier, e.g. a support

The bag of words representation does not preserve any spatial information

The **spatial pyramid** is one way to incorporate spatial information into the image descriptor.

A spatial pyramid partitions the image and counts codewords within each grid box; this is performed at multiple levels

Compute Bag-of-Words histograms for each quadrant and then concatenate them



Fig. 16.8 in Forsyth & Ponce (2nd ed.). Original credit: Lazebnik et al., 2006





Fig. 16.8 in Forsyth & Ponce (2nd ed.). Original credit: Lazebnik et al., 2006

Compute Bag-of-Words histograms for each quadrant and then concatenate them





Fig. 16.8 in Forsyth & Ponce (2nd ed.). Original credit: Lazebnik et al., 2006

Compute Bag-of-Words histograms for each quadrant and then concatenate them



VLAD (Vector of Locally Aggregated Descriptors)

histogram bin

to their visual words

we increment it by the **residual** vector **x** – **c(x)**

- There are more advanced ways to 'count' visual words than incrementing its
- For example, it might be useful to describe how local descriptors are quantized
- In the VLAD representation, instead of incrementing the histogram bin by one,












Example: VLAD





Example: VLAD





VLAD (Vector of Locally Aggregated Descriptors)

The dimensionality of a **VLAD** descriptor is *Kd*

- K: number of codewords
- -d: dimensionality of the local descriptor

codewords

VLAD characterizes the distribution of local descriptors with respect to the



Rule Based **Classifier**: Distance + Threshold



There is nothing really to "learn" (no need for training data), just measure similarity using favorite distance and choose threshold based on validation set





There is nothing really to "learn" (no need for training data), just measure similarity using favorite distance and choose threshold based on validation set

Rule Based **Classifier**: Distance + Threshold

More robust, to lighting, but basically same





There is nothing really to "learn" (no need for training data), just measure similarity using favorite distance and choose threshold based on validation set

Rule Based **Classifier**: Distance + Threshold

> Rule Based **Classifier**: Distance + Threshold

More expressive, but basically same







- No real learning, mostly parameter/design tuning using validation set
- Empirically engineered features with desired properties

- Pragmatically defined models (classifiers) that either defined by hand or require test time optimization





Bayes — estimate *parametric* form of distribution (requires training data) for each class



Bayes — estimate *parametric* form of distribution (requires training data) for each class **kNN** — <u>non-parametric</u> form of distribution (requires training data) for each class

Learned Classifier: Bayes, kNN, Linear SVM

> Learned Classifier: Bayes, kNN, Linear SVM

Learned Classifier: Bayes, kNN, Linear SVM





Bayes — estimate *parametric* form of distribution (requires training data) for each class More expressive **kNN** — <u>non-parametric</u> form of distribution (requires training data) for each class Linear SVM — *parametric* form of classifier (requires training data) with implicit feature selection / weighting

Learned Classifier: Bayes, kNN, Linear SVM

> Learned Classifier: Bayes, kNN, Linear SVM

Learned Classifier: Bayes, kNN, Linear SVM











- 2. Histogram of histograms of gradients (i.e., simple hierarchical aggregation)





- 2. Histogram of histograms of gradients (i.e., simple hierarchical aggregation)





Recognition Overview: Convolutional Neural Nets (next week)

for a specific task (classification, detection, segmentation)





Deeper hierarchies of features (obtained by learned filters) **learned together with the classifier**



Recognition Overview: Foundational Models



2. "Fine-tuning" (optimizing again from a warm start) to get good performance on the task





1. "Pre-training" (optimizing) in an unsupervised / self-supervised manner (to get good feature extractors)



Let's do a bit of a case study ...







CIFAR10 Dataset

 Hand labelled set of 10 categories from Tiny Images dataset - 60,000 32x32 images in 10 classes (50k train, 10k test)

airplane	
automobile	
bird	
cat	
deer	
dog	W. 1.
frog	
horse	
ship	
truck	

Good test set for visual recognition problems



CIFAR10 Classification

Let's build an image classifier











airplane automobile

bird

cat

deer

Start by vectorizing the data x = 3072 element vector of 0-255



 $32 \times 32 \times RGB$ (8 bit) image \rightarrow x = [65 102 33 57 54 ...]

x = 3072 element vector of 0-255













truck

dog

frog

horse

Compute a single "average" template per class



Find the nearest mean and assign class:

CIFAR10 class means:



$c_q = \arg\min_i |\mathbf{x}_q - \mathbf{m}_i|^2$

Find the nearest mean and assign class:

CIFAR10 class means:



 $P(c|\mathbf{x}) \propto P(\mathbf{x}|c)P(c)$

$c_q = \arg\min_i |\mathbf{x}_q - \mathbf{m}_i|^2$

Find the nearest mean and assign class:

 $c_q = \arg$

CIFAR10 class means:



 $P(c|\mathbf{x}) \propto P(\mathbf{x}|c)P(c)$

 $P(c) = \frac{1}{10}$ $\log P(\mathbf{x}|c) \propto (\mathbf{x}_q - \mathbf{m}_c)^T \Sigma^{-1} (\mathbf{x}_q - \mathbf{m}_c)$

$$\min_i |\mathbf{x}_q - \mathbf{m}_i|^2$$

Find the nearest mean and assign class:

CIFAR10 class means:



Performance:

Chance performance: 10% ~94% Human performance: Nearest Mean Classifier (pixels): 37%





We can view each image as a point in a high dimensional space



bird

Find nearest neighbour in training set:

Assign class to class of the nearest neighbour:







Calculate $|\mathbf{x}_q - \mathbf{x}_i|$ for all training data

- $i_{NN} = \arg\min_{i} |\mathbf{x}_{q} \mathbf{x}_{i}|$

 - $\hat{y}(\mathbf{x}_q) = y(\mathbf{x}_{i_N N})$

Find nearest neighbour in training set:

Assign class to class of the nearest neighbour:

Performance:

Chance performance: Human performance:

Source: https://cran.r-project.org/web/packages/KernelKnn/vignettes/image_classification_using_MNIST_CIFAR_data.html

- $i_{NN} = \arg\min_{i} |\mathbf{x}_{q} \mathbf{x}_{i}|$

 - $\hat{y}(\mathbf{x}_q) = y(\mathbf{x}_{i_N N})$

10% ~94% Nearest Neighbor (pixels): 40.8% Nearest Neighbor (HoG): 58.3%

Histogram of Oriented Gradients (HOG) Features

Pedestrian detection

128 pixels 16 cells 15 blocks

1 cell step size



64 pixels 8 cells 7 blocks

Redundant representation due to overlapping blocks

visualization



 $15 \times 7 \times 4 \times 9 =$ 3780



Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)





Find nearest neighbour in training set:

Assign class to class of the nearest neighbour:

Performance:

Chance performance: Human performance:

Source: https://cran.r-project.org/web/packages/KernelKnn/vignettes/image_classification_using_MNIST_CIFAR_data.html

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10% ~94% Nearest Neighbor (pixels): 40.8% Nearest Neighbor (HoG): 58.3%









Query

7900

















Query

7900

790,000























7900

790,000



Tiny Image Recognition



Nearest neighbour becomes increasingly accurate as N increases, but do we need to store a dataset of 80 million images?

[Torralba, Fergus, Freeman '08]

yellow = 7900, red = 790,000, blue = 79,000,000




bird



cat



bird

cat

















37.3% [2] / **39.5**%*[1] Linear SVM (pixels): **65.6**%*[1] Linear SVM (SIFT): Linear SVM (BoW /w SIFT, 1600 words, hard voting): 68.6% [2] Linear SVM (BoW /w SIFT, 1600 words, soft voting): 77.9% [2] Linear SVM (BoW /w SIFT, 4000 words, soft voting): 79.6% [2]

1] https://proceedings.neurips.cc/paper_files/paper/2010/file/4558dbb6f6f8bb2e16d03b85bde76e2c-Paper.pdf

[2] https://cs.stanford.edu/~acoates/papers/coatesleeng_aistats_2011.pdf

Hard voting: $f_k(x) = \begin{cases} 1 & \text{if } k = \arg\min_j ||c^{(j)} - x||_2^2 \\ 0 & \text{otherwise.} \end{cases}$

Soft voting: $f_k(x) = \max\{0, \mu(z) - z_k\}$

L2 distance to centroid k

10% Chance performance: Human performance: ~94%











Hard voting: $f_k(x) = \begin{cases} 1 & \text{if } k = \arg\min_j ||c^{(j)} - x||_2^2 \\ 0 & \text{otherwise.} \end{cases}$

Soft voting: $f_k(x) = \max\{0, \mu(z) - z_k\}$







+ 0

+ 0

+ 0

Hard voting: $f_k(x) = \begin{cases} 1 & \text{if } k = \arg\min_j ||c^{(j)} - x||_2^2 \\ 0 & \text{otherwise.} \end{cases}$

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bird

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Soft voting: $f_k(x) = \max\{0, \mu(z) - z_k\}$







+ 0.3

+ 0

+ 0

Hard voting: $f_k(x) = \begin{cases} 1 & \text{if } k = \arg\min_j ||c^{(j)} - x||_2^2 \\ 0 & \text{otherwise.} \end{cases}$

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L2 distance to centroid k

10% Chance performance: Human performance: ~94%









Deep Learning



Query:



Performance:

[3] <u>https://arxiv.org/pdf/2203.12054.pdf</u>

- 10% Chance performance: ~94% Human performance:
- Linear SVM (pixels): **37.3**% [2] / **39.5**%*[1] Linear SVM (SIFT): **65.6**%*[1] Linear SVM (BoW /w SIFT, 1600 words, hard voting): 68.6% [2] Linear SVM (BoW /w SIFT, 1600 words, soft voting): 77.9% [2] Linear SVM (BoW /w SIFT, 4000 words, soft voting): 79.6% [2] *Convolutional Neural Net (CNN): **91.3**% [3] *DINO [Caron et al., 2021]: **94.4**% [3] *RandSAC [Hua et al., 2023]: **96.9**% [3]





Take home **messages** ...

- Both classification and feature representation play significant role
- Classifiers need to be expressive to do well, but so do the features
- Parametric classifiers are much easier to work with (they are faster)
- Which is more significant, in part, depends on the amount of available data

More complex classifiers ...

Lets look at more expressive classifiers that, for example, explicitly do feature selection





Back to Classification

A decision tree is a simple non-linear parametric classifier

A data point starts at the root and recursively proceeds to the child node determined by the feature test, until it reaches a leaf node

- Consists of a tree in which each internal node is associated with a feature test
- The leaf node stores a class label or a probability distribution over class labels





Learning a decision tree from a training set involves selecting an efficient sequence of feature tests

Example: Waiting for a restaurant table

Example					At	tributes	;				Target
Lincompio	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
X_1	T	F	F	Т	Some	\$\$\$	F	Т	French	0–10	T 🌒
X_2	T	F	F	T	Full	\$	F	F	Thai	30–60	F 🗕
X_3	F	T	F	F	Some	\$	F	F	Burger	0–10	
X_4	T	F	T	T	Full	\$	F	F	Thai	10–30	
X_5	T	F	T	F	Full	\$\$\$	F	Т	French	>60	F 🗕
X_6	F	T	F	T	Some	\$\$	Т	Т	Italian	0–10	Τ •
X_7	F	T	F	F	None	\$	Т	F	Burger	0–10	F 🗕
X_8	F	F	F	T	Some	\$\$	Т	Т	Thai	0–10	Τ •
X_9	F	T	T	F	Full	\$	Т	F	Burger	>60	F 🗕
X_{10}	T	T	T	T	Full	\$\$\$	F	Т	Italian	10–30	F 🗕
X_{11}	F	F	F	F	None	\$	F	F	Thai	0–10	F 🗕
X_{12}	T	T	T	T	Full	\$	F	F	Burger	30–60	Τ •

Learning a decision tree from a training set involves selecting an efficient sequence of feature tests

Example: Waiting for a restaurant table

1

Is there an alternative restaurant near by?

Example	•				At	tributes	5				Target
Linompio	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
X_1	T	F	F	Т	Some	\$\$\$	F	Т	French	0–10	T 🌒
X_2	T	F	F	Т	Full	\$	F	F	Thai	30–60	F 🗕
X_3	F	T	F	F	Some	\$	F	F	Burger	0–10	
X_4	T	F	T	Т	Full	\$	F	F	Thai	10–30	
X_5	T	F	T	F	Full	\$\$\$	F	Т	French	>60	F 🗕
X_6	F	T	F	Т	Some	\$\$	T	Т	Italian	0–10	
X_7	F	T	F	F	None	\$	T	F	Burger	0–10	F 🗕
X_8	F	F	F	Т	Some	\$\$	T	Т	Thai	0–10	
X_9	F	T	T	F	Full	\$	T	F	Burger	>60	F •
X_{10}	T	T	T	Т	Full	\$\$\$	F	Т	Italian	10–30	F 🗕
X_{11}	F	F	F	F	None	\$	F	F	Thai	0–10	F •
X_{12}	T	T	T	Т	Full	\$	F	F	Burger	30–60	Τ •

Learning a decision tree from a training set involves selecting an efficient sequence of feature tests

Example: Waiting for a restaurant table

Is there a bar at the restaurant?

Example		↓ ↓			At	tributes	3				Target
Linompio	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
X_1	T	F	F	Т	Some	\$\$\$	F	Т	French	0–10	T 🌒
X_2	T	F	F	T	Full	\$	F	F	Thai	30–60	F 🗕
X_3	F		F	F	Some	\$	F	F	Burger	0–10	
X_4	T	F	T	T	Full	\$	F	F	Thai	10–30	
X_5	T	F	T	F	Full	\$\$\$	F	T	French	>60	F 🗕
X_6	F	T	F	T	Some	\$\$	T	T	Italian	0–10	Τ •
X_7	F	T	F	F	None	\$		F	Burger	0–10	F 🗕
X_8	F	F	F	T	Some	\$\$		T	Thai	0–10	Τ •
X_9	F		T	F	Full	\$		F	Burger	>60	F 🗕
X_{10}	T	T	T	T	Full	\$\$\$	F	T	Italian	10–30	F 🗕
X_{11}	F	F	F	F	None	\$	F	F	Thai	0–10	F 🗕
X_{12}	T	T	T	T	Full	\$	F	F	Burger	30–60	Τ •

Learning a decision tree from a training set involves selecting an efficient sequence of feature tests

Example: Waiting for a restaurant table

Is it Friday night?

											1
Example			¥		At	tributes	3			Target	
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
X_1	T	F	F	T	Some	\$\$\$	F	Т	French	0–10	T 🌒
X_2	T	F	F	T	Full	\$	F	F	Thai	30–60	F 🗕
X_3	F	T	F	F	Some	\$	F	F	Burger	0–10	
X_4	T	F	T	T	Full	\$	F	F	Thai	10–30	Τ •
X_5	T	F	T	F	Full	\$\$\$	F	T	French	>60	F 🗕
X_6	F	T	F	T	Some	\$\$		T	Italian	0–10	Τ •
X_7	F	T	F	F	None	\$	T	F	Burger	0–10	F 🗕
X_8	F	F	F	T	Some	\$\$	T	T	Thai	0–10	Τ •
X_9	F	T	T	F	Full	\$		F	Burger	>60	F 🗕
X_{10}	T	T	T	T	Full	\$\$\$	F	T	Italian	10–30	F 🗕
X_{11}	F	F	F	F	None	\$	F	F	Thai	0–10	F 🔴
X_{12}	T	T	T	T	Full	\$	F	F	Burger	30–60	Τ •

Learning a decision tree from a training set involves selecting an efficient sequence of feature tests

Example: Waiting for a restaurant table

Example		Attributes											
Lincompio	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait		
X_1	T	F	F	Т	Some	\$\$\$	F	Т	French	0–10	T 🌒		
X_2	T	F	F	Т	Full	\$	F	F	Thai	30–60	F 🗕		
X_3	F	T	F	F	Some	\$	F	F	Burger	0–10			
X_4	T	F	T	Т	Full	\$	F	F	Thai	10–30			
X_5	T	F	T	F	Full	\$\$\$	F	T	French	>60	F 🗕		
X_6	F	T	F	Т	Some	\$\$	T	T	Italian	0–10	Τ •		
X_7	F	T	F	F	None	\$	Т	F	Burger	0–10	F 🗕		
X_8	F	F	F	Т	Some	\$\$	T	T	Thai	0–10	Τ •		
X_9	F	T	T	F	Full	\$	T	F	Burger	>60	F 🗕		
X_{10}	T	T	T	Т	Full	\$\$\$	F	T	Italian	10–30	F 🗕		
X_{11}	F	F	F	F	None	\$	F	F	Thai	0–10	F 🗕		
X_{12}	T	T	T	Т	Full	\$	F	F	Burger	30–60	Τ •		

How many people in the restaurant?

Which test is more helpful?





Figure credit: Russell and Norvig (3rd ed.)

The **entropy** of a set S of data samples is defined as

H(S) = -

where C is the set of classes represented in S, and p(c) is the empirical distribution of class c in S

and zero when all data samples are from the same class.

$$\sum_{c \in C} p(c) \log(p(c))$$

Entropy is highest when data samples are spread equally across all classes,

Entropy at each node ... Which test is more helpful?



Figure credit: Russell and Norvig (3rd ed.)

$$I = H(S) -$$

In the previous example, the information gains of the two candidate tests are:

$I_{Patrons} = 0.541$

So we choose the 'Patrons' test.

In general we try to select the feature test that maximizes the **information gain**:

$$\sum_{i \in \{children\}} \frac{|S^i|}{|S|} H(S^i)$$

$$I_{Type} = 0$$

$$I = H(S) -$$

In the previous example, the information gains of the two candidate tests are:

 $I_{Patrons} = 0.541$

So we choose the 'Patrons' test.

Build a tree in a greedy recursive manner by maximizing information gain at each node

In general we try to select the feature test that maximizes the **information gain**:

$$\sum_{i \in \{children\}} \frac{|S^i|}{|S|} H(S^i)$$

$$I_{Type} = 0$$

Following this construction procedure we obtain the final decision tree:



Figure credit: Russell and Norvig (3rd ed.)

A random forest is an ensemble of decision trees.

Randomness is incorporated via training set sampling and/or generation of the candidate binary tests

The prediction of the random forest is obtained by averaging over all decision trees.



Forsyth & Ponce (2nd ed.) Figure 14.19. Original credit: J. Shotton et al., 2011



Microsoft Kinect







Kinect allows users of Microsoft's Xbox 360 console to interact with games using natural body motions instead of a traditional handheld controller. The pose (joint positions) of the user is predicted using a random forest trained on depth features.



Figure credit: J. Shotton et al., 2011

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Kinect allows users of Microsoft's Xbox 360 console to interact with games using natural body motions instead of a traditional handheld controller. The pose (joint positions) of the user is predicted using a random forest trained on depth features.





Jamie Shotton

Figure credit: J. Shotton et al., 2011

Simple test: threshold on the difference of two depth values at an offset from a target pixel ...



 $f_{\theta}(I, \mathbf{x}) = d_I \left(\mathbf{x} + \frac{\mathbf{u}}{d_I(\mathbf{x})} \right) - d_I \left(\mathbf{x} + \frac{\mathbf{v}}{d_I(\mathbf{x})} \right)$



Figure credit: J. Shotton et al., 2011

•••

What are the parameters of this test?

 f_{θ}

 $f_{\theta}(I, \mathbf{x}) > \Theta_j$



$$q(I, \mathbf{x}) = d_I \left(\mathbf{x} + \frac{\mathbf{u}}{d_I(\mathbf{x})} \right) - d_I \left(\mathbf{x} + \frac{\mathbf{v}}{d_I(\mathbf{x})} \right)$$



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What are the parameters of this test?

How many such tests can we have?

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What are the parameters of this test?

How many such tests can we have?

(# pix) x (# pix) x (# threshold)

 $f_{\theta}(I, \mathbf{x}) > \Theta_{i}$



 $f_{\theta}(I, \mathbf{x}) = d_I \left(\mathbf{x} + \frac{\mathbf{u}}{d_I(\mathbf{x})} \right) - d_I \left(\mathbf{x} + \frac{\mathbf{v}}{d_I(\mathbf{x})} \right)$



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Learning is slow (weeks)!

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What are the parameters of this test?

How many such tests can we have?

(# pix) x (# pix) x (# threshold)

Learning is slow (weeks)!

Inference is fast (real-time)!

 $f_{\theta}(I,\mathbf{x}) > \Theta_{i}$



 $f_{\theta}(I, \mathbf{x}) = d_I \left(\mathbf{x} + \frac{\mathbf{u}}{d_I(\mathbf{x})} \right) - d_I \left(\mathbf{x} + \frac{\mathbf{v}}{d_I(\mathbf{x})} \right)$





....

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$$q(I, \mathbf{x}) = d_I \left(\mathbf{x} + \frac{\mathbf{u}}{d_I(\mathbf{x})} \right) - d_I \left(\mathbf{x} + \frac{\mathbf{v}}{d_I(\mathbf{x})} \right)$$





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Figure credit: J. Shotton et al., 2011

Combining **Classifiers**

One common strategy to obtain a better classifier is to combine multiple classifiers.

A simple approach is to train an ensemble of independent classifiers, and average their predictions.

Boosting is another approach.

- Train an ensemble of classifiers sequentially.

 Bias subsequent classifiers to correctly predict training examples that previous classifiers got wrong.

- The final boosted classifier is a weighted combination of the individual classifiers.











Final classifier is a combination of weak classifiers



Object Detection: Introduction

We have been discussing image classification, where we pass a whole image into a classifier and obtain a class label as output

We assumed the image contained a single, central object

object class in an image

- The task of **object detection** is to detect and localize all instances of a target
- Localization typically means putting a tight bounding box around the object

Train an image classifier as described previously. 'Slide' a fixed-sized detection window across the image and evaluate the classifier on each window.



Train an image classifier as described previously. 'Slide' a fixed-sized detection window across the image and evaluate the classifier on each window. Is there a car?



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This is a search over location — We have to search over scale as well — We may also have to search over aspect ratios

What data we **train** a classifier on? Image Classifiers





Image classifiers can be applied to regions/windows, but do not work so well in practice ...

What data we **train** a classifier on? Image Classifiers





What data we **train** a classifier on? Image Classifiers





Object Classifiers



















Let's assume we have **object** labeled data ...

Object classifiers work a lot better ... but require expensive bounding box annotations ...

Object Classifiers



















Let's assume we have **object** labeled data ...

Object classifiers work a lot better ... but require expensive bounding box annotations ...

Object Classifiers

(for convenience we will normalize patches to 64x64 ... or 128x128)









Example: Face Detection

The Viola-Jones face detector is a classic sliding window detector that learns both efficient features and a classifier

- A key strategy is to use features that are fast to evaluate to reject most windows early

The Viola-Jones detector computes 'rectangular' features within each window

Example: Face Detection Summary



Figure credit: K. Grauman



Example: Face Detection Summary



Figure credit: K. Grauman



Example: Face Detection

Observations:

- On average only 0.01% of all sub-windows are positive (faces)
- Equal computation time is spent on all sub-window
- Shouldn't we spend most time only on **potentially positive** sub-windows?

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A simple 2-feature classifier can achieve almost 100% detection rate (0% false negatives) with 50% false positive rate

Example: Face Detection

Observations:

- On average only 0.01% of all sub-windows are positive (faces)
- Equal computation time is spent on all sub-window
- Shouldn't we spend most time only on **potentially positive** sub-windows?

Solution:

most negative (clearly non-face) windows

- 2nd layer with 10 features can tackle "harder" negative-windows which survived the 1st layer, and so on...

A simple 2-feature classifier can achieve almost 100% detection rate (0% false negatives) with 50% false positive rate

- A simple 2-feature classifier can act as a 1st layer of a series to filter out

Cascading Classifiers



To make detection **faster**, features can be reordered by increasing complexity of evaluation and the thresholds adjusted so that the early (simpler) tests have few or no false negatives

Any window that is rejected by early tests can be discarded quickly without computing the other features

This is referred to as a **cascade** architecture

Cascading Classifiers



A classifier in the cascade is not necessarily restricted to a single feature

Example: Face Detection Summary



Figure credit: K. Grauman



Hard Negative Mining





Image From: Jamie Kang



Recall: Sliding Window

Train an image classifier as described previously. 'Slide' a fixed-sized detection window across the image and evaluate the classifier on each window.



Image credit: KITTI Vision Benchmark

Recall: Sliding Window

Train an image classifier as described previously. 'Slide' a fixed-sized detection window across the image and evaluate the classifier on each window.



looking for.

Image credit: KITTI Vision Benchmark

This is a lot of possible windows! And most will not contain the object we are

- object-like properties
- background texture
- exhaustive sliding window search

Object proposal algorithms generate a short list of regions that have generic

- These regions are likely to contain some kind of foreground object instead of

The object detector then considers these candidate regions only, instead of

First introduced by Alexe et al., who asked 'what is an object?' and defined an 'objectness' score based on several visual cues



Figure credit: Alexe et al., 2012



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First introduced by Alexe et al., who asked 'what is an object?' and defined an 'objectness' score based on several visual cues



This work argued that objects typically — are unique within the image and stand out as salient have a contrasting appearance from surroundings and/or have a well-defined closed boundary in space



Multiscale Saliency

- Favors regions with a unique appearance within the image







High scale

Low scale

Successful Case

Failure Case



Colour Contrast

Favors regions with a contrasting colour appearance from immediate surroundings



Successful Cases

Failure Case



Superpixels Straddling

- Favors regions with a well-defined closed boundary
- contain pixels both inside and outside of the window



- Measures the extent to which superpixels (obtained by image segmentation)





Superpixels Straddling

- Favors regions with a well-defined closed boundary
- contain pixels both inside and outside of the window



(a)



Successful Cases

— Measures the extent to which superpixels (obtained by image segmentation)

(b)



Failure Case



TABLE 2: For each detector [11, 18, 33] we report its performance (left column) and that of our algorithm 1 using the same window scoring function (right column). We show the average number of windows evaluated per image #win and the detection performance as the mean average precision (mAP) over all 20 classes.

	[11] O	BJ- [11]	[18] C	BJ- [18]	ESS-BOW[33]	OBJ-BOW
mAP	0.186	0.162	0.268	0.225	0.127	0.125
#win	79945	1349	18562 -	1358	183501	

Speeding up [11] HOG pedestrian detector [18] Deformable part model detector [33] Bag of words detector

 Table credit: Alexe et al., 2012

Summary

Detection scores in the deformable part model are based on both appearance and location

The deformable part model is trained iteratively by alternating the steps 1. Assume components and part locations given; compute appearance and

- 1. Assume components and part lo offset models
- 2. Assume appearance and offset part locations

An object **proposal** algorithm generates a short list of regions with generic object-like properties that can be evaluated by an object detector in place of an exhaustive sliding window search

2. Assume appearance and offset models given; compute components and