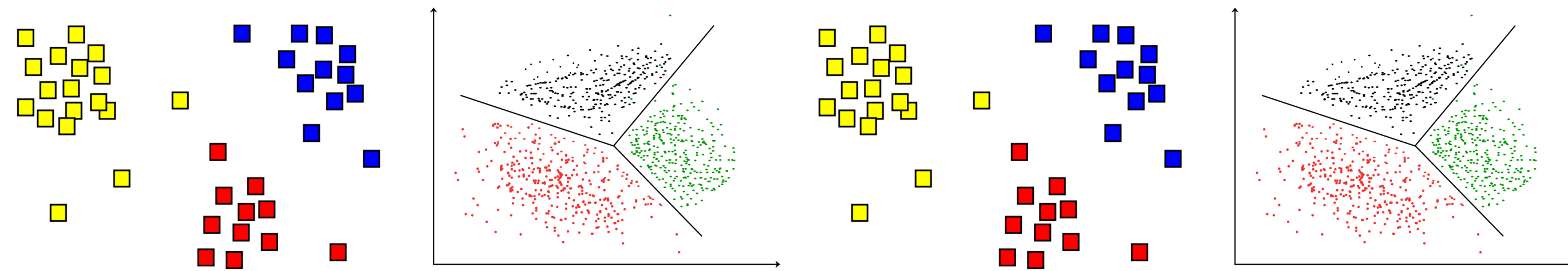




CPSC 425: Computer Vision



Lecture 18: Visual Classification 1, Bag of Words

Menu for Today

Topics:

- Visual **Classification**
- **Bag of Words** Representations

Readings:

- **Today's** Lecture: Szeliski 11.4, 12.3-12.4, 9.3, 5.1-5.2

Reminders:

- **Quiz 4** will be available tonight (Topics: SIFT, Image Warping, Stereo)
- **Quiz 5** will be next Monday (Topics: Optical Flow, Classification)
- Issue with **Assignment 5** (see Piazza, instructions have been updated)

CVPR 2025

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Important Dates

Submitting 8 papers

Paper Submission Deadline	Nov 14 '24 11:59 PM PST *	00 weeks 00 days 10:27:52
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All dates	Timezone: America/Vancouver	

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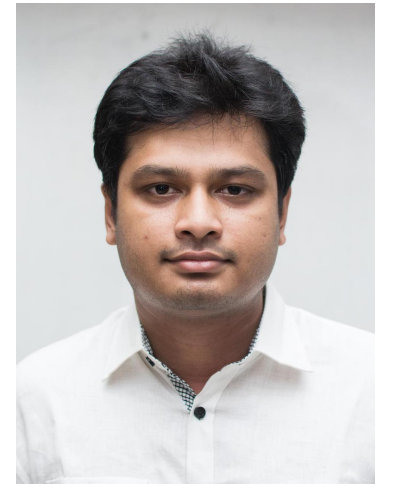
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Training of Vision-Language Models



Jiayun Luo



Rayat Hossain

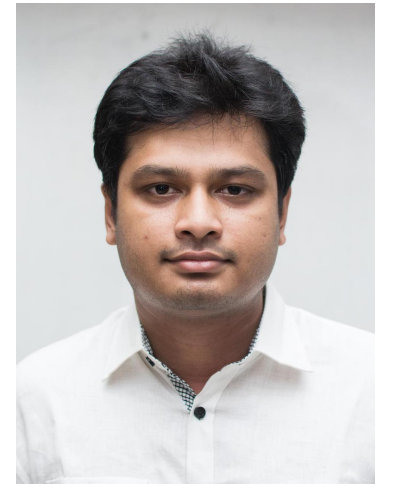
A big tan stuffed bear sitting in front of the store where there are many sale items on display; the door appears to be closed with no people in sight.



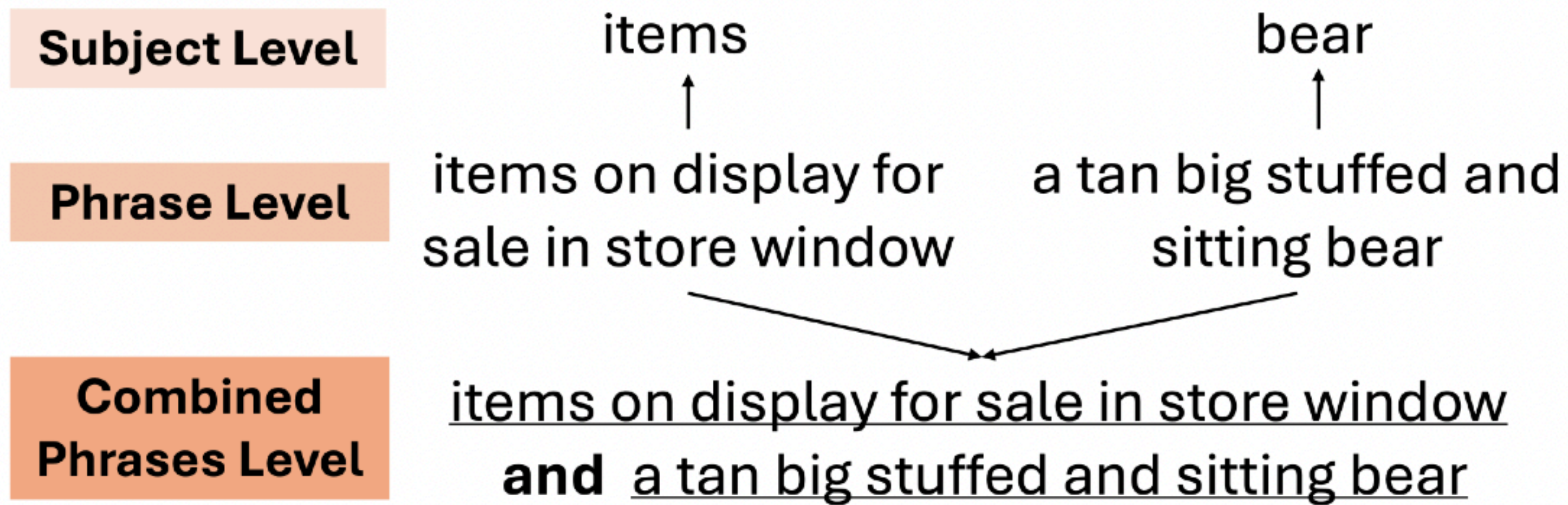
Training of Vision-Language Models



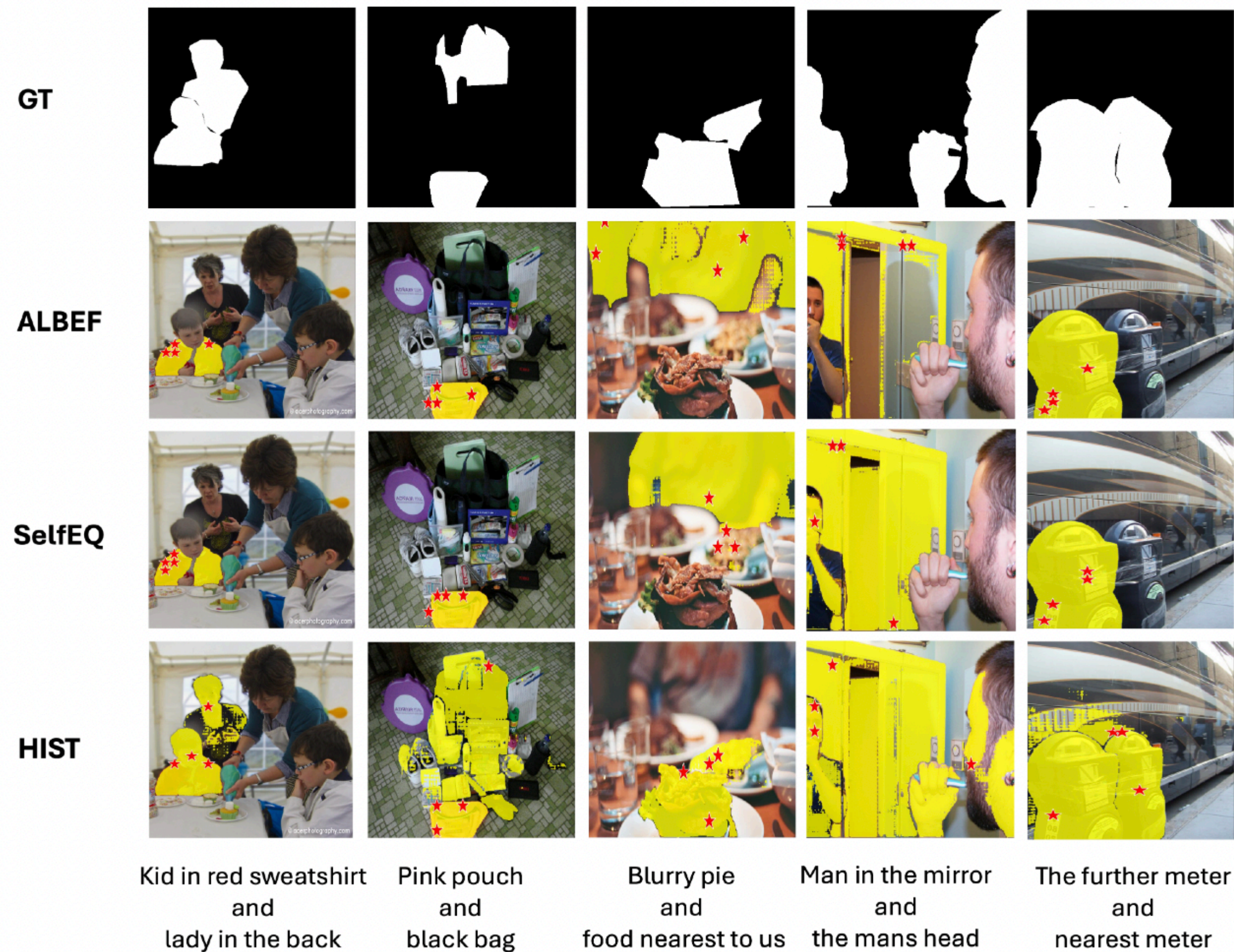
Jiayun Luo



Rayat Hossain



Segmentation ...



Method	Training	Flickr30K	Referit
InfoGround [10]	VG-boxes	76.7	-
VMRM [8]	VG-boxes	81.1	-
AMC [41]	VG-boxes	86.6	73.2
ALBEF [21]	Zero-shot	79.4	59.7
BLIP [22]	Zero-shot	80.1	51.6
g [33]	VG	75.6	66.0
g++ [32]	VG	80.0	70.3
ALBEF + SelfEQ [†] [12]	VG	81.7	67.0
ALBEF + SelfEQ [12]	VG	81.9	67.4
(Ours) ALBEF + HIST	VG	83.6	<u>69.5</u>
(Ours) BLIP + HIST	VG	81.5	58.1
g [33]	COCO	75.4	61.0
g++ [32]	COCO	78.1	61.5
ALBEF + SelfEQ [†] [12]	COCO	84.1	62.8
ALBEF + SelfEQ [12]	COCO	84.1	<u>62.8</u>
(Ours) ALBEF + HIST	COCO	85.3	63.4
(Ours) BLIP + HIST	COCO	<u>84.7</u>	57.6

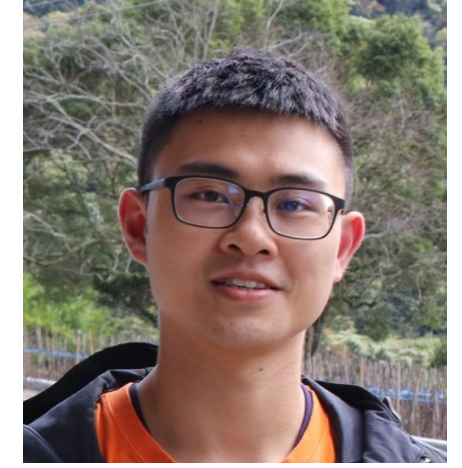
Few-shot Segmentation



Rayat Hossain

Image	GT	0-shot w/o ITM	0-shot w ITM	1-shot

Visual Program Synthesis

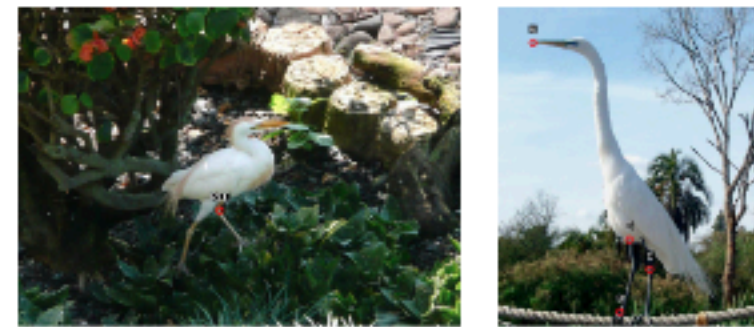


Wan-Cyuan (Chris) Fan

TASK DEFINITION: In this task, you are given a prompt and two images. In the first image, there is only one point labeled with a red circle and REF tag. In the second image, there are four points labeled with red circle and a letter tag of A, B, C, and D. You have to ... the second image corresponds to the point in the first image. You may have to know where these points are to answer the question. Here are three examples of the user task.

EXAMPLES from the task:

EXAMPLE 0



TASK REQUEST PROMPT #:

 ... Which point on ... (A) Point A (B) Point B (C) Point C...

The correct answer is: (C)

EXAMPLE 1



TASK REQUEST PROMPT #:

<Image> <Image> ... Which point ... (D) Point.

The correct answer is: (D)

⋮

(OPTIONAL) USER CONSTRAINTS: For example, execution time need to be less than 5 sec per sample, or models with fewer than 3B parameters...

Visual Program Synthesis

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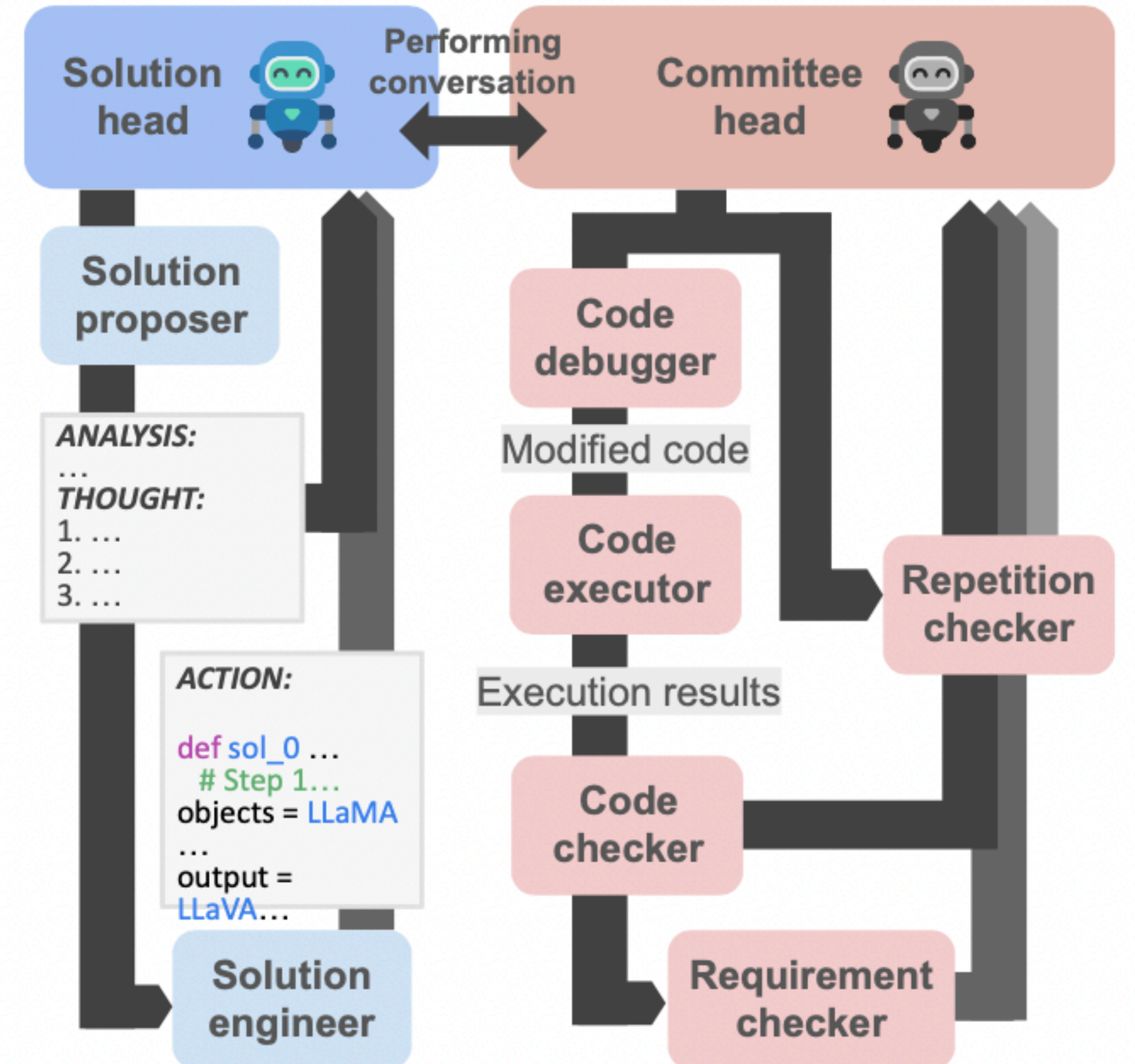


TASK REQUEST PROMPT #:
<Image> <Image> ... Which point ... (D) Point.

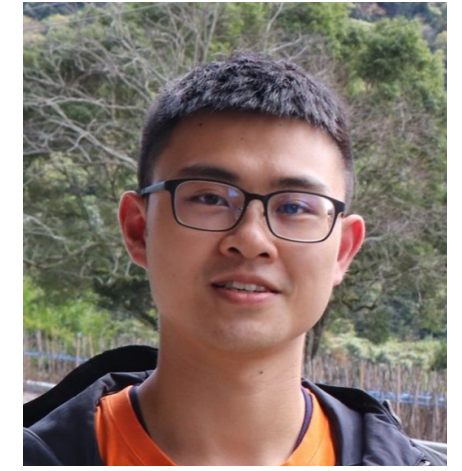
The correct answer is: (D)

⋮

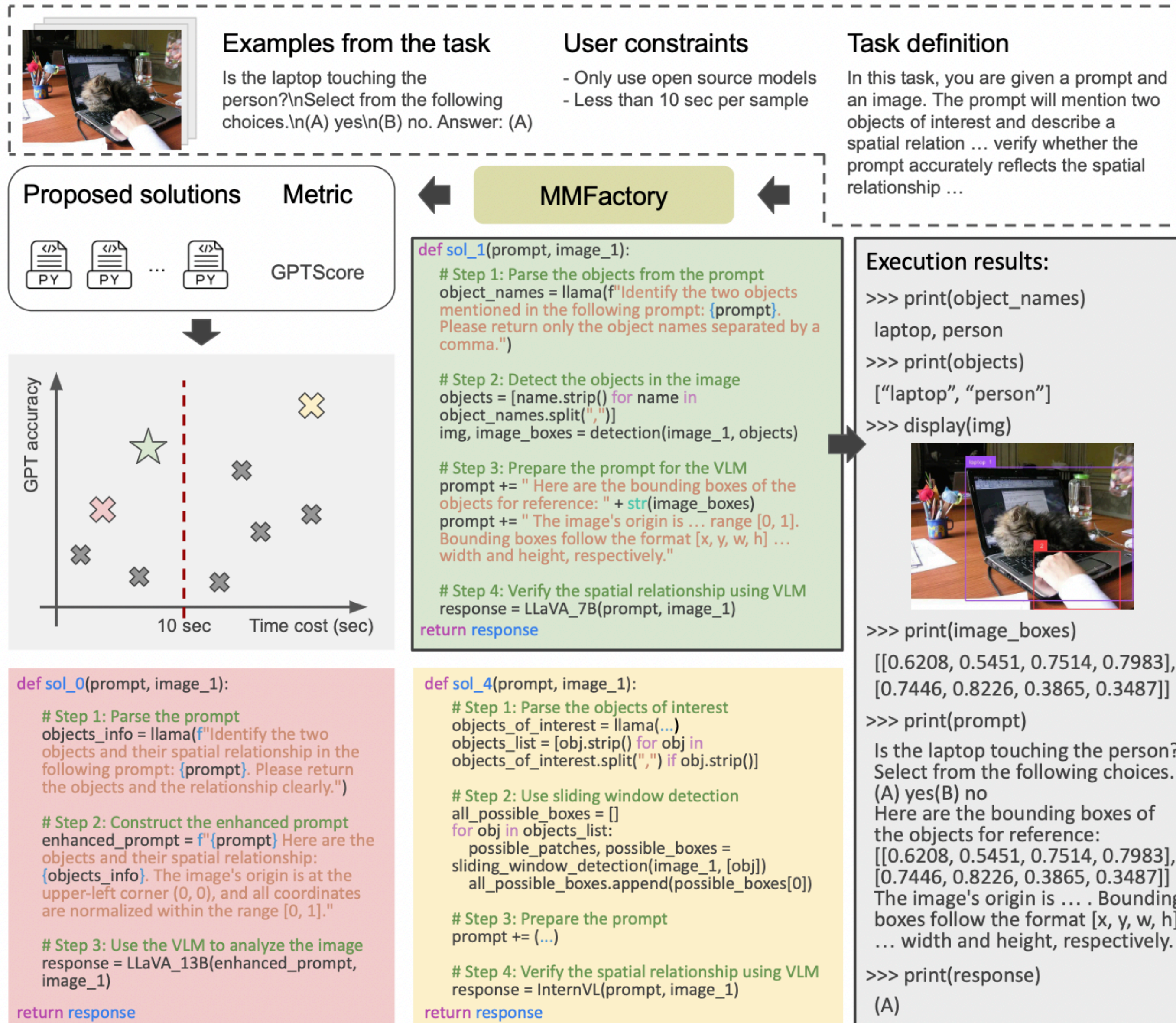
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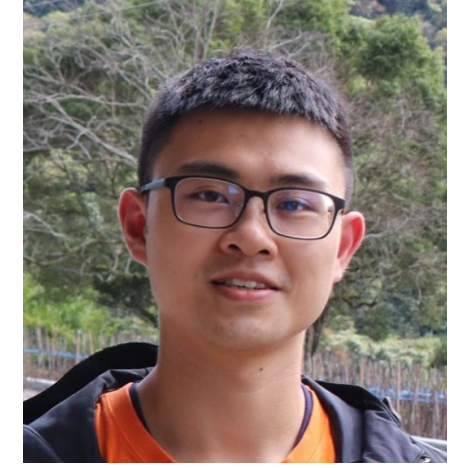
Visual Program Synthesis



Wan-Cyuan (Chris) Fan



Visual Program Synthesis



Wan-Cyuan (Chris) Fan

Method	Depth	Spatial	Jigsaw	Vis corr.	Sem. Corr.	Art	Count	Fun. Corr.	Local.	Multi-view	Refl.	Fore.	IQ	Sim.
Open-source multimodal LLMs														
OpenFlamingo-v2	<u>54.03</u>	43.36	47.33	25.58	30.22	52.14	21.67	36.15	<u>52.00</u>	41.35	43.28	15.91	23.33	<u>55.15</u>
InstructBLIP-7B	51.61	56.64	52.67	30.81	30.94	47.86	29.17	<u>23.85</u>	44.80	58.65	29.85	29.55	23.33	46.32
InstructBLIP-13B	51.61	65.73	52.67	29.65	<u>32.37</u>	50.43	30.83	22.31	<u>52.00</u>	54.14	46.27	13.64	26.00	46.32
CogVLM	50.81	67.13	52.67	20.93	23.57	49.57	<u>46.32</u>	<u>23.85</u>	43.20	<u>57.14</u>	26.87	24.24	26.67	46.32
LLaVA-v1.5-7B	52.42	61.54	11.33	25.58	23.02	47.86	43.33	21.54	48.80	49.62	36.57	<u>28.03</u>	24.00	46.32
LLaVA-v1.5-13B	53.23	67.83	<u>58.00</u>	29.07	<u>32.37</u>	47.86	50.00	20.77	47.20	41.35	<u>45.52</u>	<u>27.27</u>	<u>28.00</u>	46.32
Ours (LLaVA-7B)	51.61	78.82	56.67	<u>33.14</u>	<u>32.37</u>	<u>54.70</u>	41.23	21.54	56.56	55.64	37.04	26.52	23.33	58.52
Ours (LLaVA-13B)	58.06	<u>69.93</u>	64.00	34.30	34.53	58.12	47.24	<u>23.85</u>	51.64	51.13	45.06	26.52	28.00	45.93
API-based models														
Qwen-VL-Max	58.87	77.62	3.33	22.67	29.29	37.61	55.83	28.46	49.60	53.38	49.25	47.73	22.00	51.47
Gemini Pro	50.00	67.13	54.00	37.21	22.14	49.57	65.00	32.31	46.40	41.35	<u>46.27</u>	45.45	27.33	55.88
Claude 3 OPUS	57.26	57.34	32.67	31.40	20.71	<u>60.68</u>	49.17	22.31	46.40	<u>57.89</u>	27.61	<u>62.12</u>	21.33	70.59
GPT-4o	<u>74.19</u>	69.23	55.33	75.00	53.96	82.91	51.67	<u>39.23</u>	<u>56.00</u>	60.15	38.81	85.61	30.00	65.44
GPT-4o (+ SoM + orig.)	75.0	82.5	-	-	-	-	-	-	-	-	-	-	-	-
GPT-4o (+ Visprog)	46.8	37.8	-	-	-	-	-	-	-	-	-	-	-	-
GPT-4o (+ Sketchpad)	83.9	<u>81.1</u>	<u>70.7</u>	<u>80.8</u>	58.3	77.19	<u>66.67</u>	42.11	65.44	45.61	33.13	78.95	22.81	84.21
Ours (GPT-4o)	<u>80.25</u>	81.82	75.33	85.47	<u>58.27</u>	83.01	61.67	55.38	59.02	60.20	35.07	84.82	<u>28.67</u>	<u>75.32</u>

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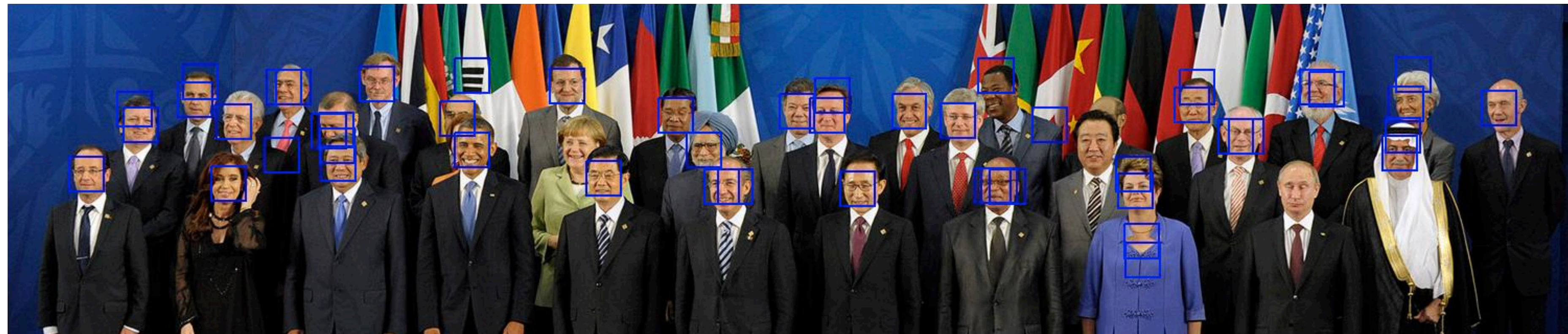
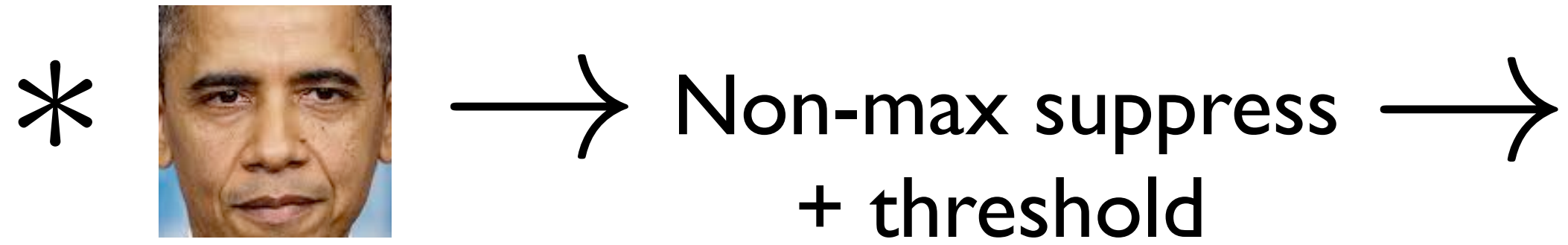


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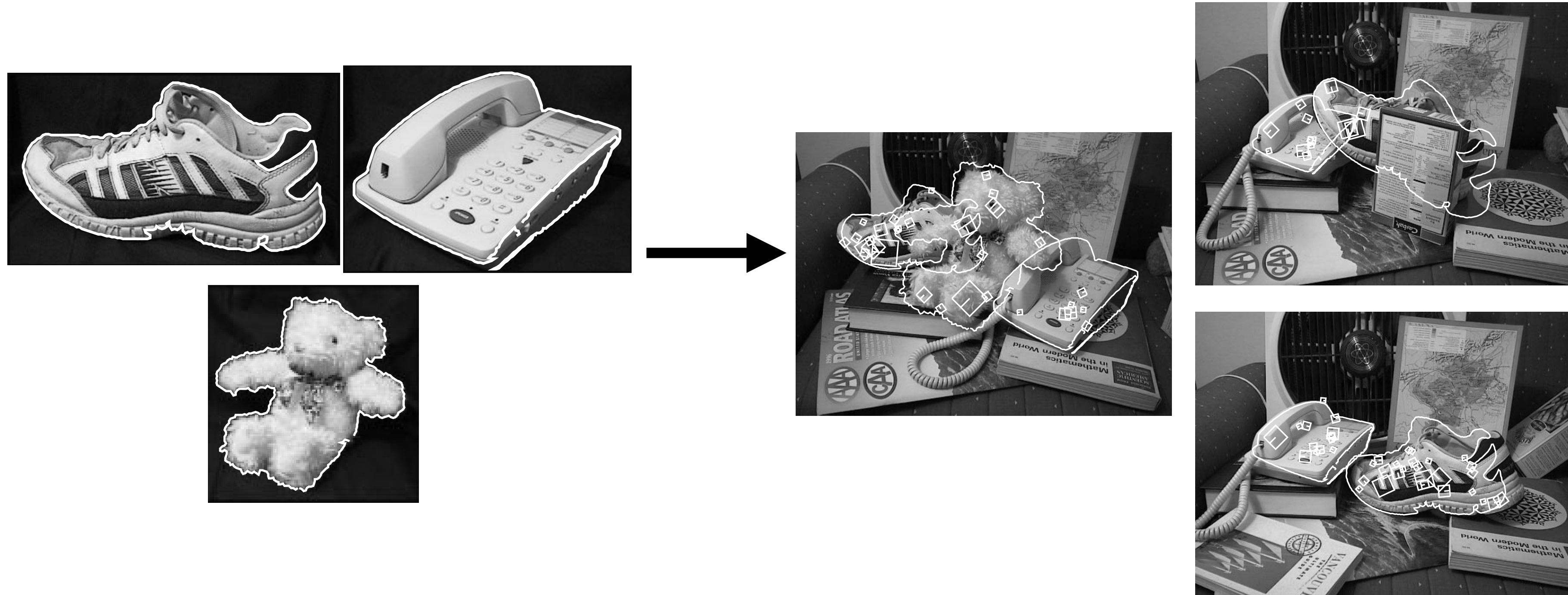
Object Recognition / Detection

Template matching ...



Object Recognition / Detection

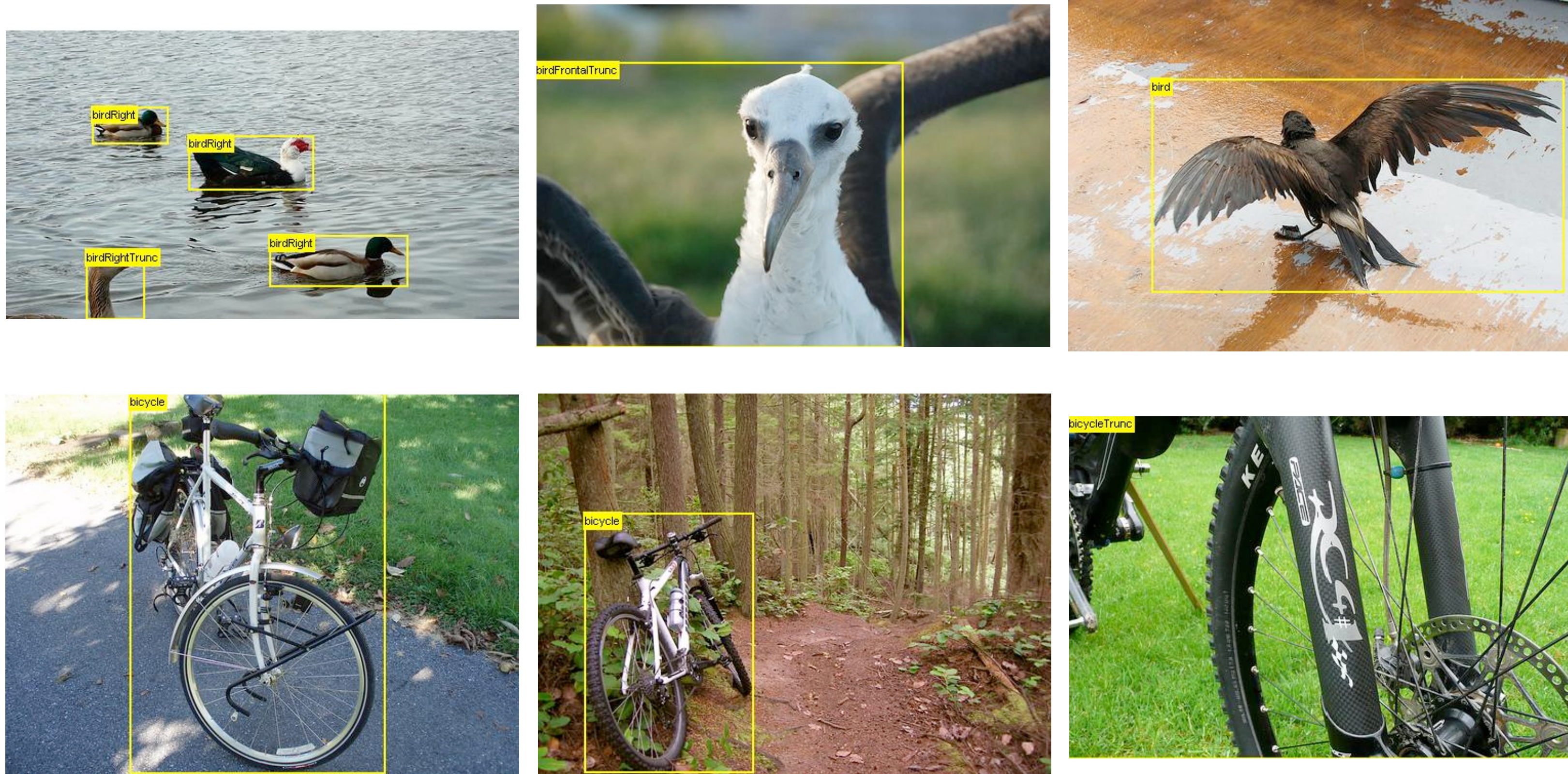
Object recognition with SIFT features and RANSAC [Lowe 1999]



What is present? Where? What orientation?

Object Recognition / Detection

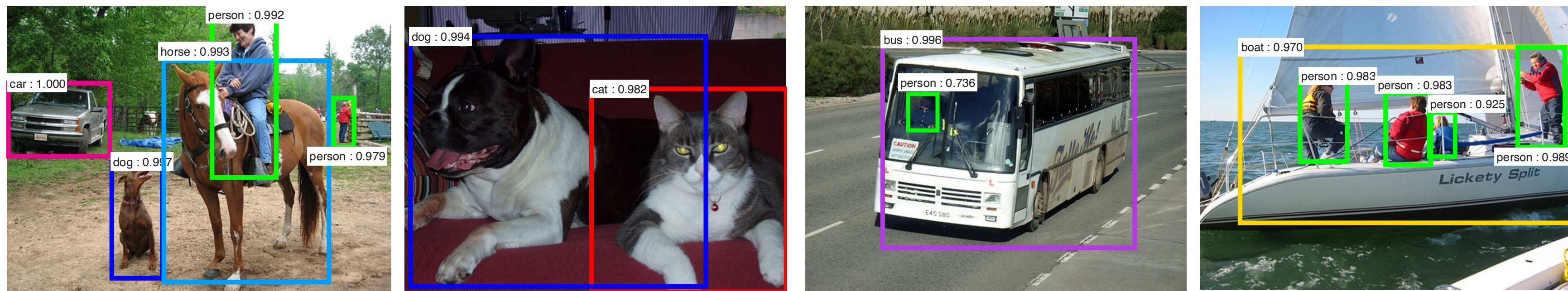
PASCAL Visual Object Classes Challenges [2005-2012]



What is present? Where? What orientation?

Object Classification and Detection

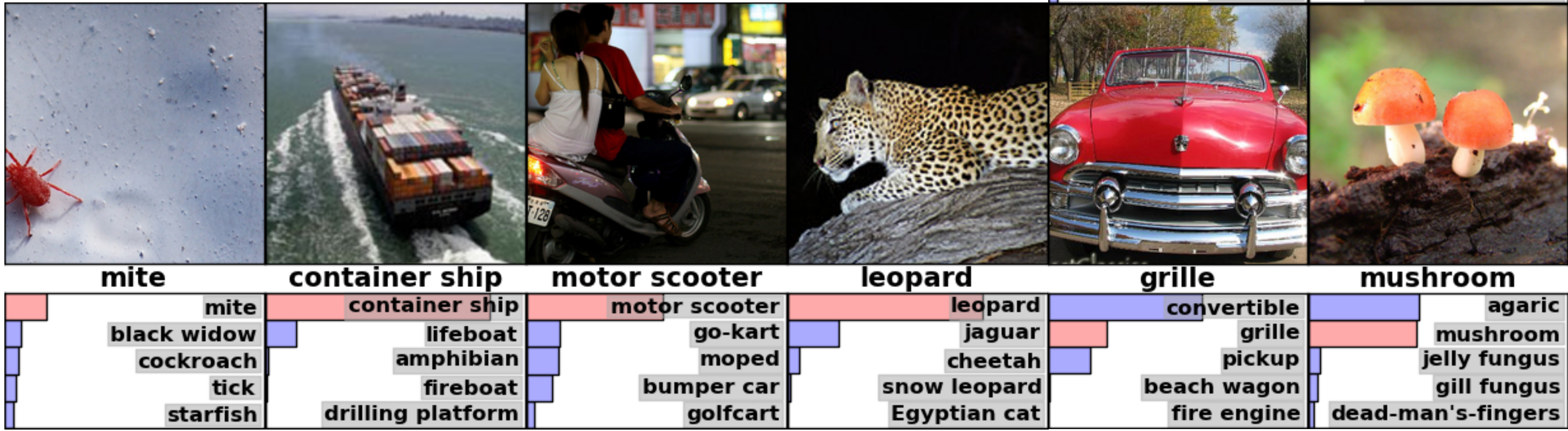
Detection: Label per region, e.g., PASCAL VOC



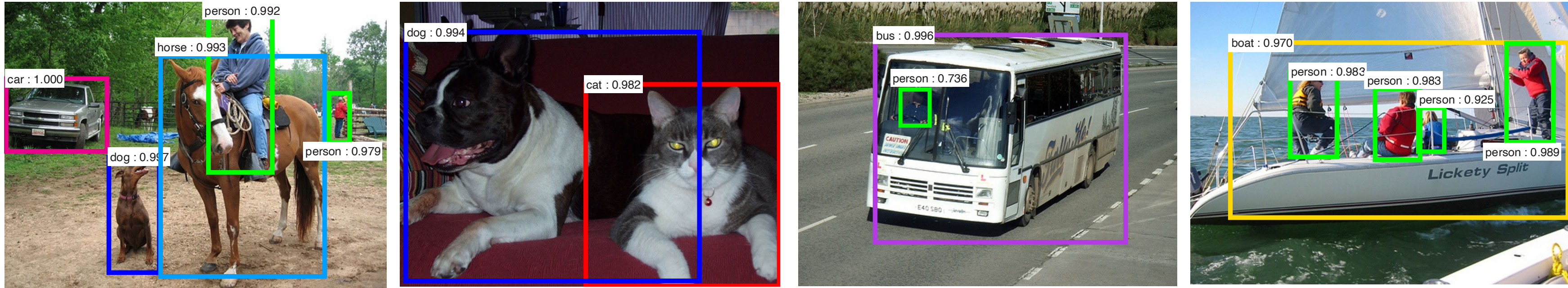
[Krizhevsky et al 2011] [Ren et al 2016]

Object Classification and Detection

Classification: Label per image, e.g., ImageNet



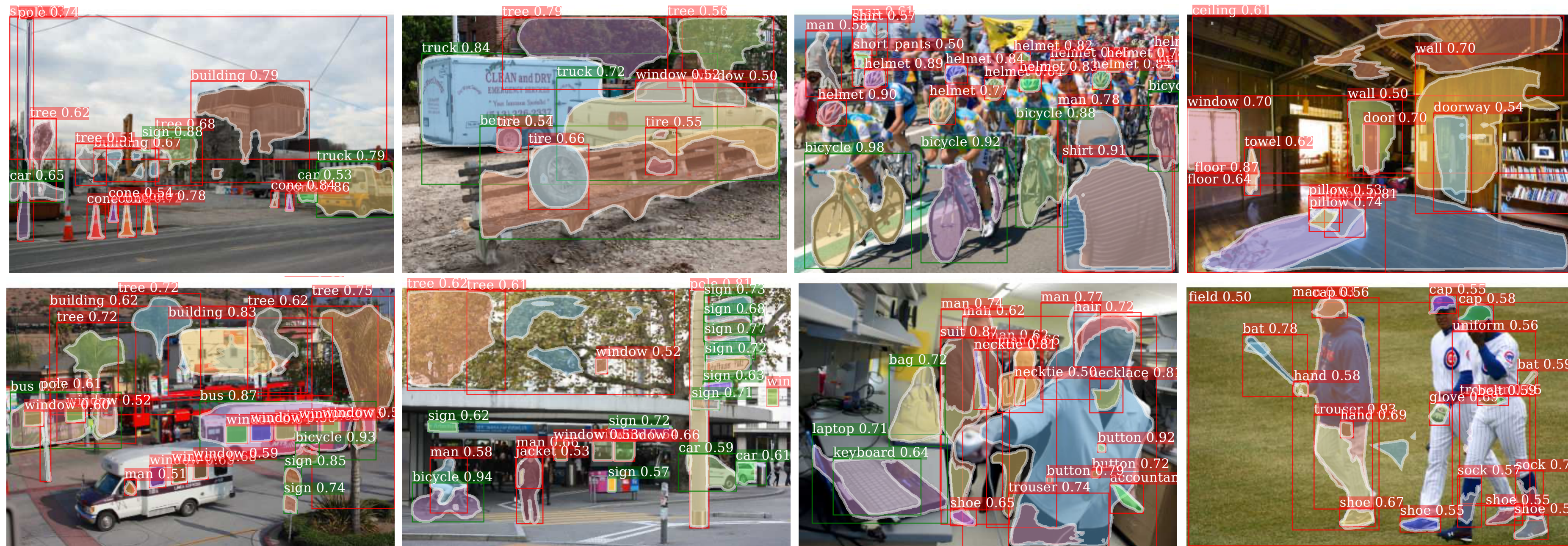
Detection: Label per region, e.g., PASCAL VOC



[Krizhevsky et al 2011] [Ren et al 2016]

Segmentation

Segmentation: Label per pixel, e.g., MS COCO

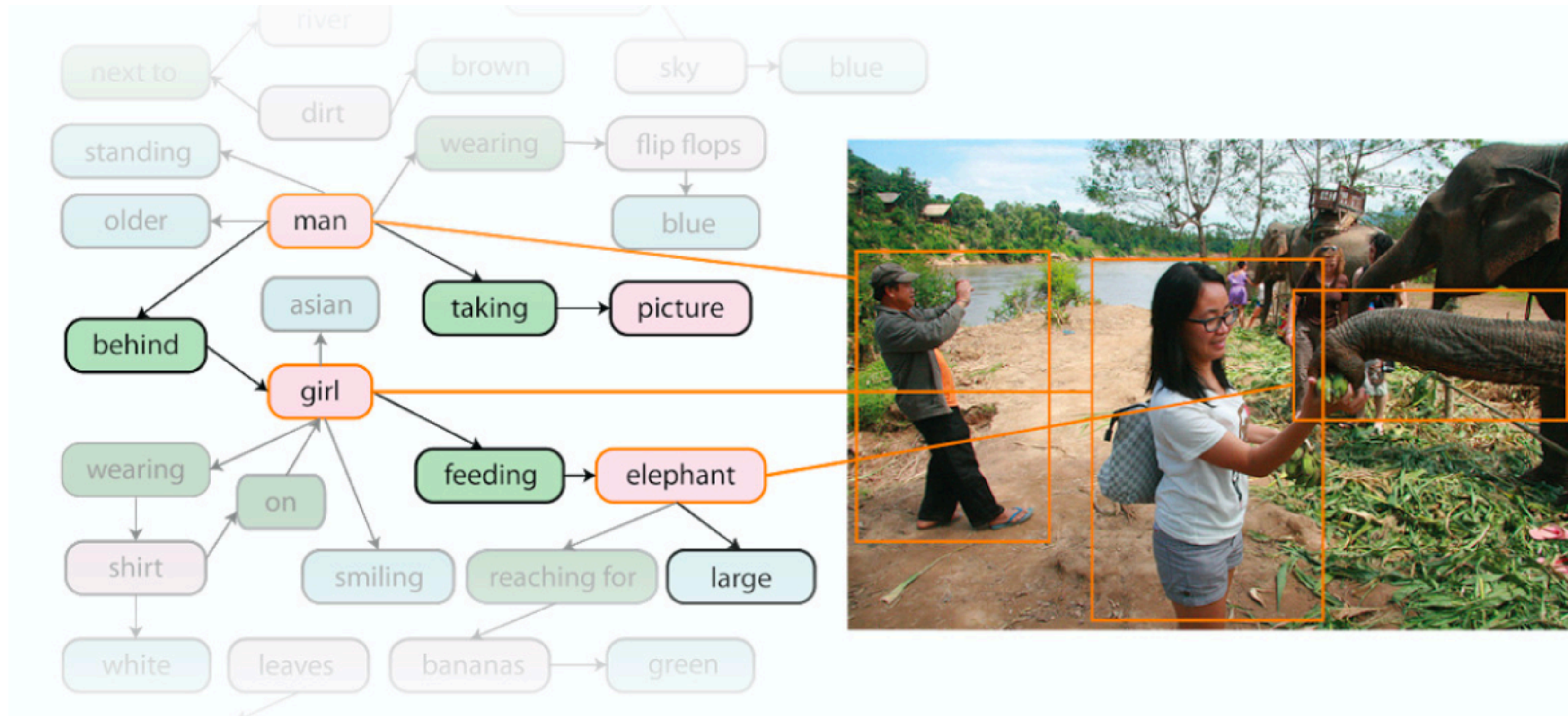


[Hu et al 2017]

Structured Image Understanding

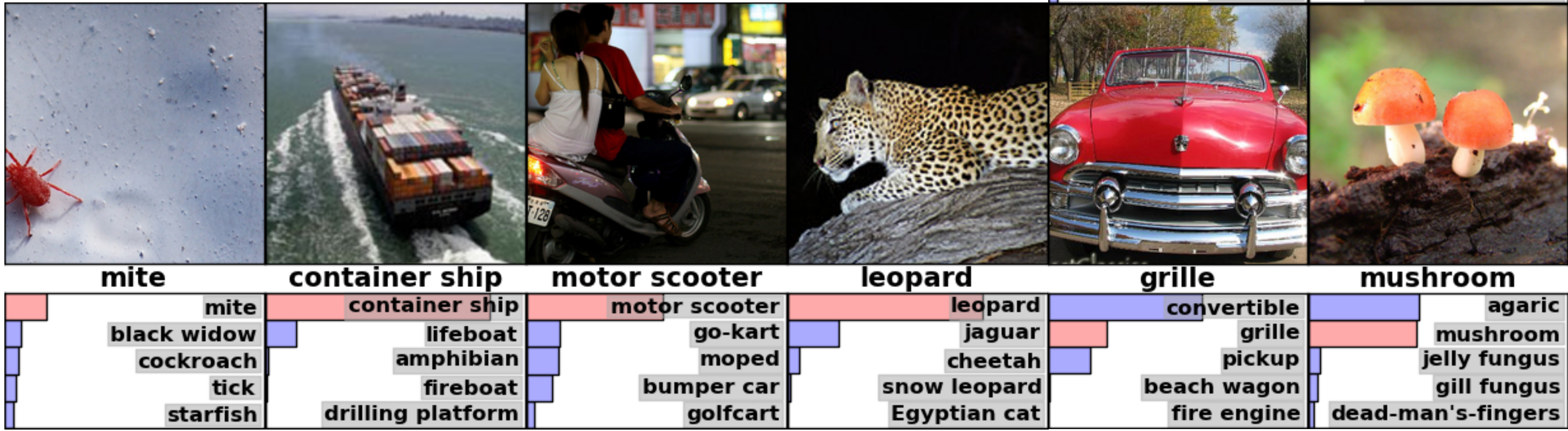
“Girl feeding large elephant”

“A man taking a picture behind girl”



Object Classification

Classification: Label per image, e.g., ImageNet



[Krizhevsky et al 2011] Ren et al 2016]

Classification: **Instance** vs. **Category**



Instance of Aeroplane (Wright Flyer)



Category of Aeroplane

Classification: **Instance** vs. **Category**



Instance of a cat



Category of domestic cats

Taxonomy of Cats

- ↳ Mammals (Class Mammalia)
- ↳ Therians (Subclass Theria)
- ↳ Placental Mammals (Infraclass Placentalia)
- ↳ Ungulates, Carnivorans, and Allies (Superorder Laurasiatheria)
- ↳ Carnivorans (Order Carnivora)
- ↳ Felines (Family Felidae)
- ↳ Small Cats (Subfamily Felinae)
- ↳ Genus *Felis*
 - ↳ Chinese Mountain Cat (*Felis bieti*)
 - ↳ Domestic Cat (*Felis catus*)
 - ↳ Jungle Cat (*Felis chaus*)
 - ↳ African Wildcat (*Felis lybica*)
 - ↳ Sand Cat (*Felis margarita*)
 - ↳ Black-footed Cat (*Felis nigripes*)
 - ↳ European Wildcat (*Felis silvestris*)

Bengal Tiger
[Omveer Choudhary]



Ocelot
[Jitze Couperus]



European Wildcat
[the wasp factory]



[[inaturalist.org](https://www.inaturalist.org)]

WordNet

We can use **language** to organize **visual categories**

This is the approach taken in **ImageNet** [Deng et al 2009], which uses the WordNet lexical database [wordnet.princeton.edu]

As in **language**, visual categories have **complex relationships**

e.g., a “sail” is part of a “sailboat” which is a “watercraft”

- **S: (n) sailboat, sailing boat** (a small sailing vessel; usually with a single mast)
 - **direct hyponym / full hyponym**
 - **S: (n) catboat** (a sailboat with a single mast set far forward)
 - **S: (n) sharpie** (a shallow-draft sailboat with a sharp prow, flat bottom, and triangular sail; formerly used along the northern Atlantic coast of the United States)
 - **S: (n) trimaran** (a fast sailboat with 3 parallel hulls)
 - **part meronym**
 - **direct hypernym / inherited hypernym / sister term**
 - **S: (n) sailing vessel, sailing ship** (a vessel that is powered by the wind; often having several masts)

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 - **S: (n) sailing vessel, sailing ship** (a vessel that is powered by the wind; often having several masts)

If we call a “**sailboat**” a **watercraft**, is this wrong? What if we call it a “**sail**”?

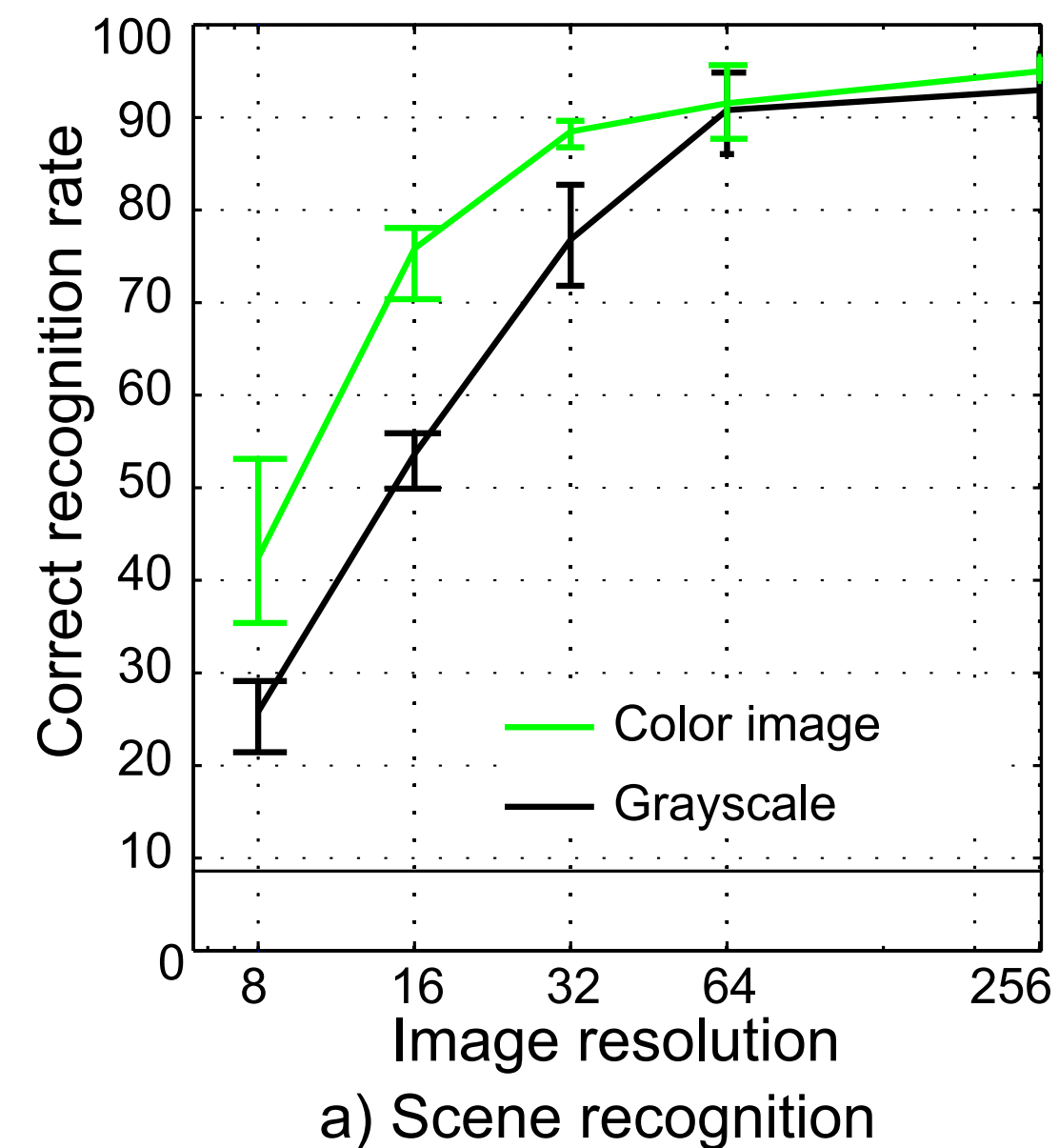
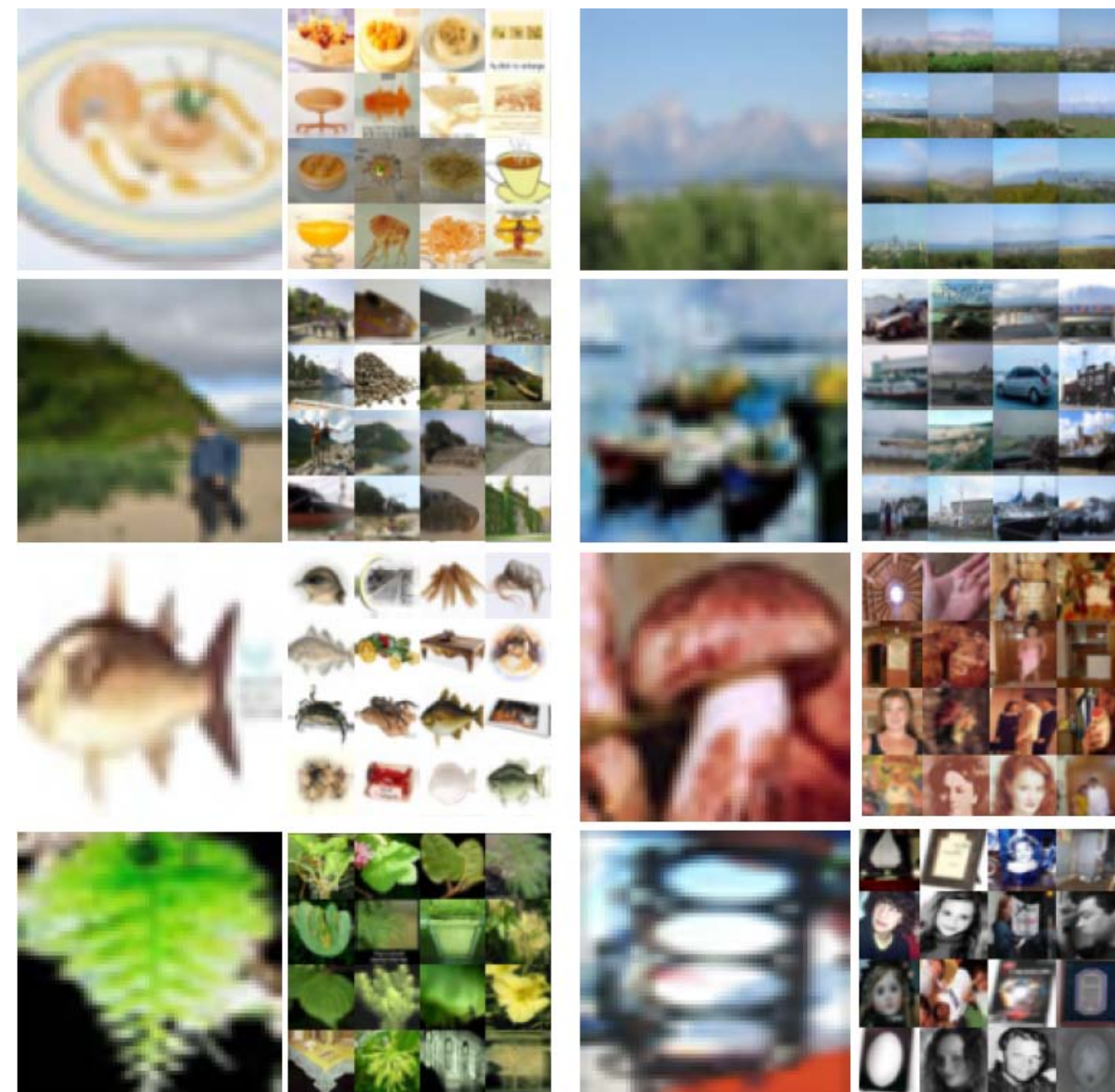
Tiny Image Dataset

Precursor to ImageNet and CIFAR10/100

80 million images collected via image search circa 2008 using 75,062 noun synsets from WordNet (labels are noisy)

Very small images (32x32xRGB) used to minimise storage

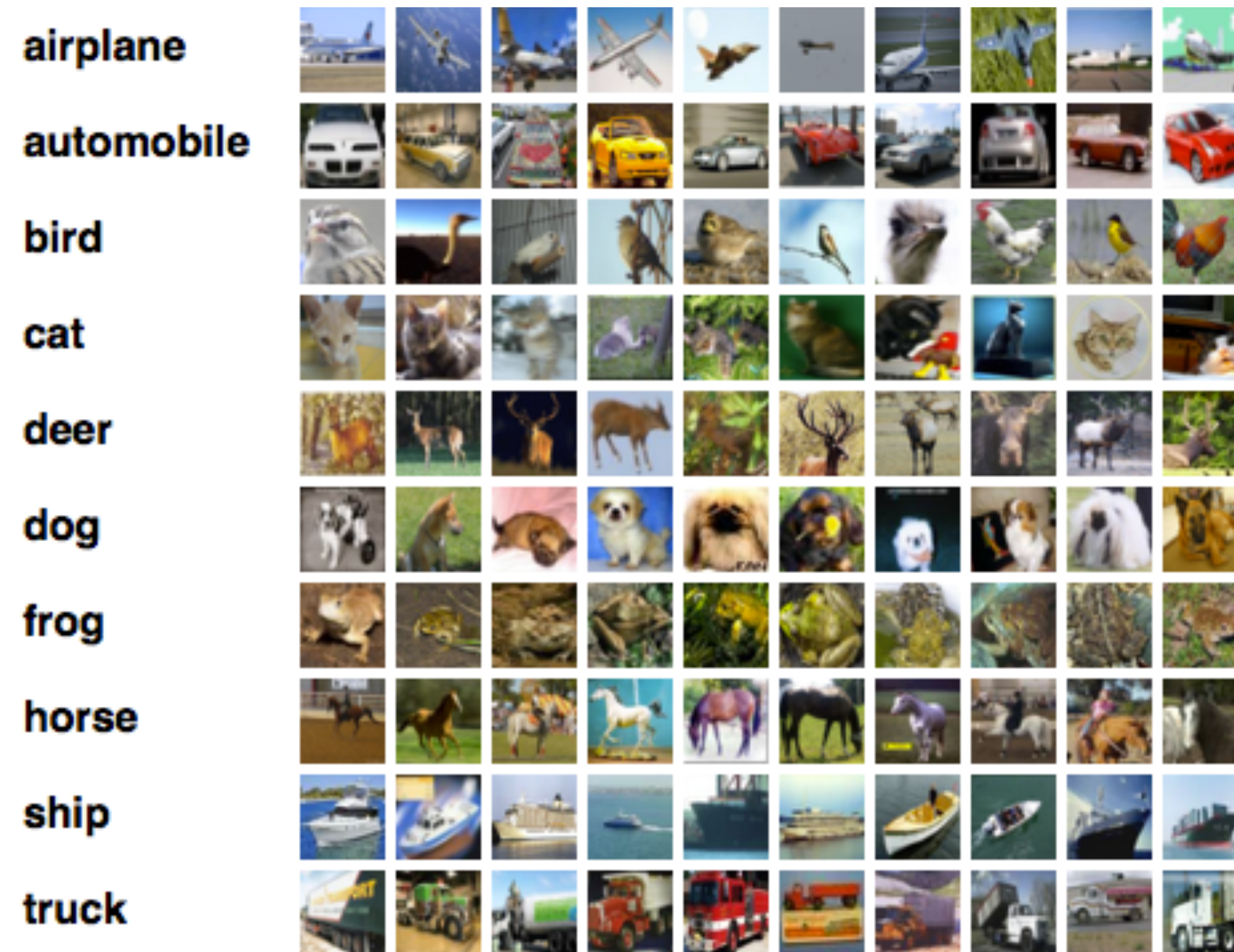
Note human performance is still quite good at this scale!



CIFAR10 Dataset

Hand labelled set of 10 categories from Tiny Images dataset

60,000 32x32 images in 10 classes (50k train, 10k test)



Good test set for visual recognition problems

Classification

Problem:

Assign new observations into one of a fixed set of categories (classes)

Key Idea(s):

Build a model of data in a given category based on observations of instances in that category

Classification



(assume given set of discrete labels)
{dog, cat, truck, plane, ...}



cat

Classification



08	02	22	97	38	15	00	40	00	75	04	05	07	78	52	12	50	77	91	88
49	49	99	40	17	81	18	57	60	87	17	40	98	43	69	48	04	56	62	00
81	49	31	73	55	79	14	29	93	71	40	67	52	88	30	03	49	13	36	65
52	70	95	23	04	60	11	42	69	24	68	56	01	32	56	71	37	02	36	91
22	31	16	71	51	67	03	59	41	92	36	54	22	40	40	28	66	33	13	80
24	47	39	80	99	03	45	02	44	75	33	53	78	36	84	20	35	17	12	50
32	98	81	28	64	23	67	10	26	38	40	67	59	54	70	66	18	38	64	70
67	26	20	68	02	62	12	20	95	63	94	39	63	08	40	91	66	49	94	21
24	55	58	05	66	73	99	26	97	17	78	78	96	83	14	88	34	89	63	72
21	36	23	09	75	00	76	44	20	45	35	14	00	61	33	97	34	31	33	95
78	17	53	28	22	75	31	67	15	94	03	80	04	62	16	14	09	53	56	92
16	39	05	42	96	35	31	47	55	58	88	24	00	17	54	24	36	29	85	57
86	56	00	48	35	71	89	07	05	44	44	37	44	60	21	58	51	54	17	58
19	80	81	68	05	94	47	69	28	73	92	13	86	52	17	77	04	89	55	40
04	52	08	83	97	35	99	16	07	97	57	32	16	26	26	79	33	27	98	66
59	36	68	87	57	62	20	72	03	46	33	67	46	55	12	32	63	93	53	69
04	42	16	73	35	35	39	11	24	94	72	18	08	46	29	32	40	62	76	36
20	69	36	41	72	30	23	88	34	63	99	69	82	67	59	85	74	04	36	16
20	73	35	29	78	31	90	01	74	31	49	71	48	86	81	16	23	57	05	54
01	70	54	71	83	51	54	69	16	92	33	48	61	43	52	01	89	13	67	48

What the computer sees

image classification →

- 82% cat
- 15% dog
- 2% hat
- 1% mug

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A **classifier** is a procedure that accepts as input a set of features and outputs a class **label** (probability over class labels)

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Classifiers can be **binary** (face vs. not-face) or **multi-class** (cat, dog, horse, ...).

Binary: $[0]/[1]$

Multi-class: $[1, 0, 0, 0, \dots]$ (one-hot)

$[9]$ (label)

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We build a classifier using a **training set** of labelled examples $\{(\mathbf{x}_i, y_i)\}$, where each \mathbf{x}_i is a feature vector and each y_i is a class label.

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We build a classifier using a **training set** of labelled examples $\{(\mathbf{x}_i, y_i)\}$, where each \mathbf{x}_i is a feature vector and each y_i is a class label.

Given a previously unseen observation, we use the classifier to predict its class label.

Binary: $[0]/[1]$

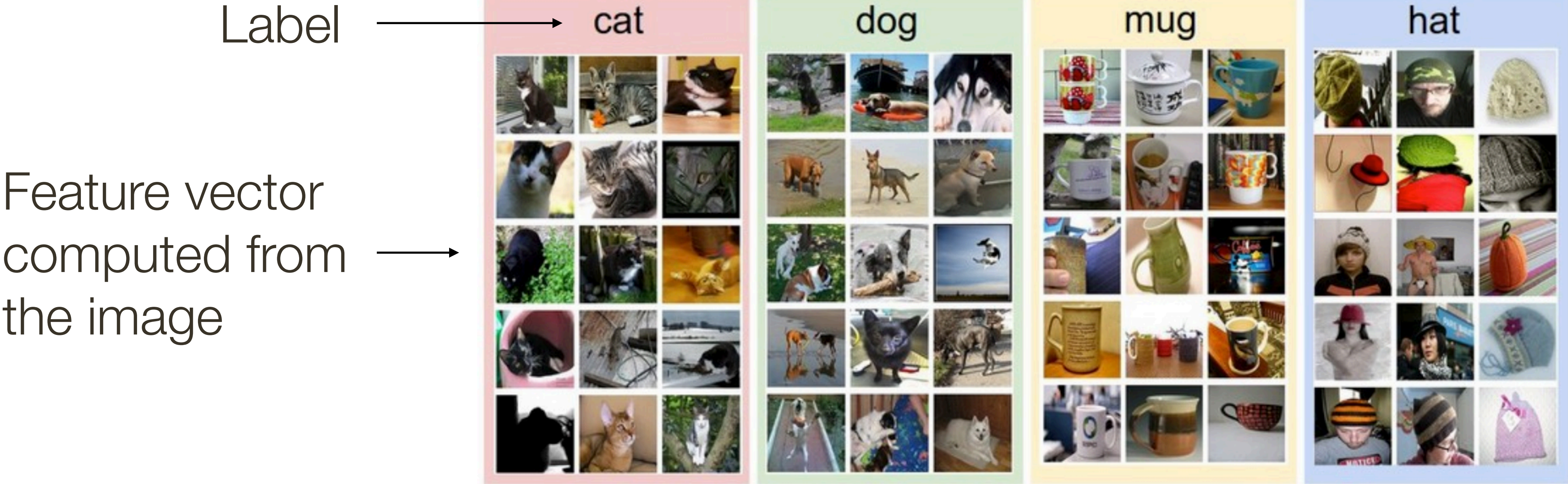
Multi-class: $[1, 0, 0, 0, \dots]$ (one-hot)

$[9]$ (label)

Classification

- Collect a database of images with labels
- Use ML to train an image classifier
- Evaluate the classifier on test images

Example training set



Example 1: A Toy Classification Problem

Categorize images of fish

— “Atlantic salmon” vs “Pacific salmon”

Use **features** such as length, width, lightness, fin shape & number, mouth position, etc.

Given a previously unobserved image of a salmon, use the learned classifier to guess whether it is an Atlantic or Pacific salmon

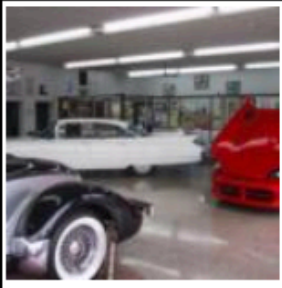
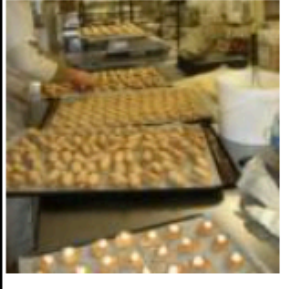

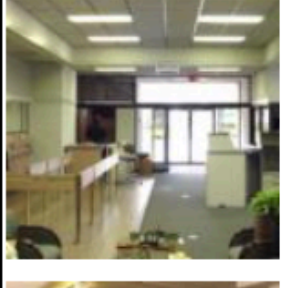
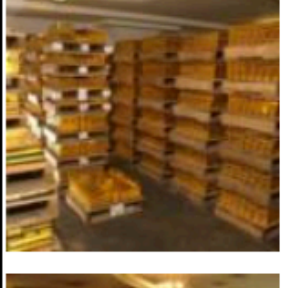





Figure credit: Duda & Hart

Example 2: Real Classification Problem

SUN Dataset

- 131K images
- 908 **scene** categories

indoor	shopping and dining		auto showroom
outdoor natural	workplace (office building, factory, lab, etc.)		bakery kitchen
outdoor man-made	home or hotel		bakery shop
	transportation (vehicle interiors, stations, etc.)		bank indoor
	sports and leisure		bank vault
	cultural (art, education, religion, military, law, politics, etc.)		banquet hall
			bar
			

Example 3: Real Classification Problem

ImageNet Dataset

- 14 Million images
- 21K **object** categories

Natural object

An object occurring naturally; not made by man

0 pictures
82.76% Popularity Percentile
Wordnet IDs

- Numbers in brackets: (the number of synsets in the subtree).
- ImageNet 2011 Fall Release (32326)
 - plant, flora, plant life (4486)
 - geological formation, formation (1)
 - aquifer (0)
 - beach (1)
 - cave (3)
 - cliff, drop, drop-off (2)
 - delta (0)
 - diapir (0)
 - folium (0)
 - foreshore (0)
 - ice mass (10)
 - lakefront (0)
 - massif (0)
 - monocline (0)
 - mouth (0)
 - natural depression, depression (0)
 - natural elevation, elevation (41)
 - oceanfront (0)
 - range, mountain range, range of mountains (0)
 - relict (0)
 - ridge, ridgeline (2)
 - ridge (0)
 - shore (7)
 - slope, incline, side (17)
 - spring, fountain, outflow, outpouring, talus, scree (0)
 - vein, mineral vein (1)
 - volcanic crater, crater (2)
 - wall (0)
 - water table, water level, ground

Treemap Visualization Images of the Synset Downloads

ImageNet 2011 Fall Release Natural object

Plant

Covering

Sample Extraterrestrial Body

Asterism Mechanism Celestial

Radiator Body Rock

Tangle Nest

Example 3: Real Classification Problem

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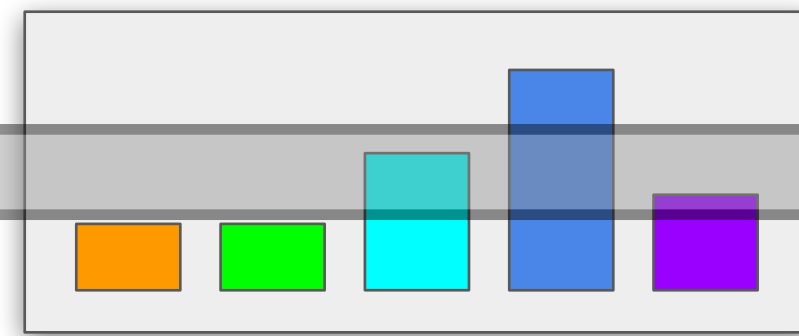
Tangle Nest

Closed-world problem

Issue: Classification assumes that incoming image belongs to one of k classes. However, in practice it is impossible to enumerate all relevant classes in the world, nor would doing so be useful. So how do we deal with images which don't belong?

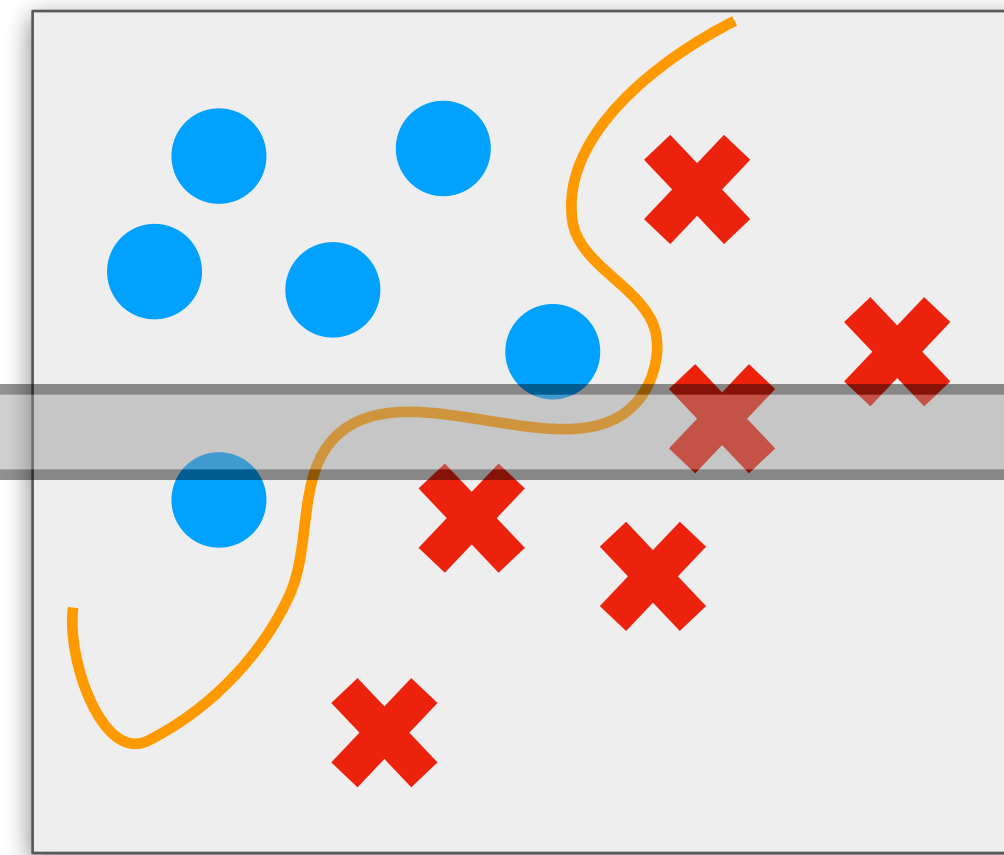
Solution: Create an “unknown” or “irrelevant” class.

Traditional Image Classification Pipeline



Features

HoG
SIFT
Daisy
...



ML model

SVM
Random Forests
...

Answer

Traditional Image Classification Pipeline

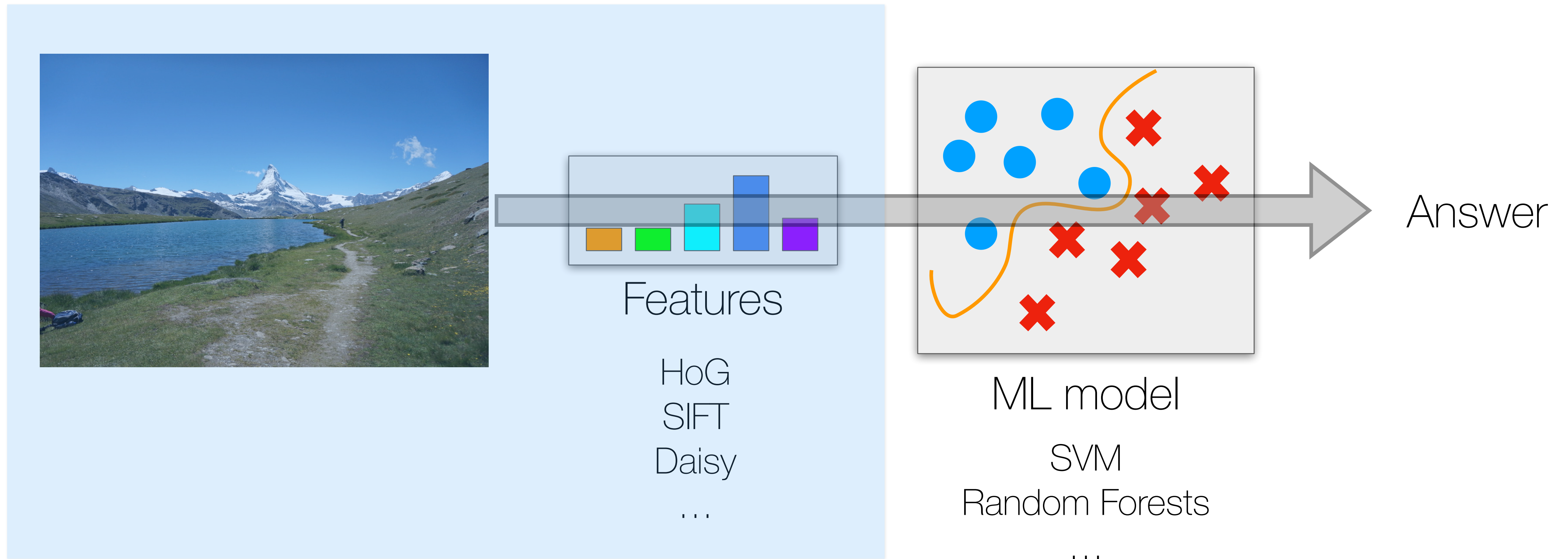


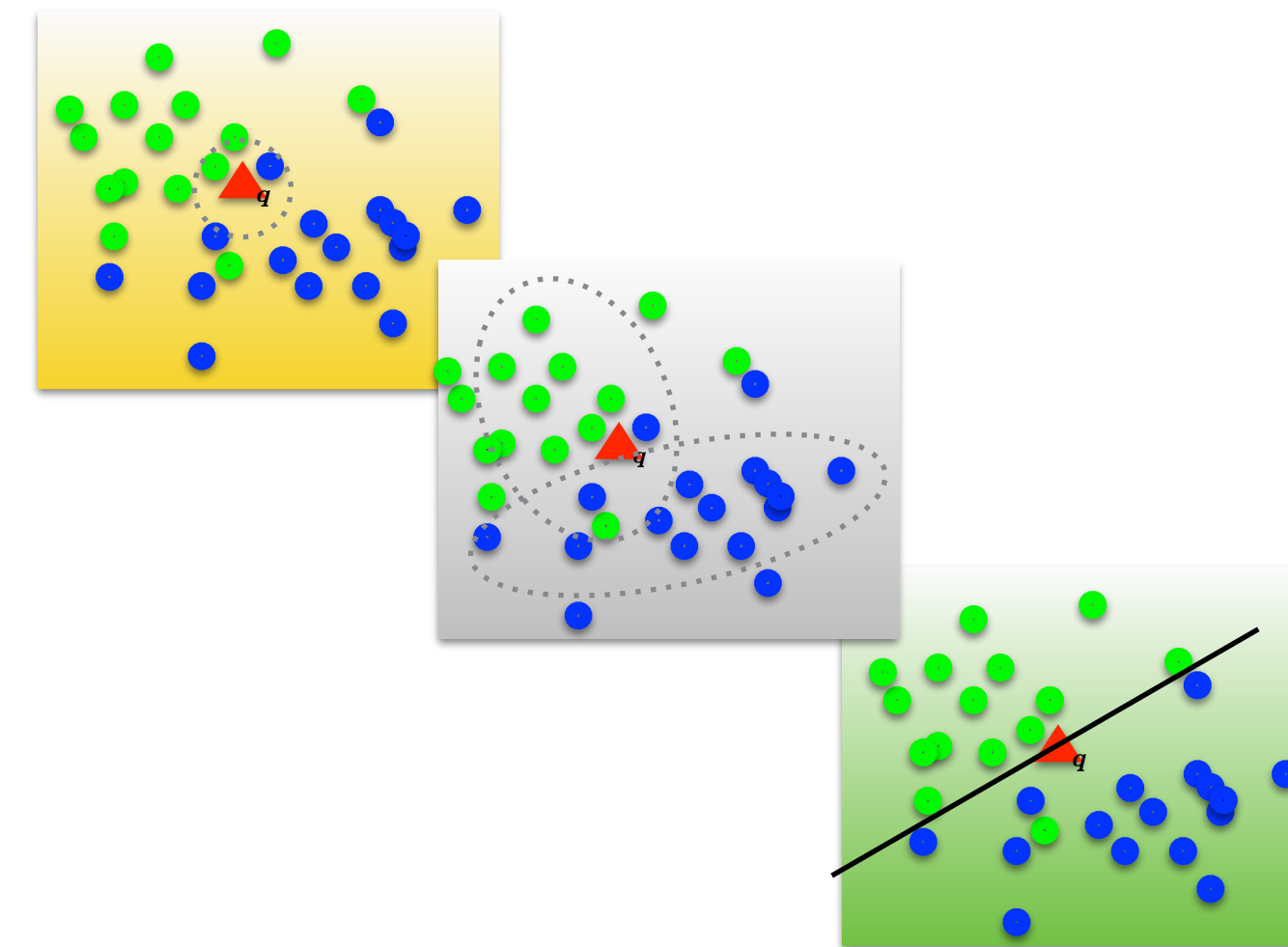
Image Classification

Representation of Images

- Image pixels directly
- Bag of Words

Classification Algorithms

- Bayes' Classifier
- Nearest Neighbor Classifier
- SVM Classifier



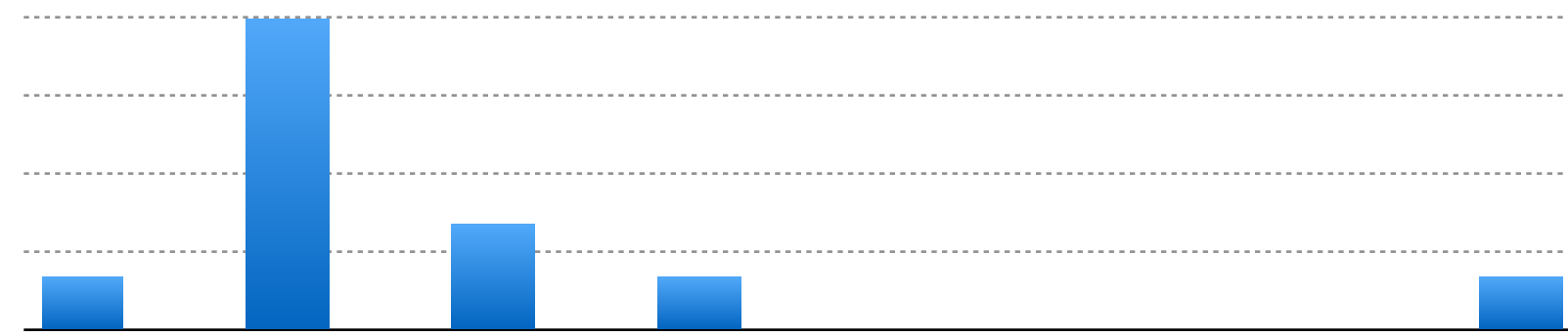
Visual **Words**

Many algorithms for image classification accumulate evidence on the basis of **visual words**.

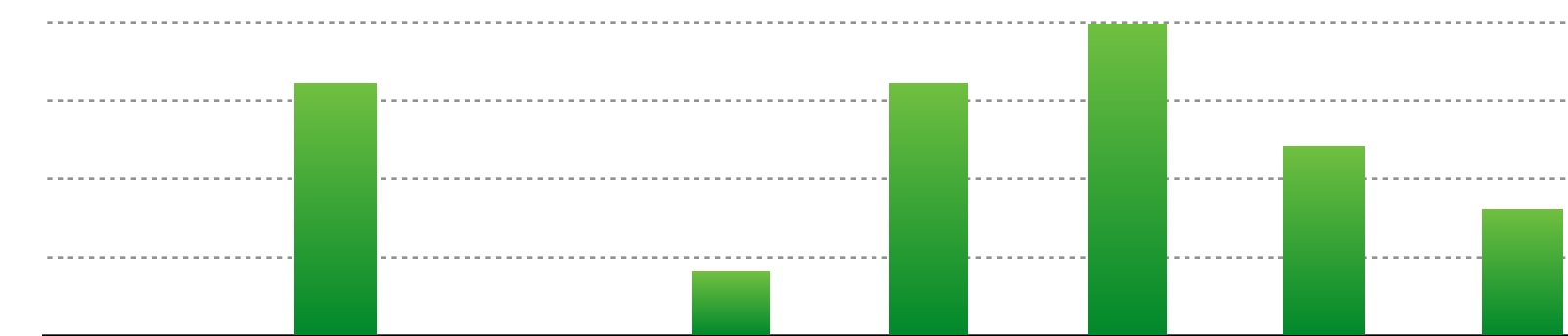
To classify a text document (e.g. as an article on sports, entertainment, business, politics) we might find patterns in the occurrences of certain words.

Vector Space Model

G. Salton. 'Mathematics and Information Retrieval' Journal of Documentation, 1979



1	6	2	1	0	0	0	1
Tartan	robot	CHIMP	CMU	bio	soft	ankle	sensor



0	4	0	1	4	5	3	2
Tartan	robot	CHIMP	CMU	bio	soft	ankle	sensor

<http://www.fodey.com/generators/newspaper/snippet.asp>

Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)

Vector Space Model

A document (datapoint) is a vector of counts over each word (feature)

$$\mathbf{v}_d = [n(w_{1,d}) \quad n(w_{2,d}) \quad \cdots \quad n(w_{T,d})]$$

$n(\cdot)$ counts the number of occurrences

just a histogram over words



What is the similarity between two documents?

Vector Space Model

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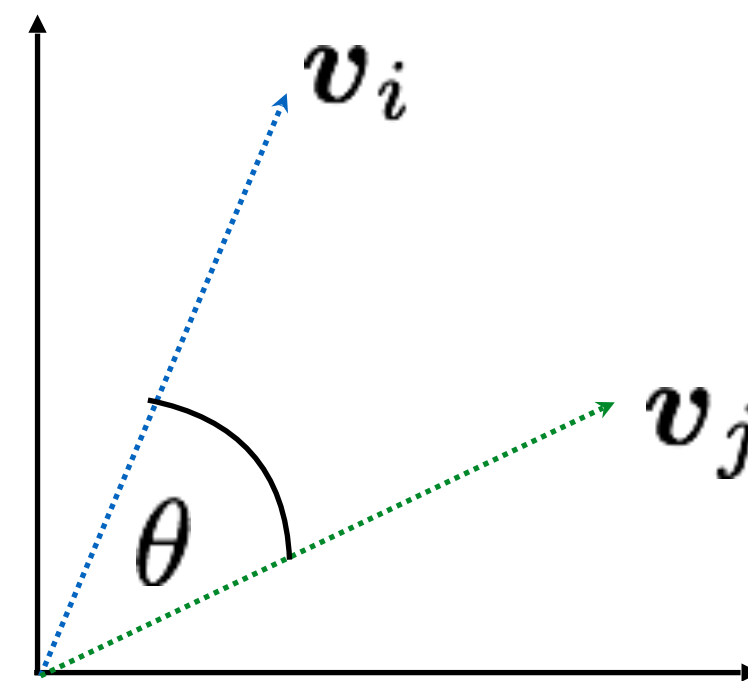
just a histogram over words



What is the similarity between two documents?

Use any distance you want but the cosine distance is fast and well designed for high-dimensional vector spaces:

$$\begin{aligned} d(\mathbf{v}_i, \mathbf{v}_j) &= \cos \theta \\ &= \frac{\mathbf{v}_i \cdot \mathbf{v}_j}{\|\mathbf{v}_i\| \|\mathbf{v}_j\|} \end{aligned}$$



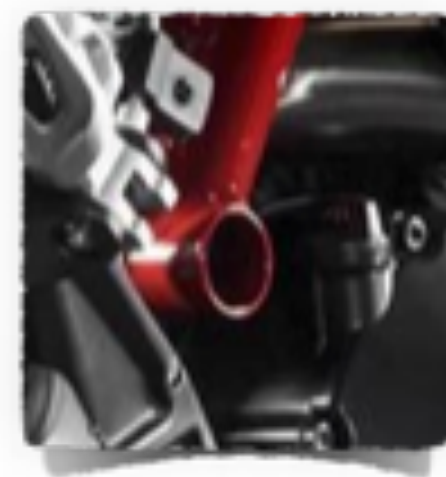
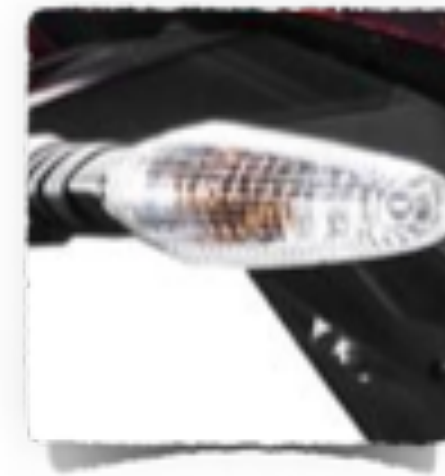
Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)

Visual **Words**

In images, the equivalent of a **word** is a **local image patch**. The local image patch is described using a descriptor such as SIFT.

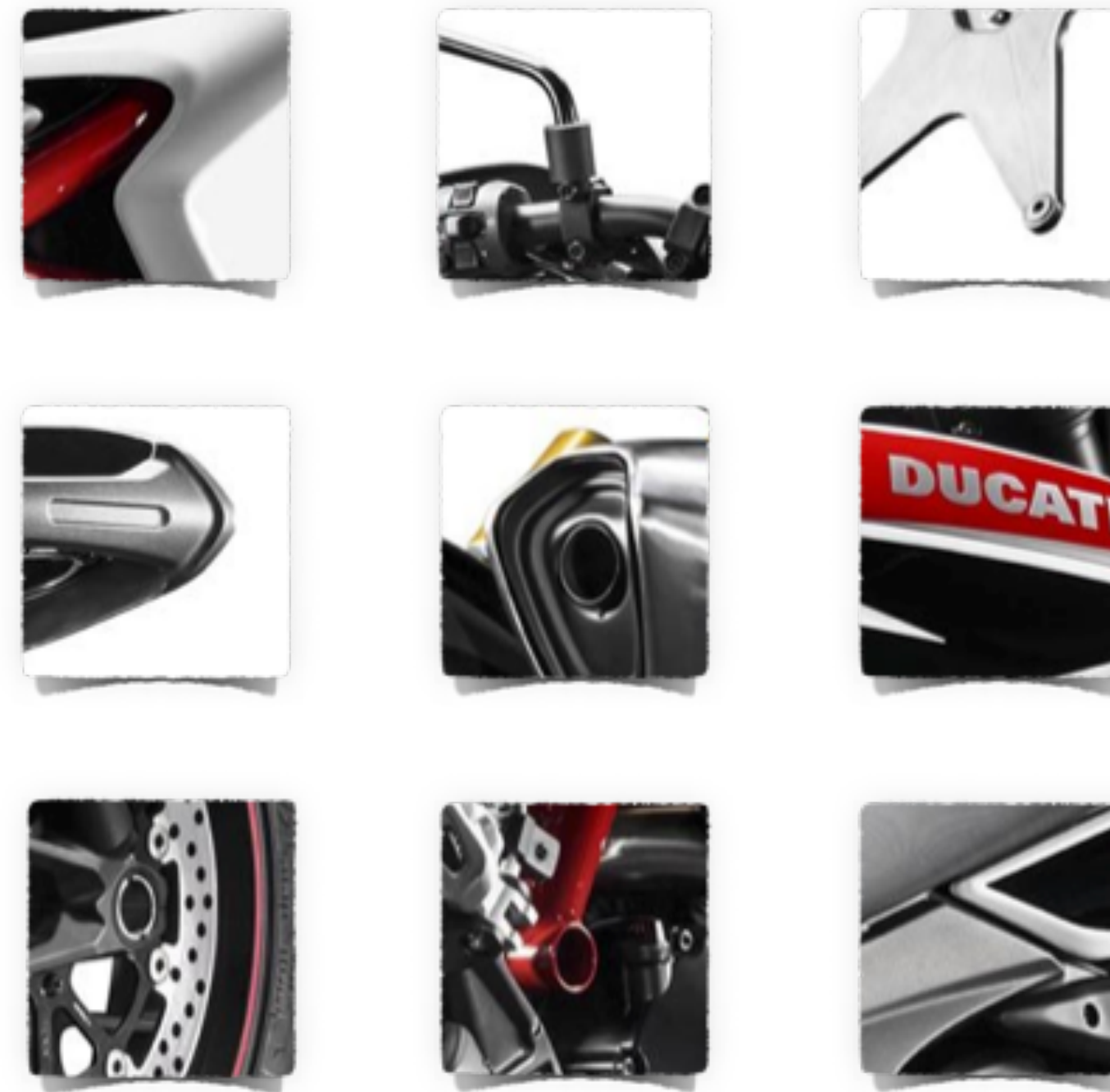
We construct a **vocabulary** or **codebook** of local descriptors, containing representative local descriptors.

What **Objects** do These Parts Belong To?



Some local feature are very informative

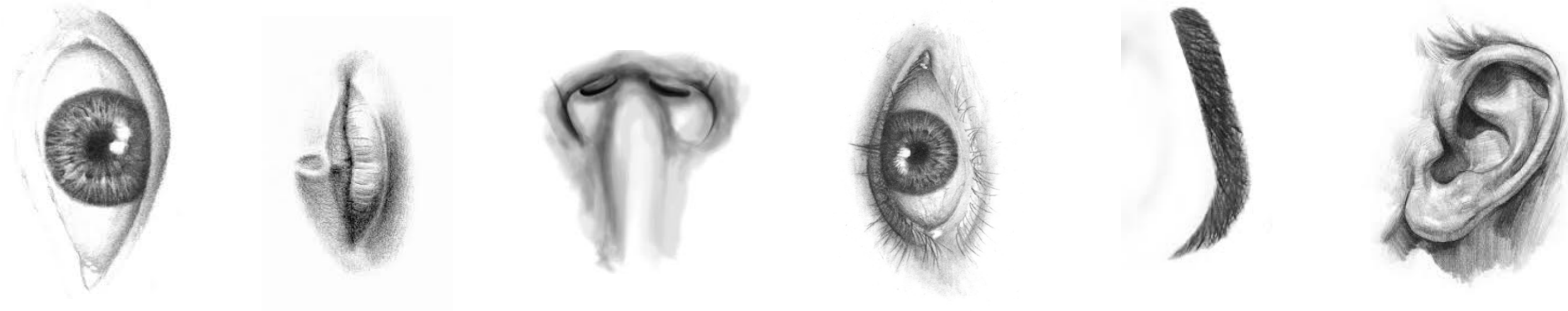
An object as



a collection of local features
(bag-of-features)

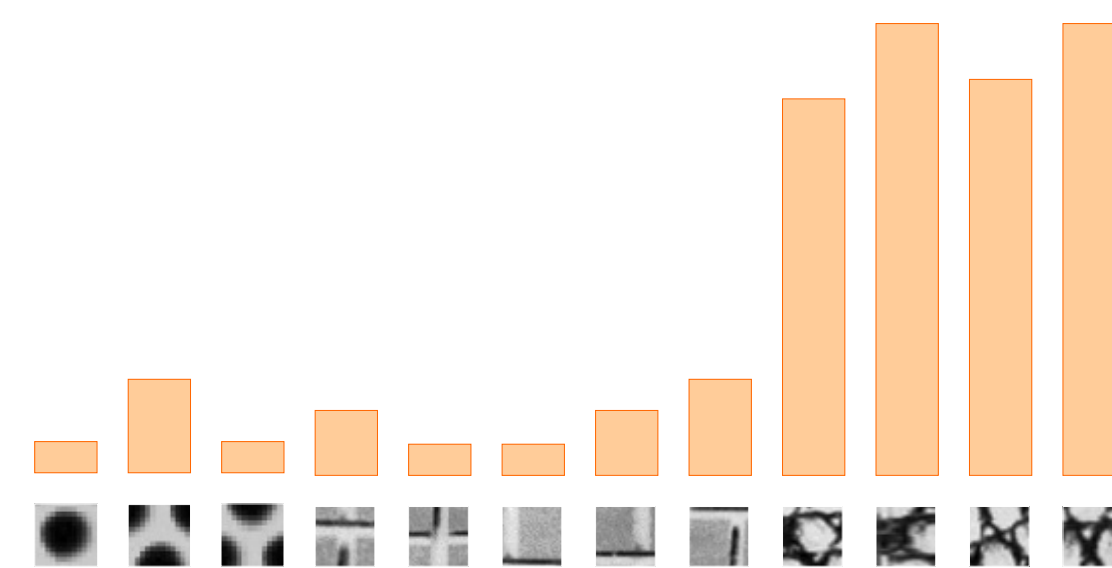
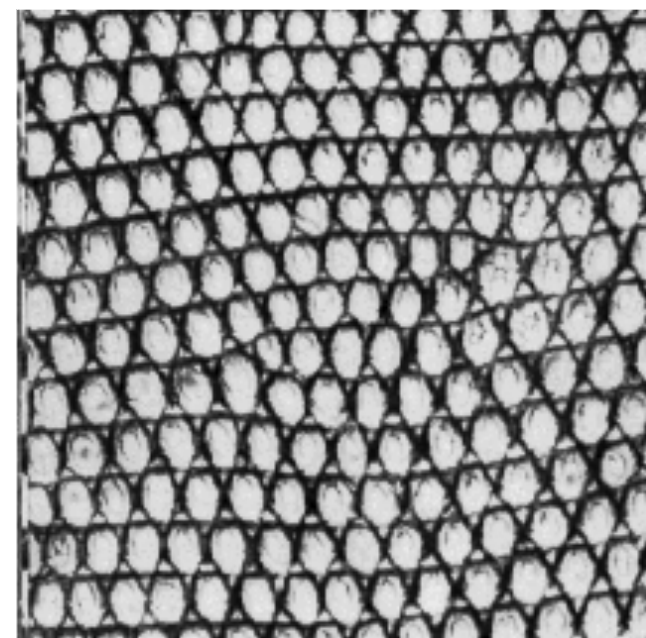
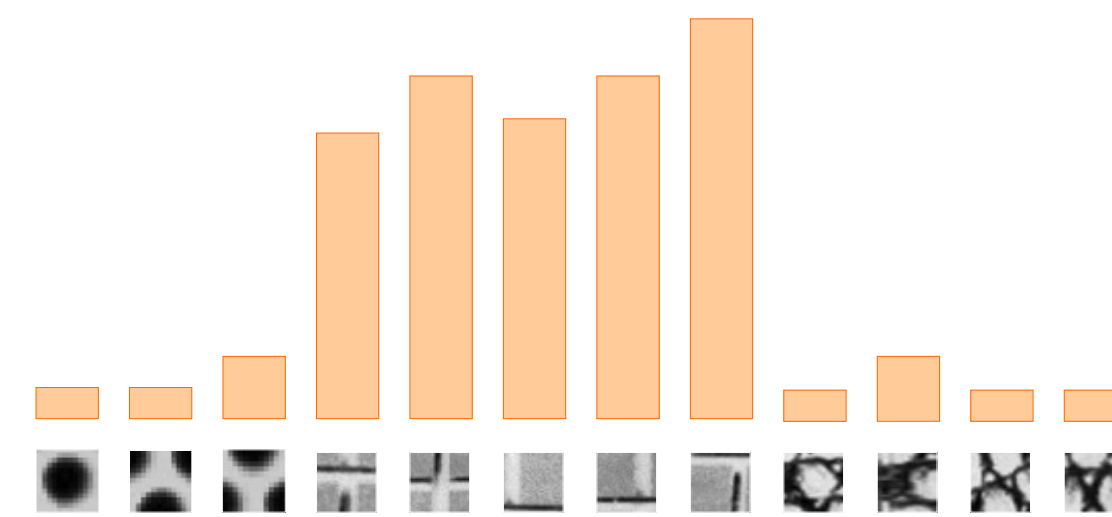
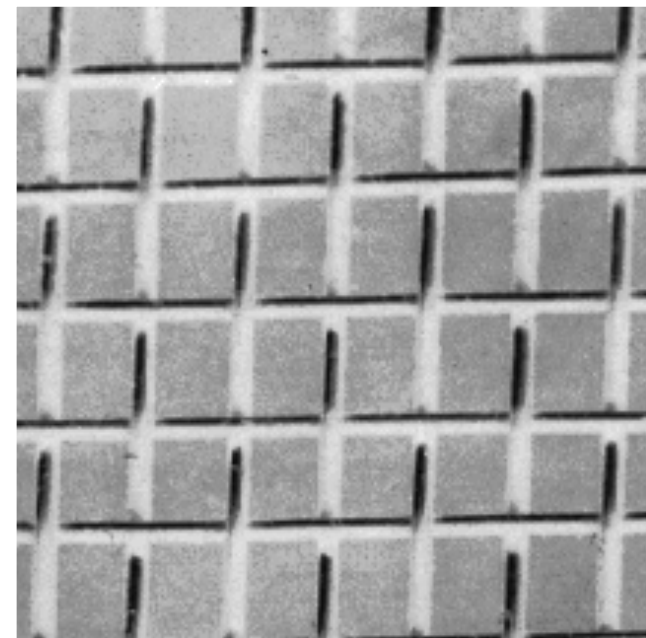
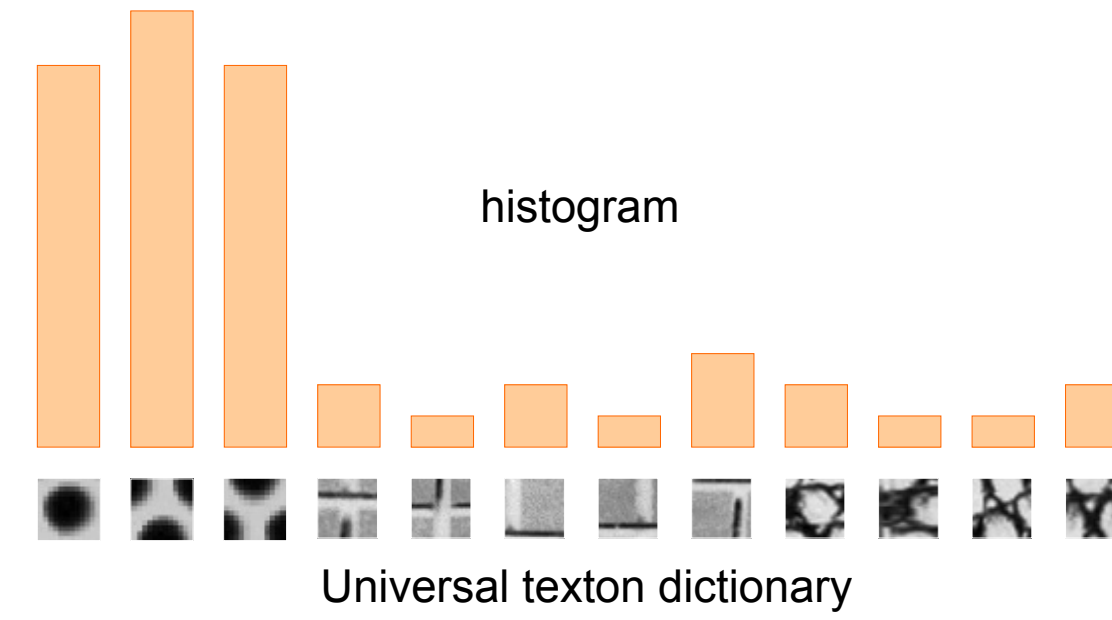
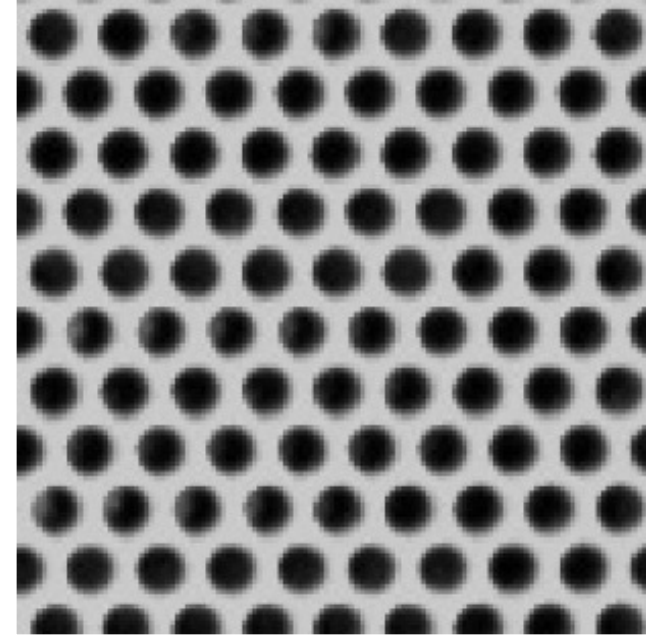
- deals well with occlusion
- scale invariant
- rotation invariant

(not so) Crazy Assumption



spatial information of local features
can be ignored for object recognition (i.e., verification)

Recall: Texture Representation



Standard **Bag-of-Words** Pipeline (for image classification)

Dictionary Learning:

Learn Visual Words using clustering

Encode:

build Bags-of-Words (BOW) vectors
for each image

Classify:

Train and test data using BOWs

Standard **Bag-of-Words** Pipeline (for image classification)

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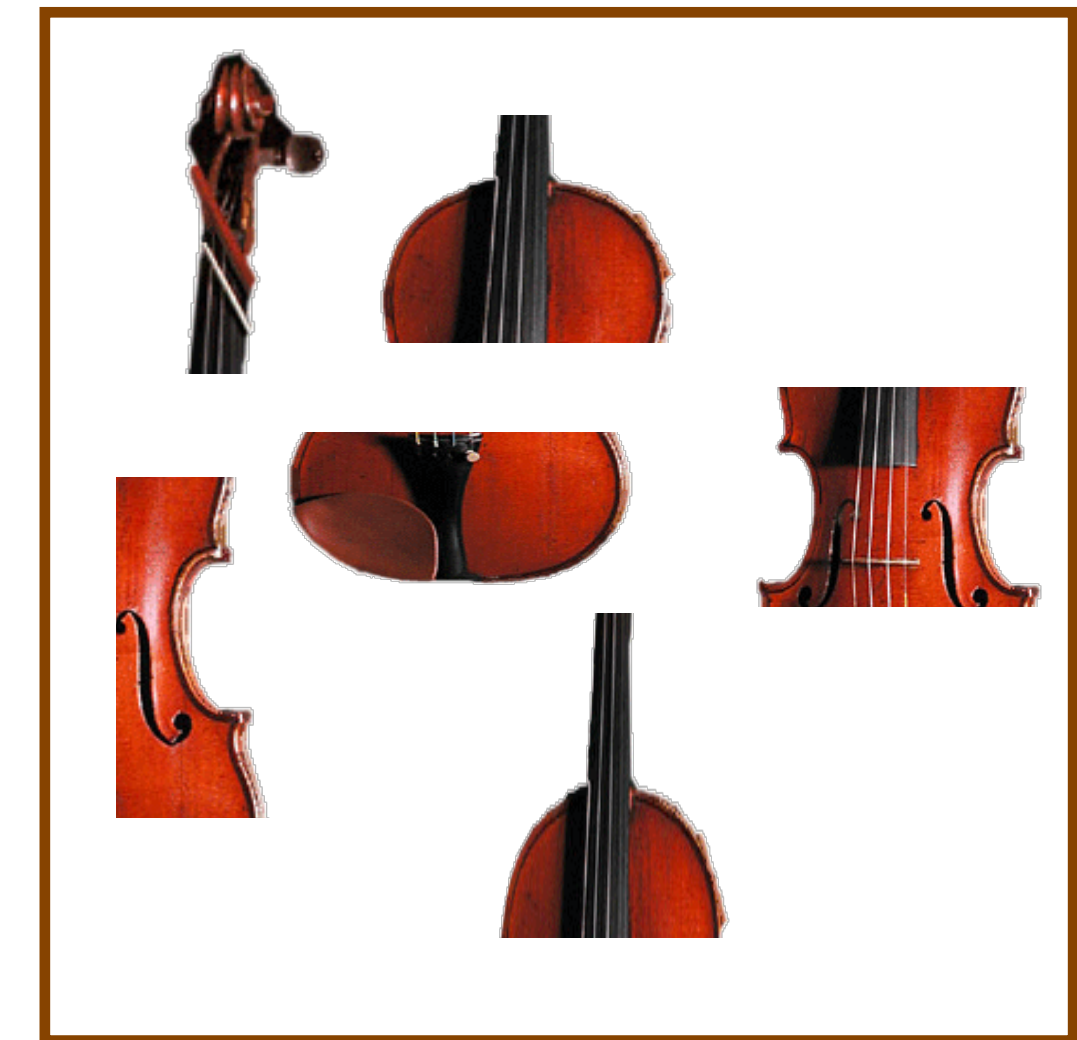
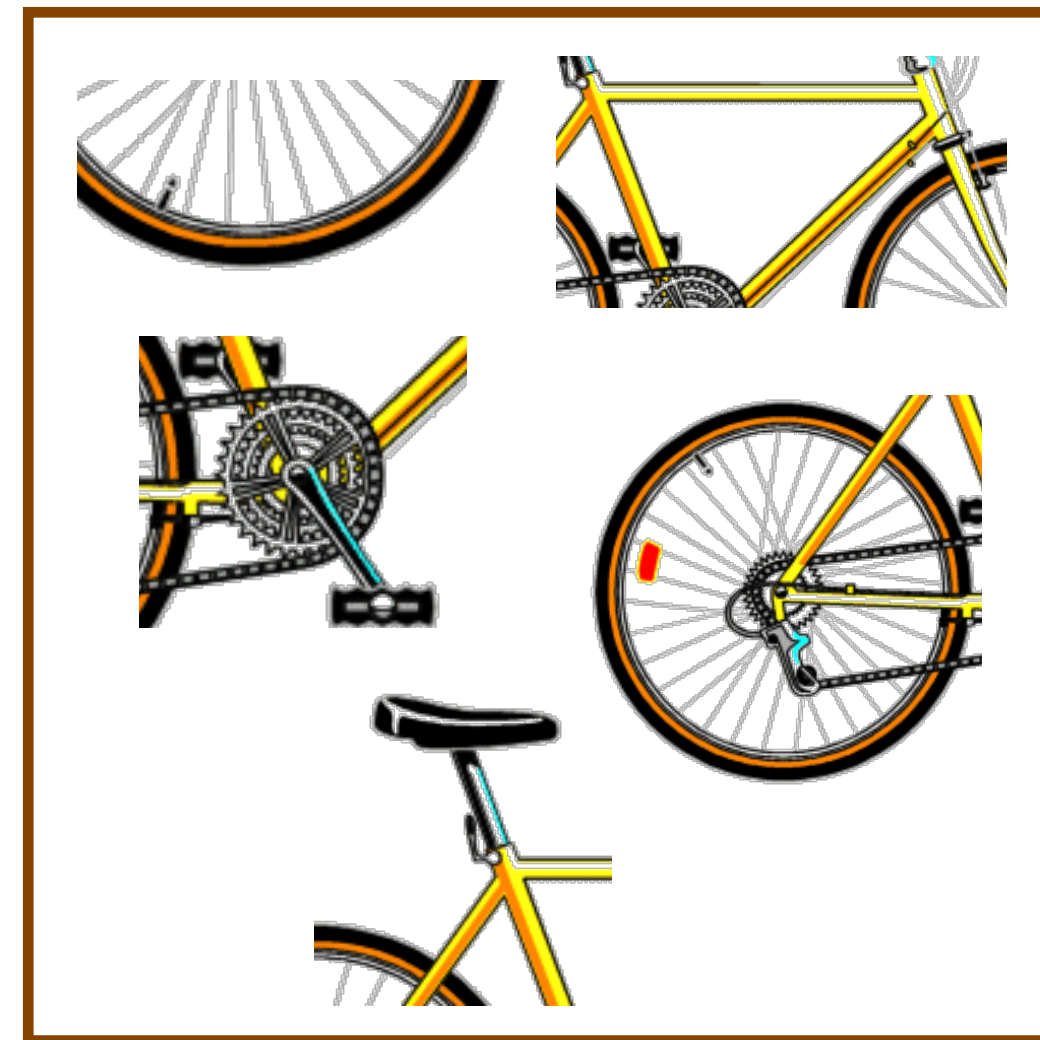
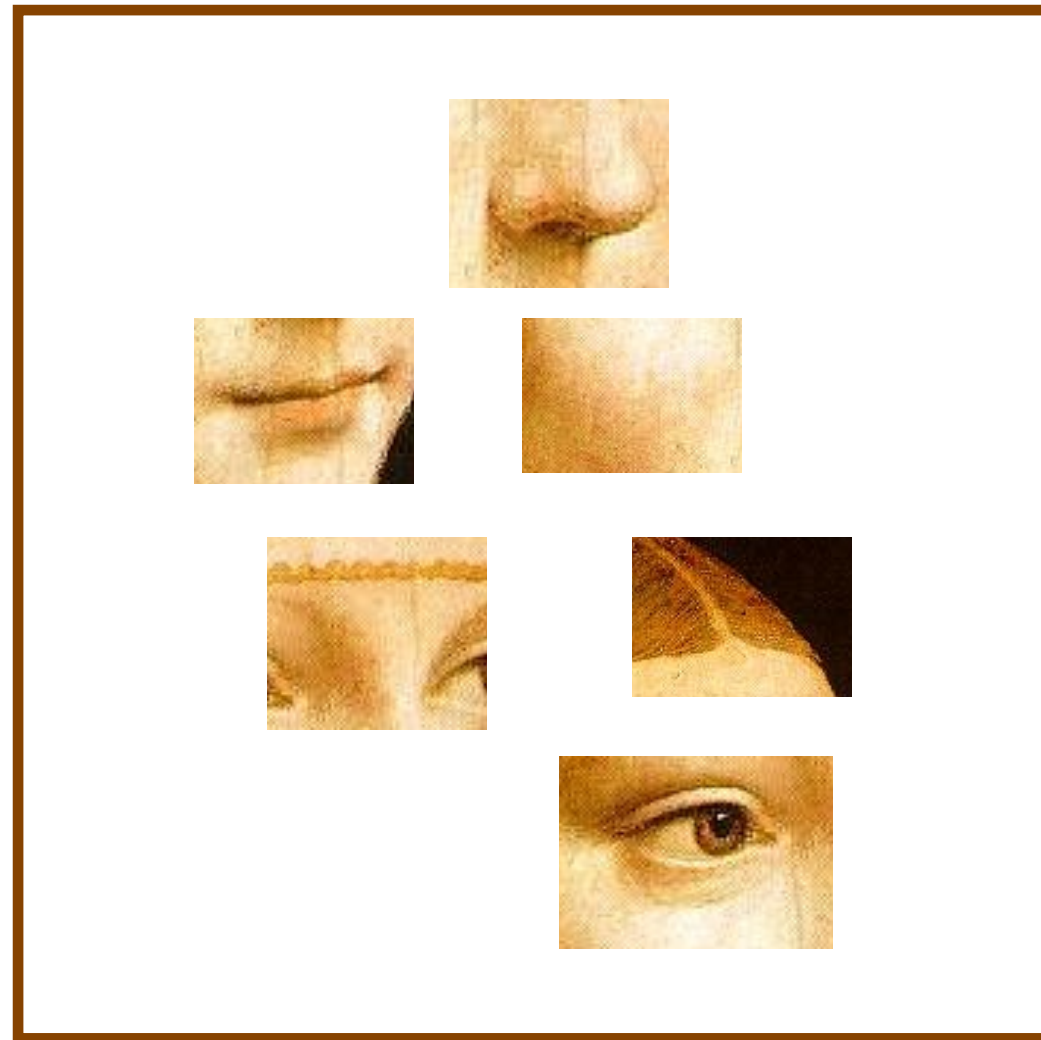
build Bags-of-Words (BOW) vectors
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Classify:

Train and test data using BOWs

1. Dictionary Learning: Learn Visual Words using Clustering

1. Extract features (e.g., SIFT) from images



1. Dictionary Learning: Learn Visual Words using Clustering

2. Learn visual dictionary (e.g., K-means clustering)



What **Features** Should We Extract?

- Regular grid

Vogel & Schiele, 2003

Fei-Fei & Perona, 2005

- Interest point detector

Csurka et al. 2004

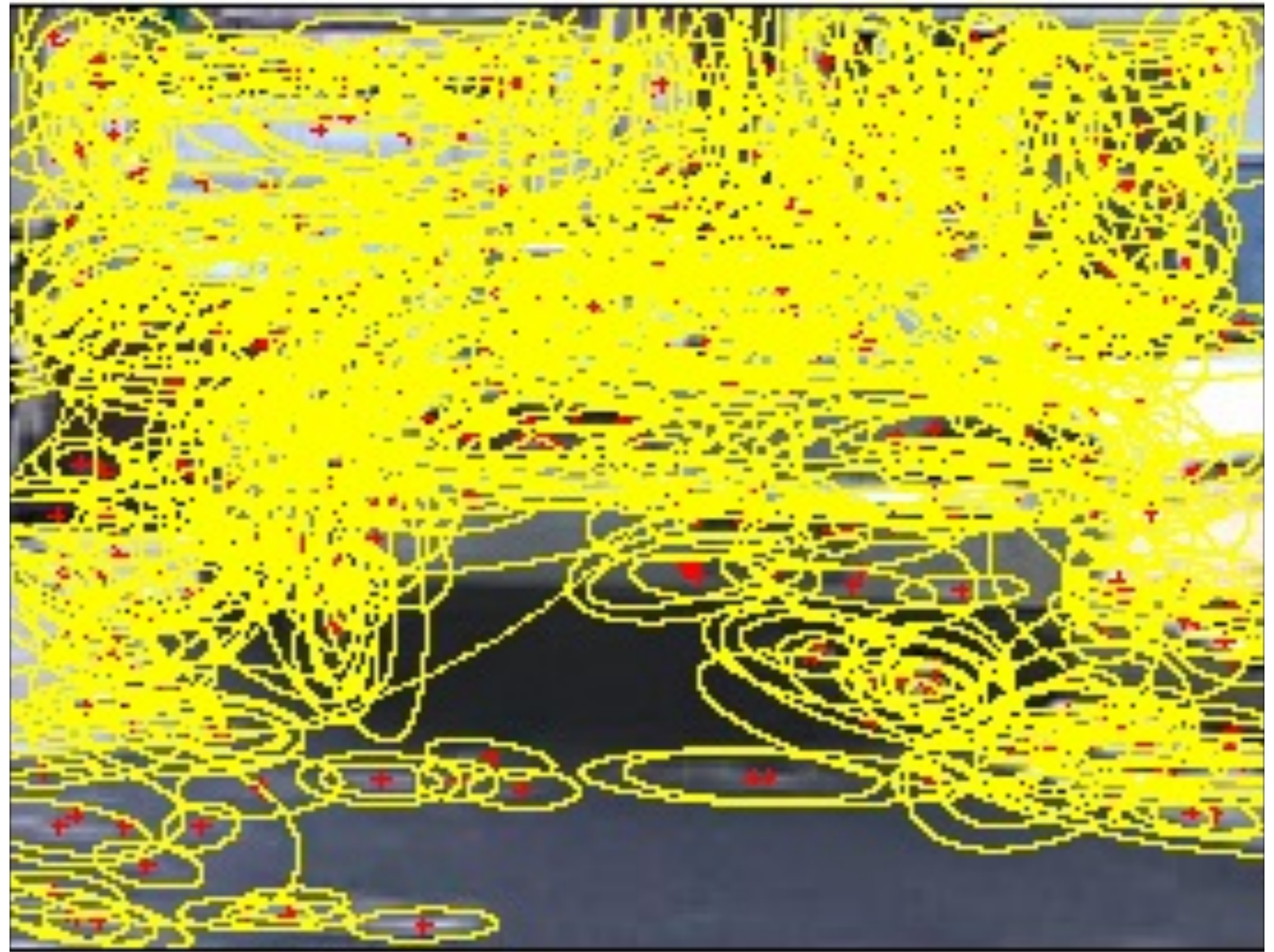
Fei-Fei & Perona, 2005

Sivic et al. 2005

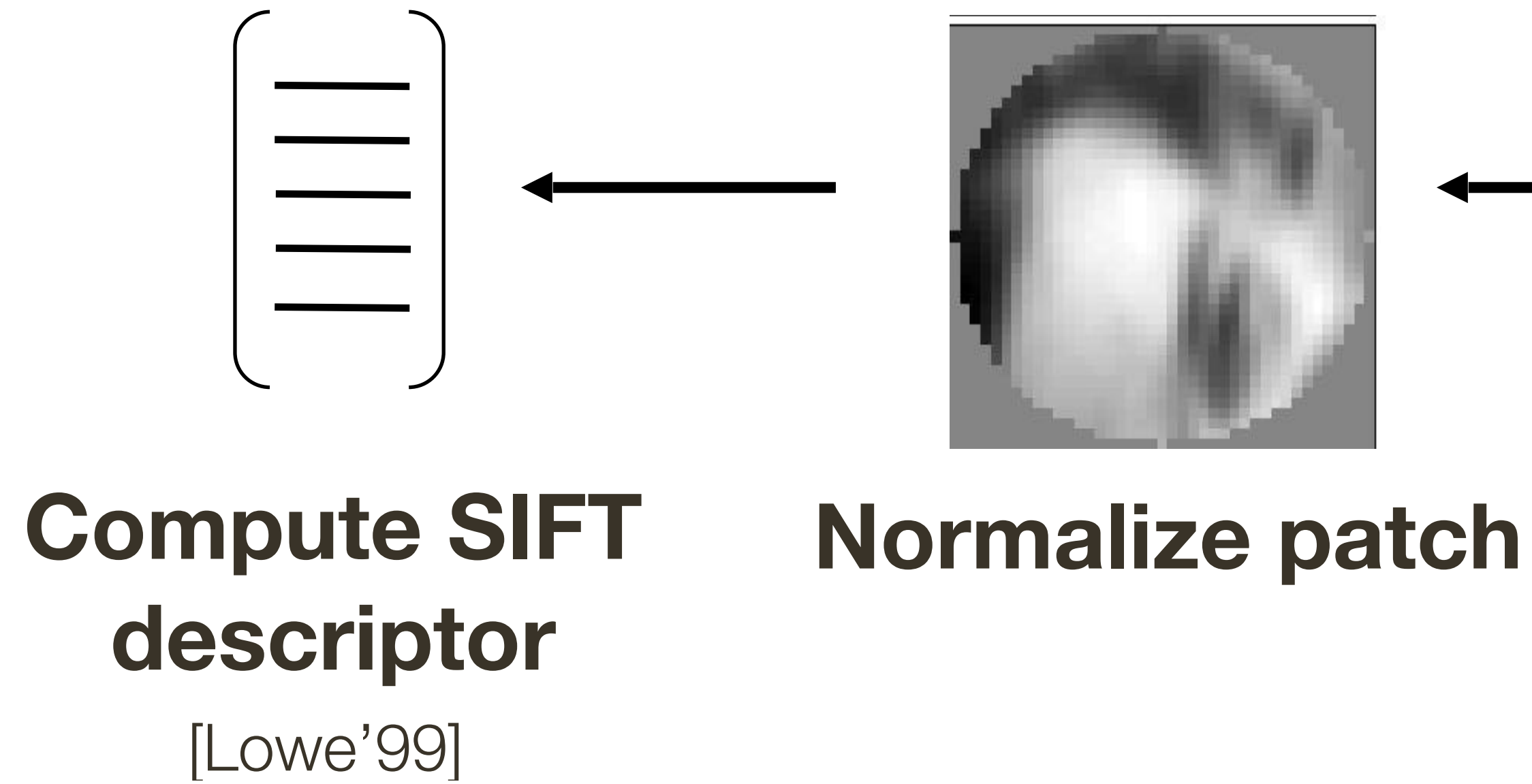
- Other methods

Random sampling (Vidal-Naquet & Ullman, 2002)

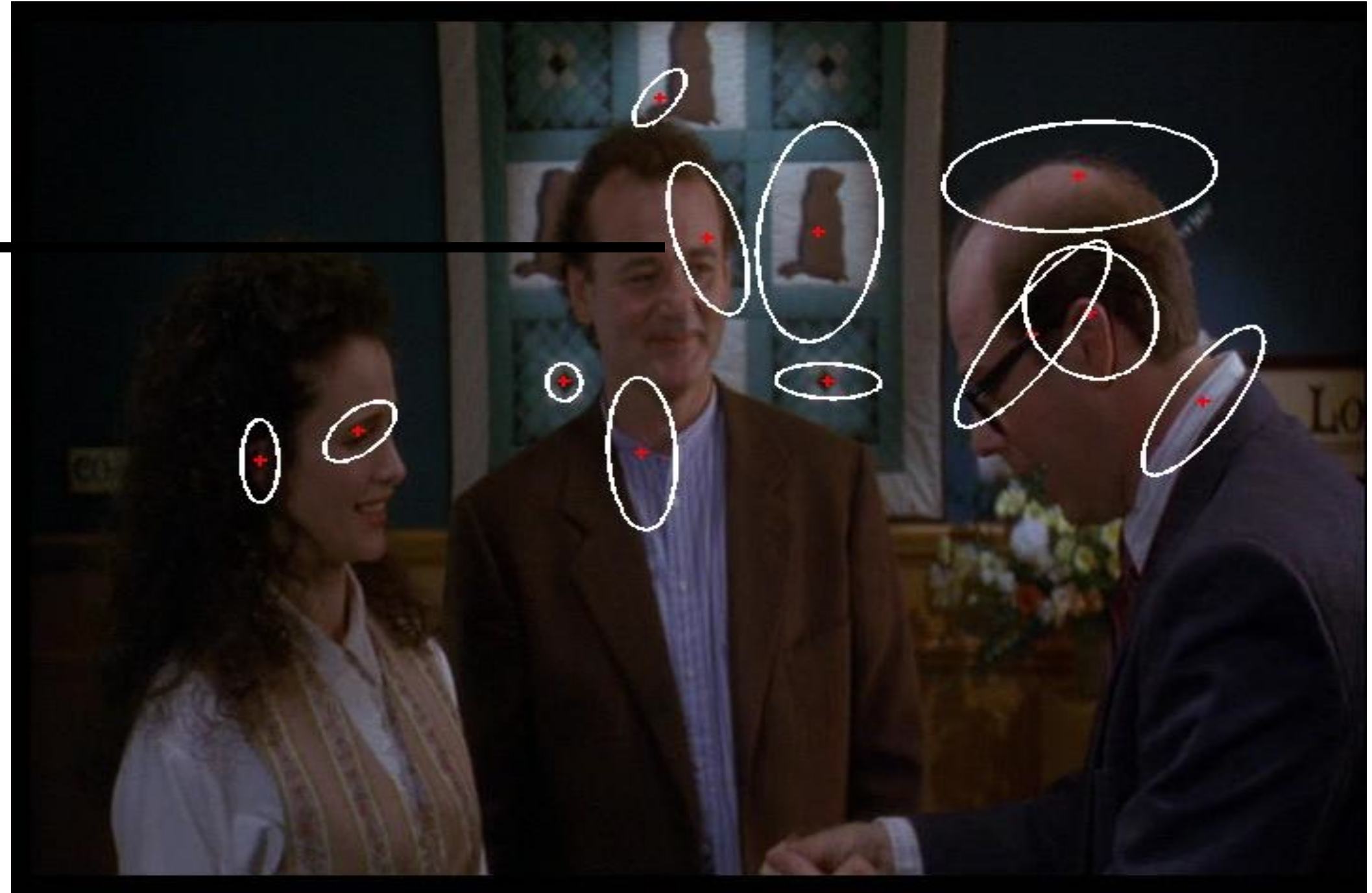
Segmentation-based patches (Barnard et al. 2003)



Extracting **SIFT** Patches



Normalize patch



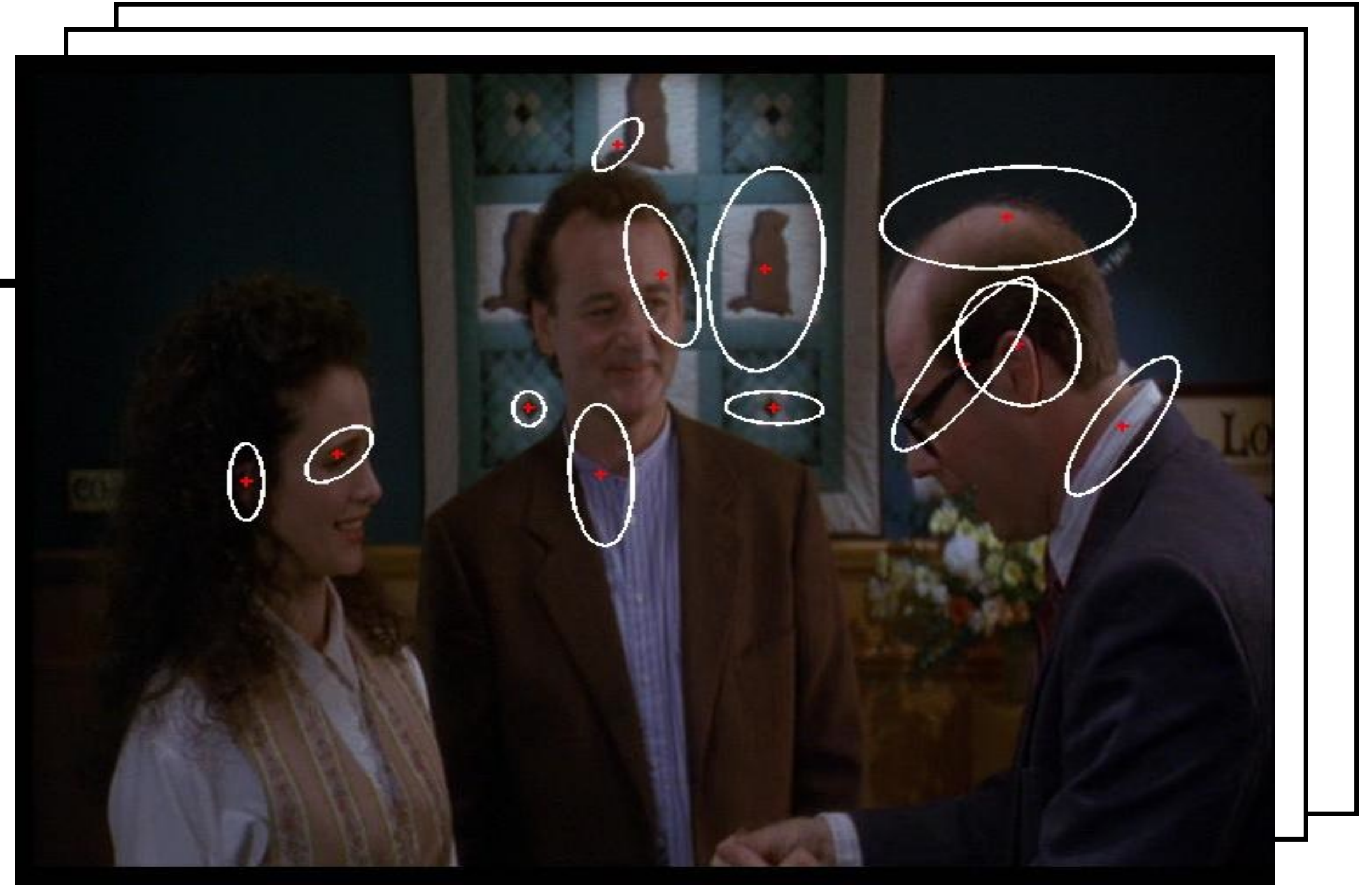
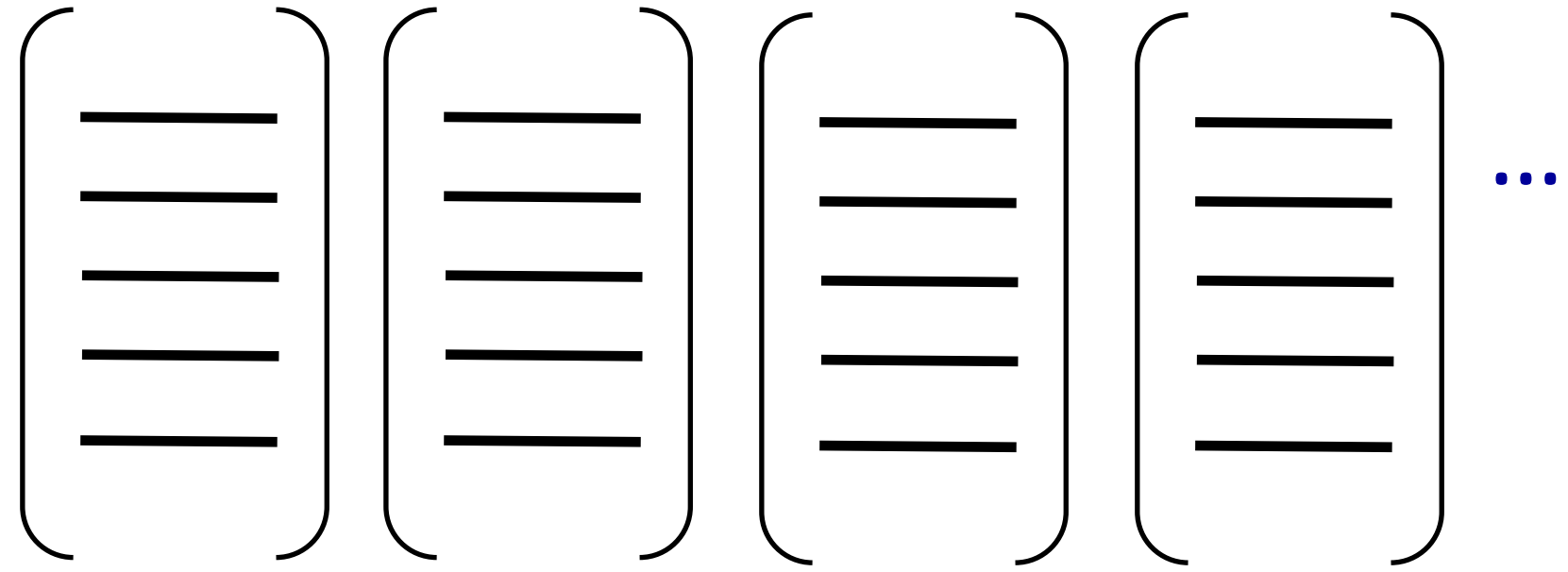
Detect patches

[Mikojaczyk and Schmid '02]

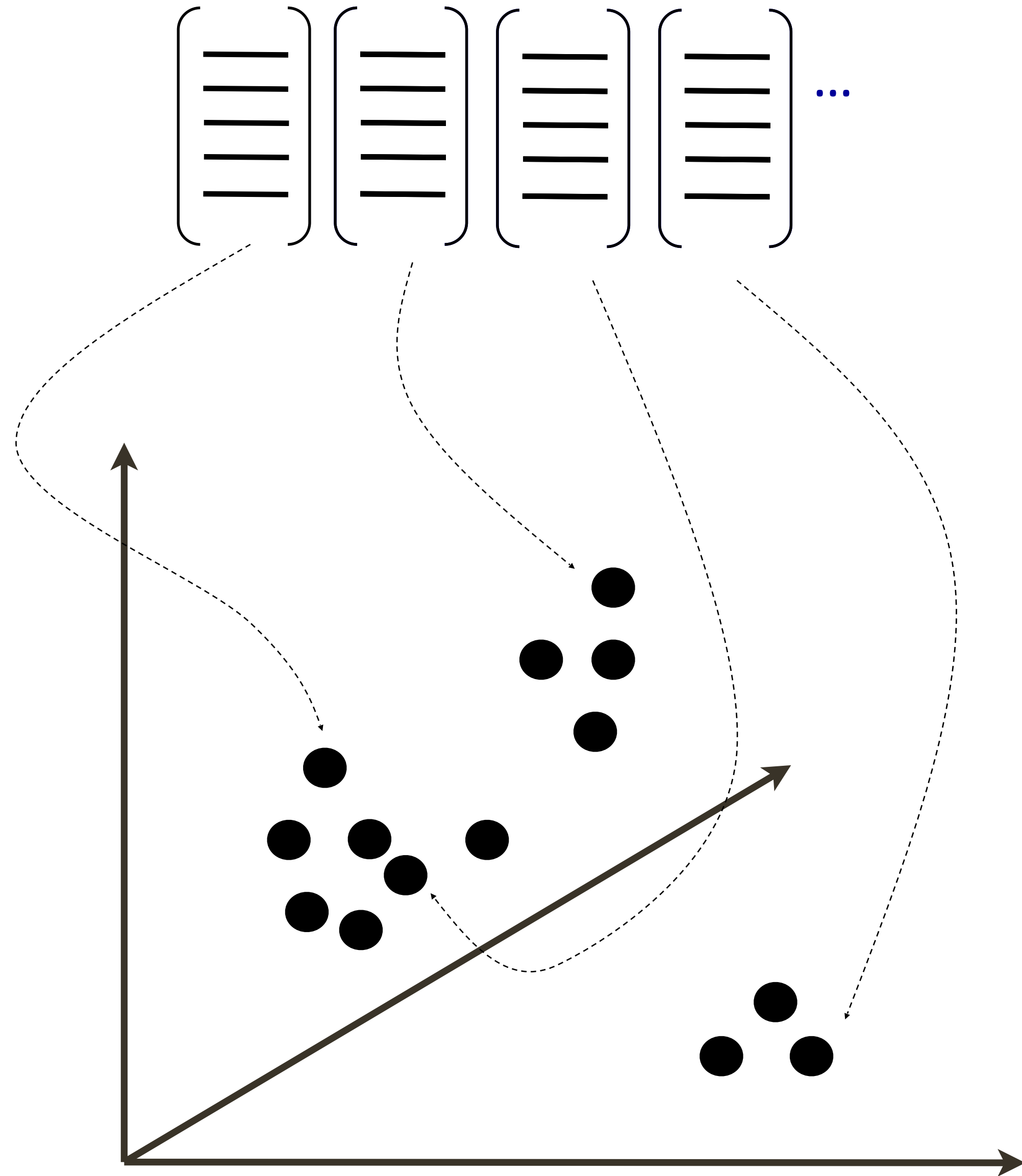
[Mata, Chum, Urban & Pajdla, '02]

[Sivic & Zisserman, '03]

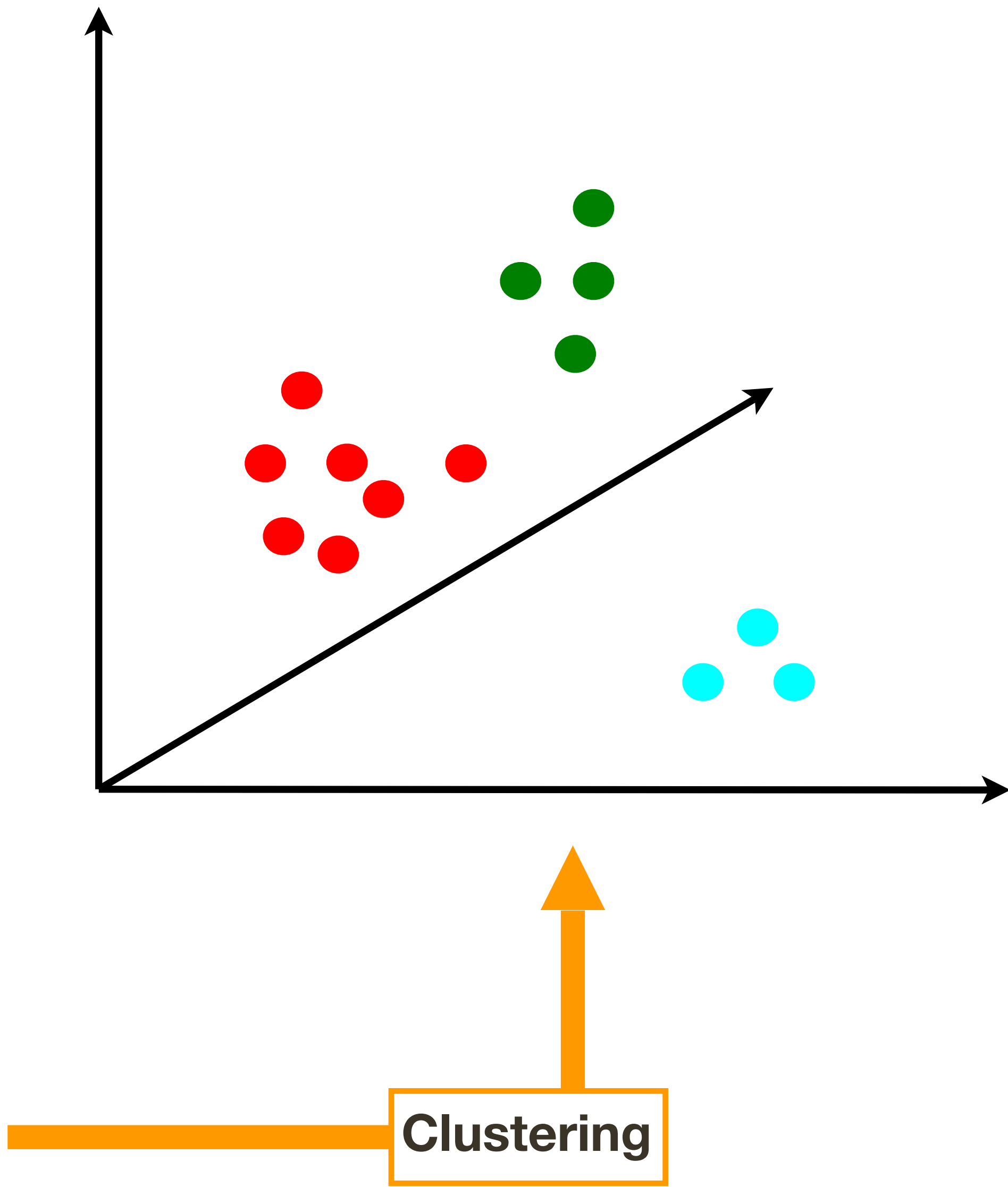
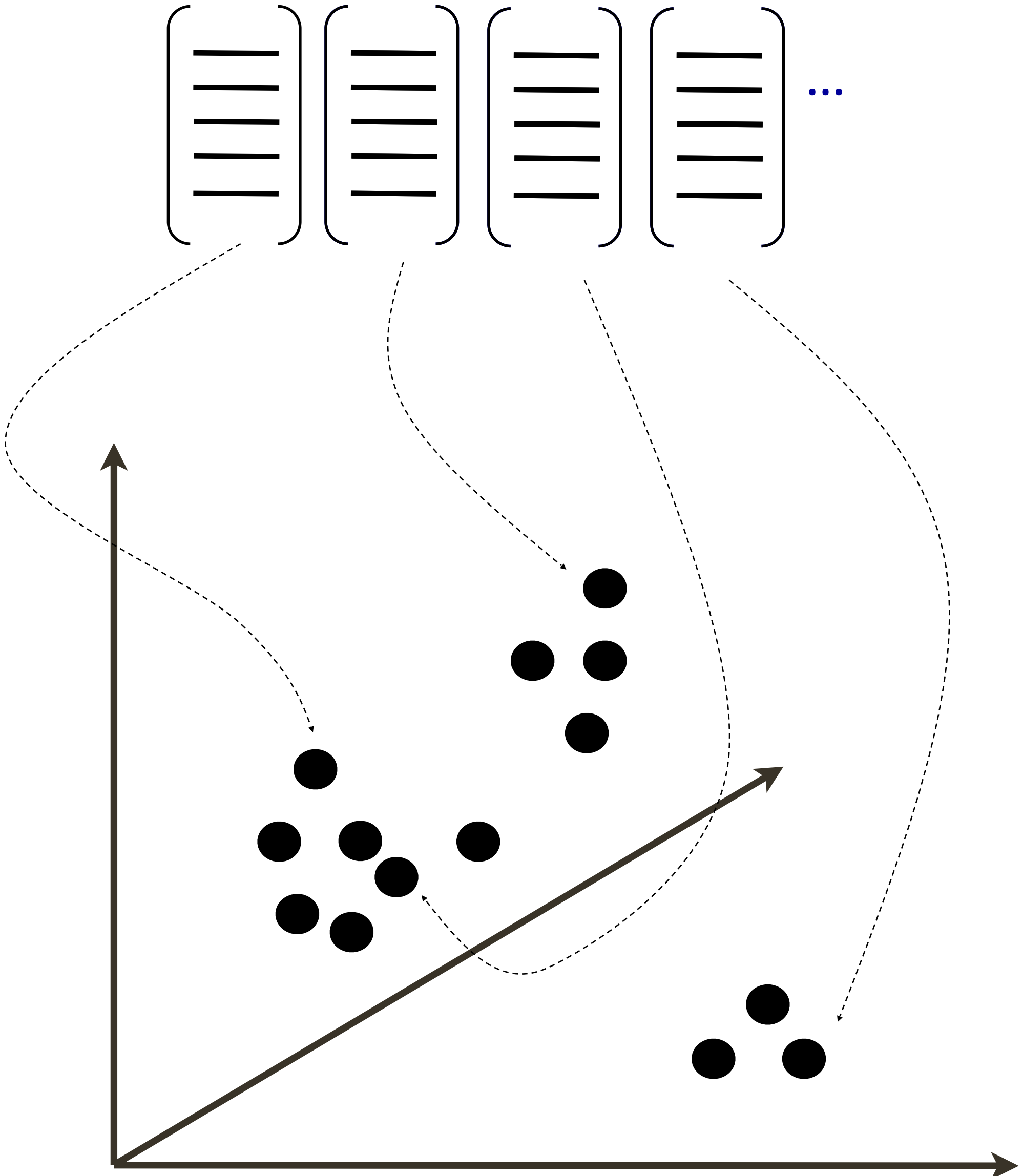
Extracting **SIFT** Patches



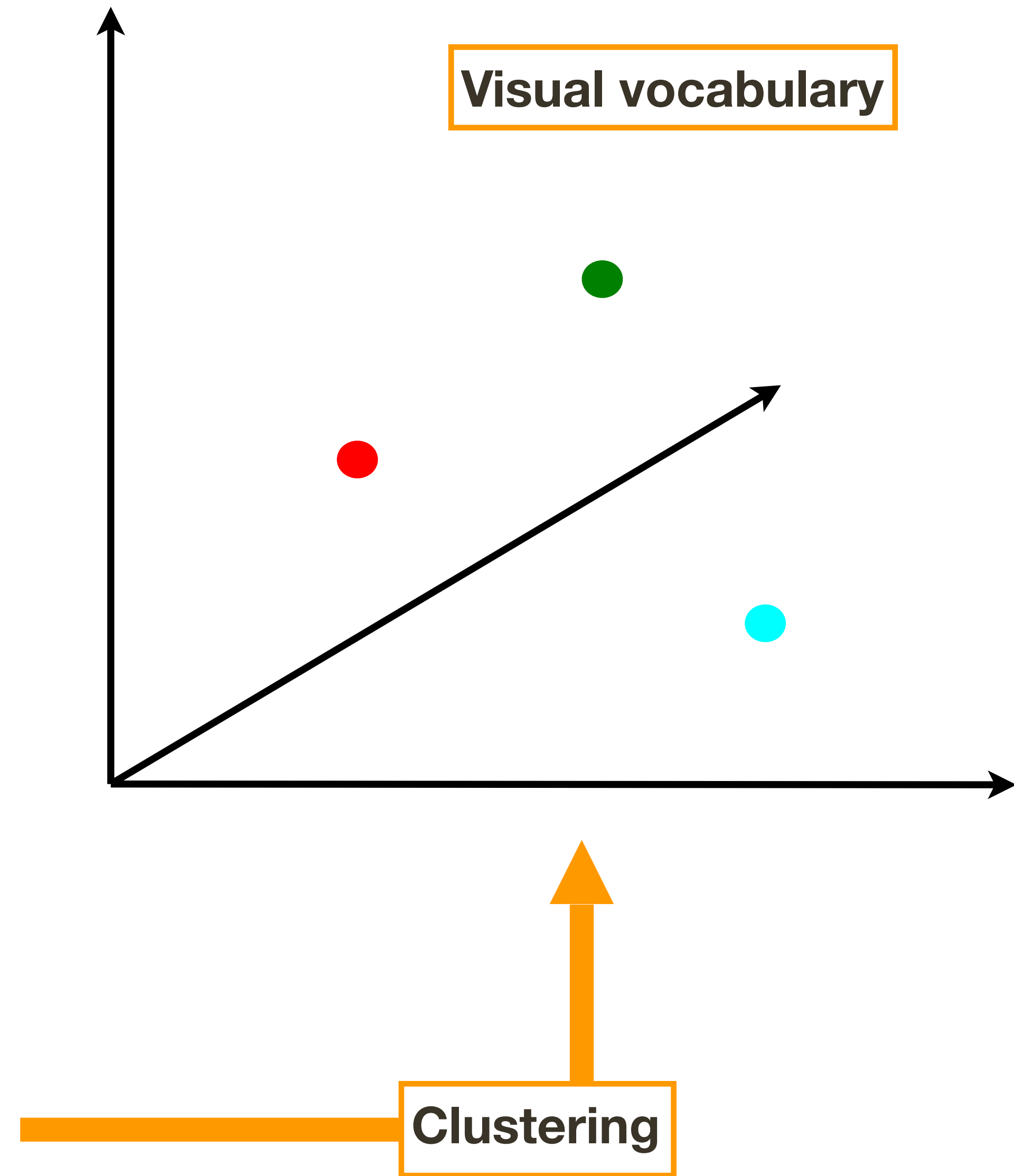
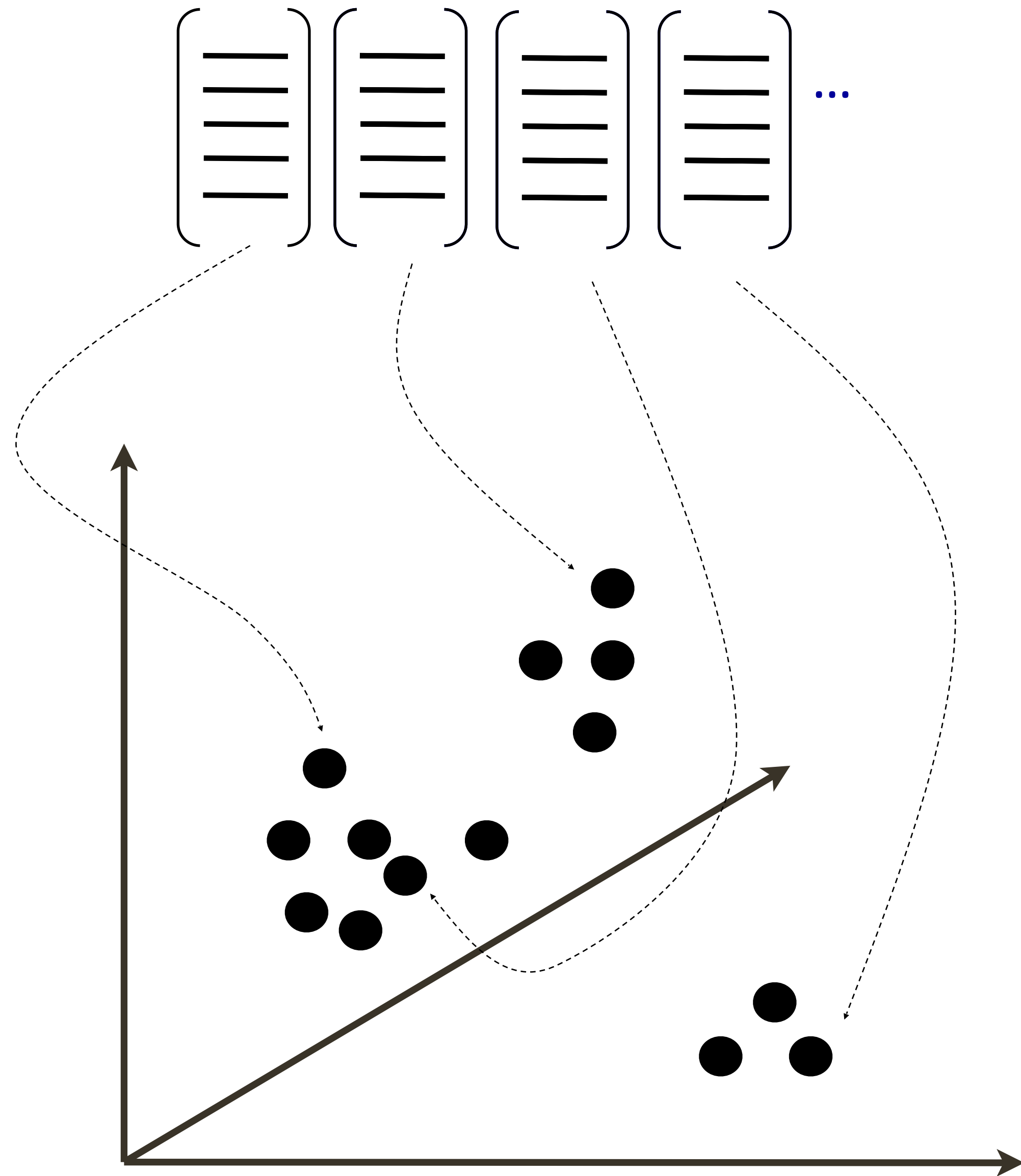
Creating Dictionary



Creating Dictionary



Creating Dictionary



K-means clustering

K-Means Clustering

Assume we **know** how many clusters there are in the data - denote by K

Each **cluster** is represented by a **cluster center**, or mean

Our objective is to **minimize the representation error** (or quantization error) in letting each data point be represented by some cluster center

Minimize

$$\sum_{i \in \text{clusters}} \left\{ \sum_{j \in i^{\text{th}} \text{ cluster}} \|x_j - \mu_i\|^2 \right\}$$

K-Means Clustering

K-means clustering alternates between two steps:

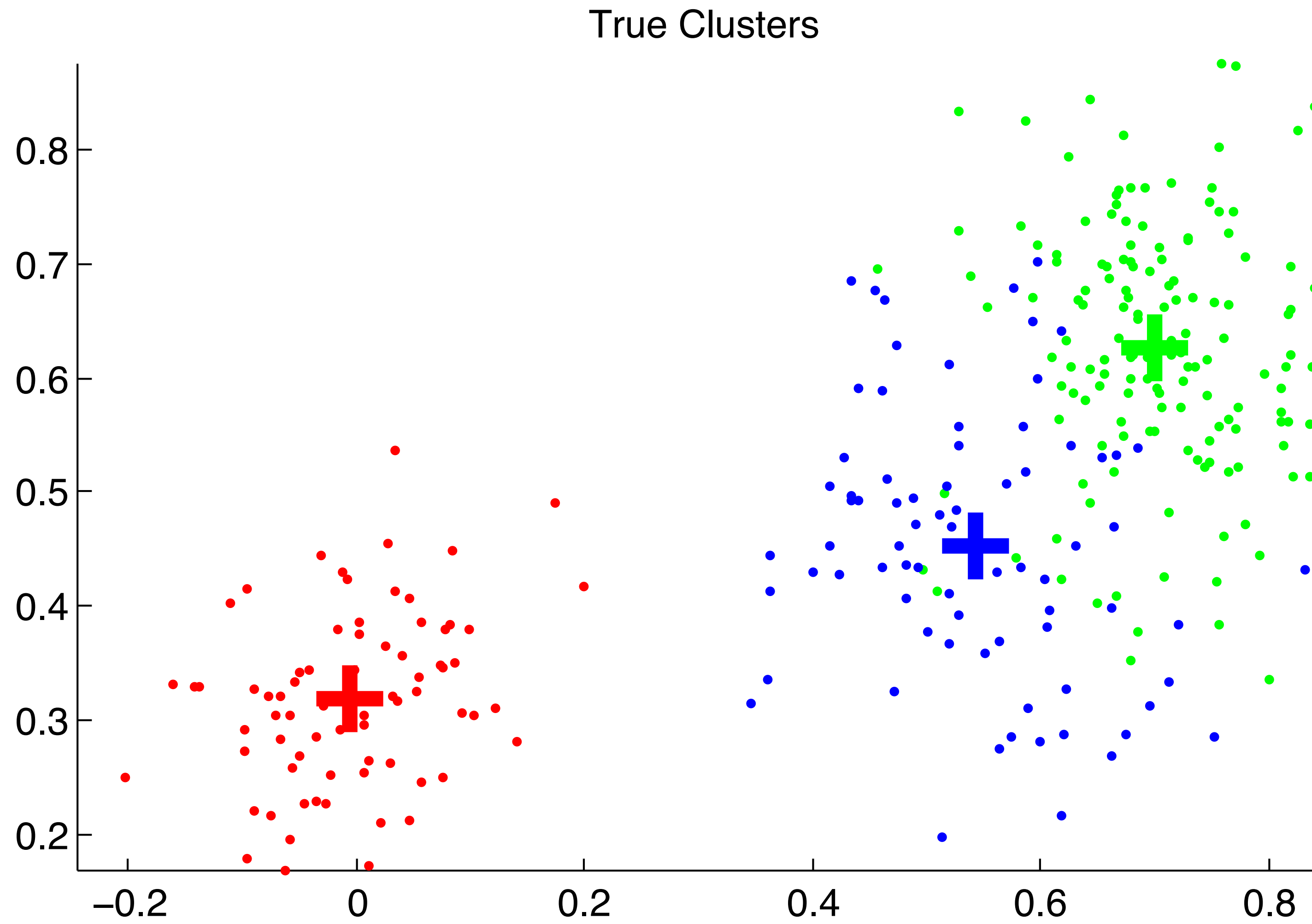
- 1.** Assume the cluster centers are known (fixed). Assign each point to the closest cluster center.
- 2.** Assume the assignment of points to clusters is known (fixed). Compute the best center for each cluster, as the mean of the points assigned to the cluster.

The algorithm is initialized by choosing K random cluster centers

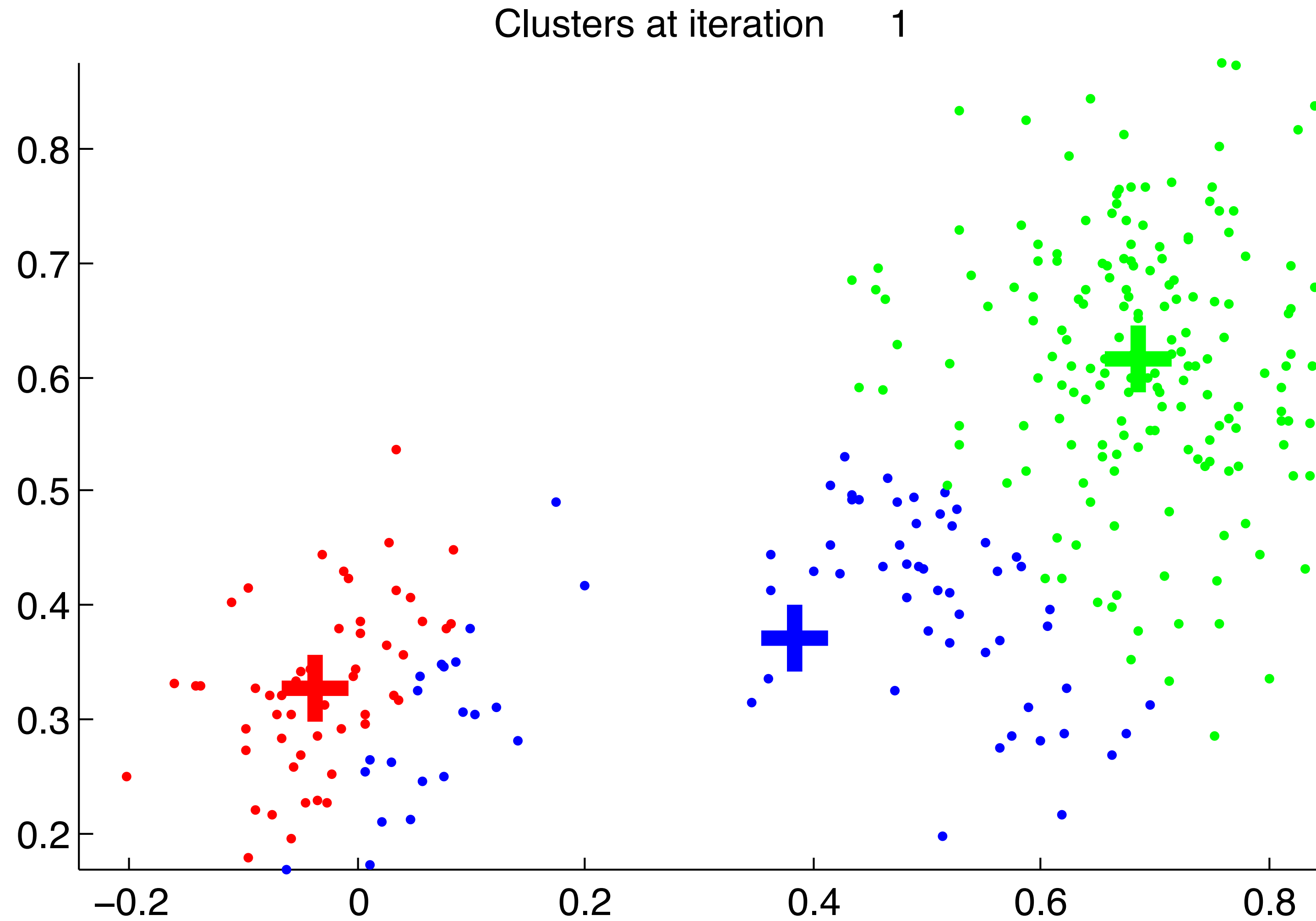
K-means converges to a local minimum of the objective function

— Results are initialization dependent

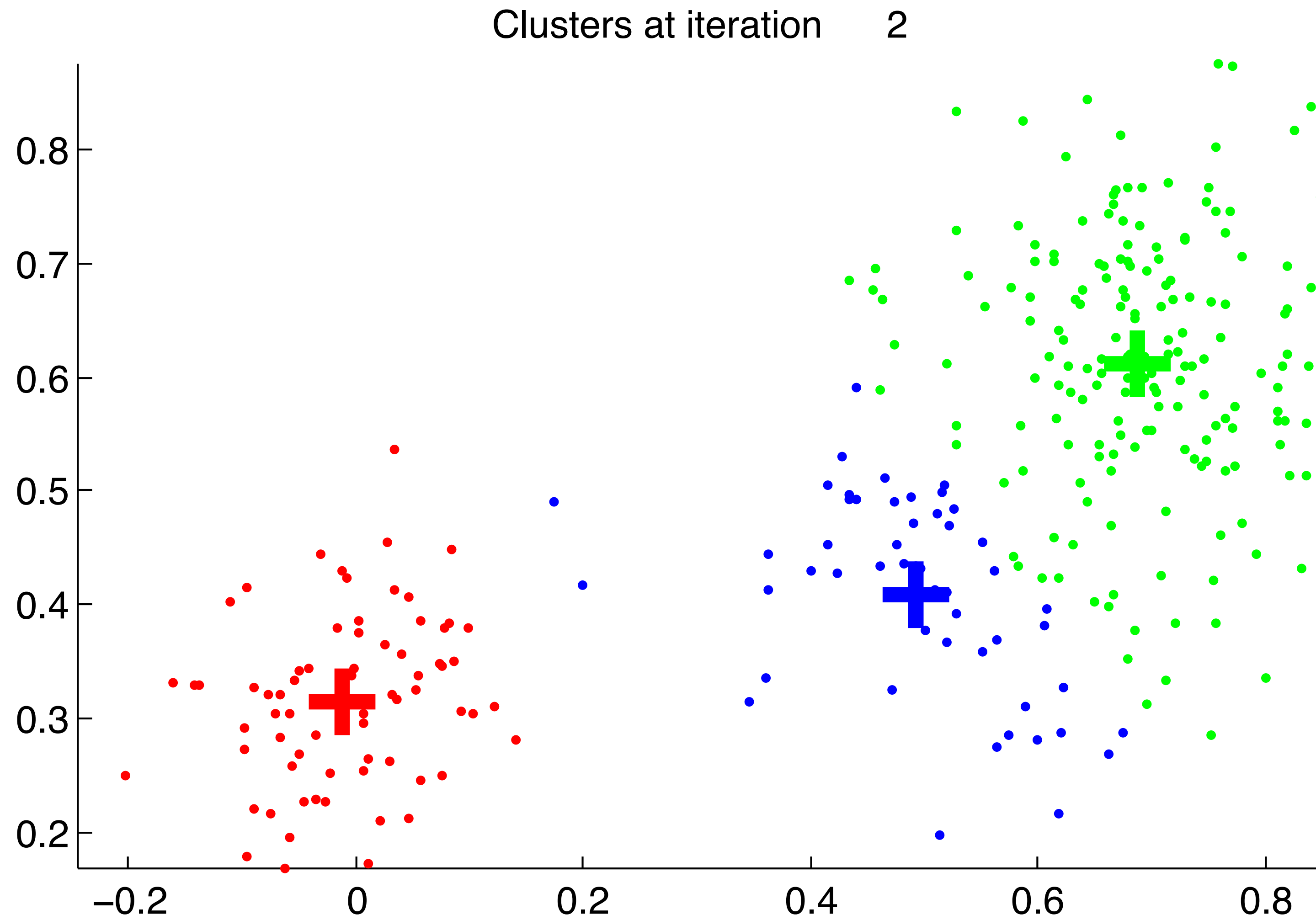
Example 1: K-Means Clustering



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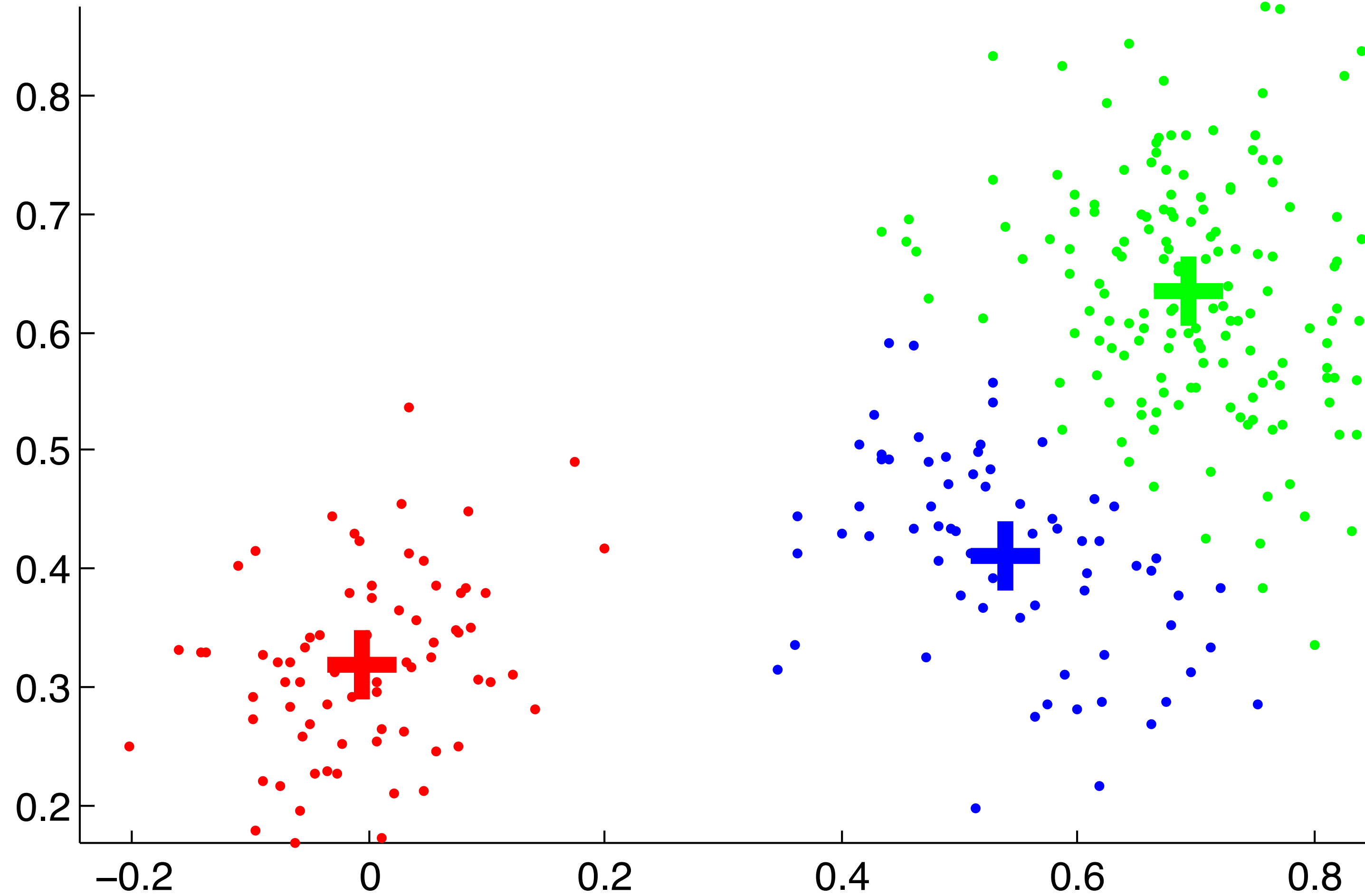


Example 1: K-Means Clustering

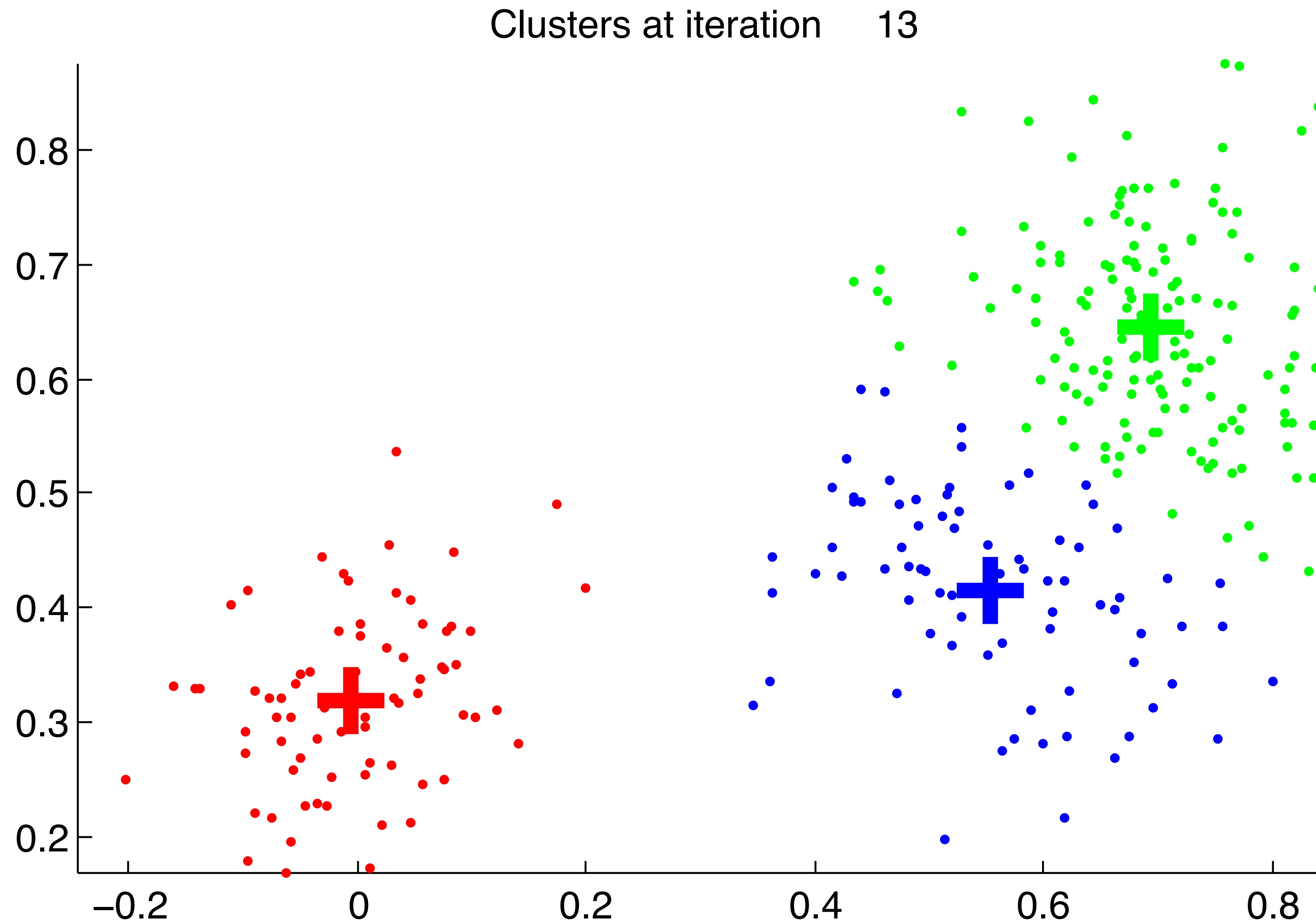


Example 1: K-Means Clustering

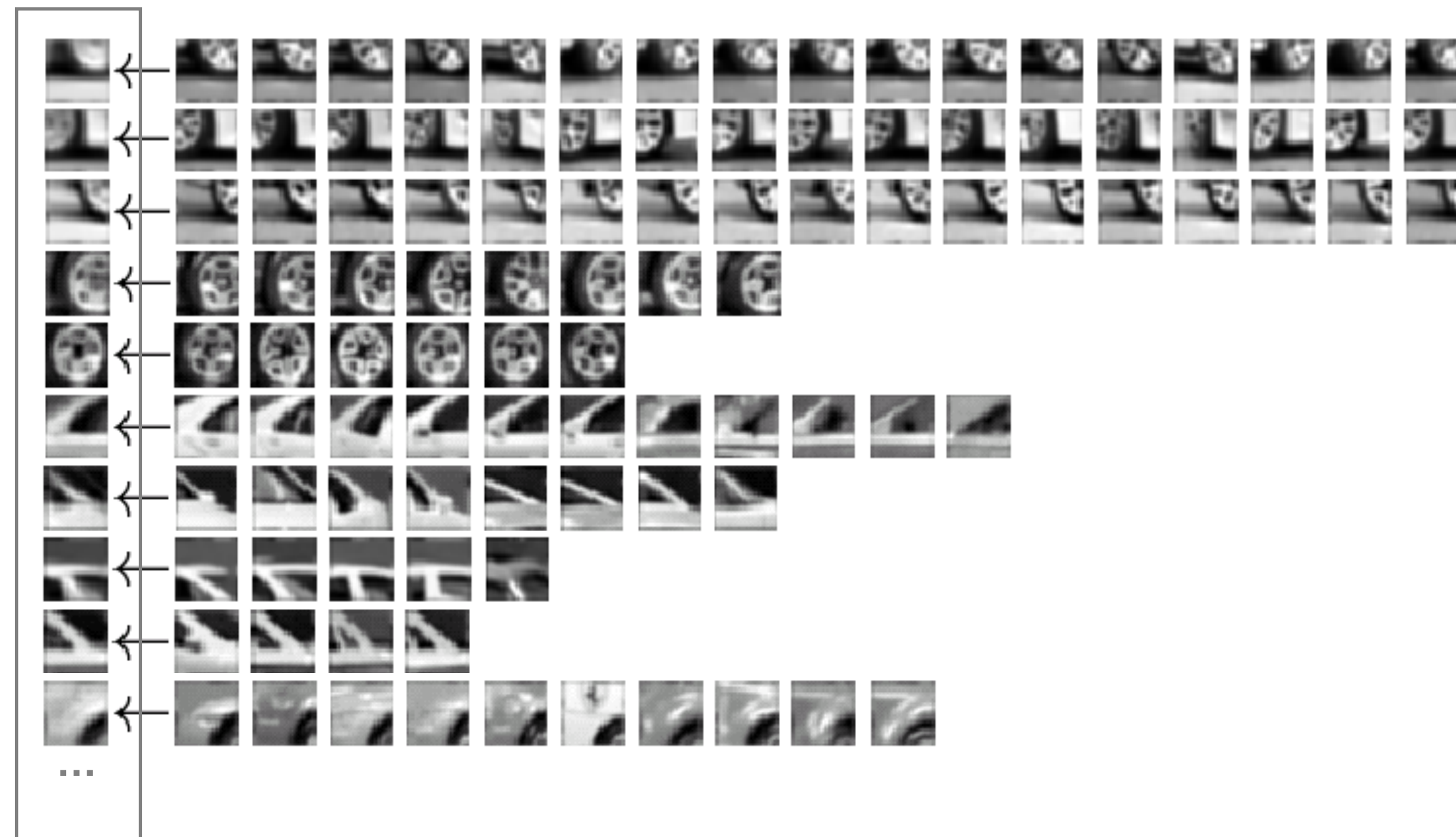
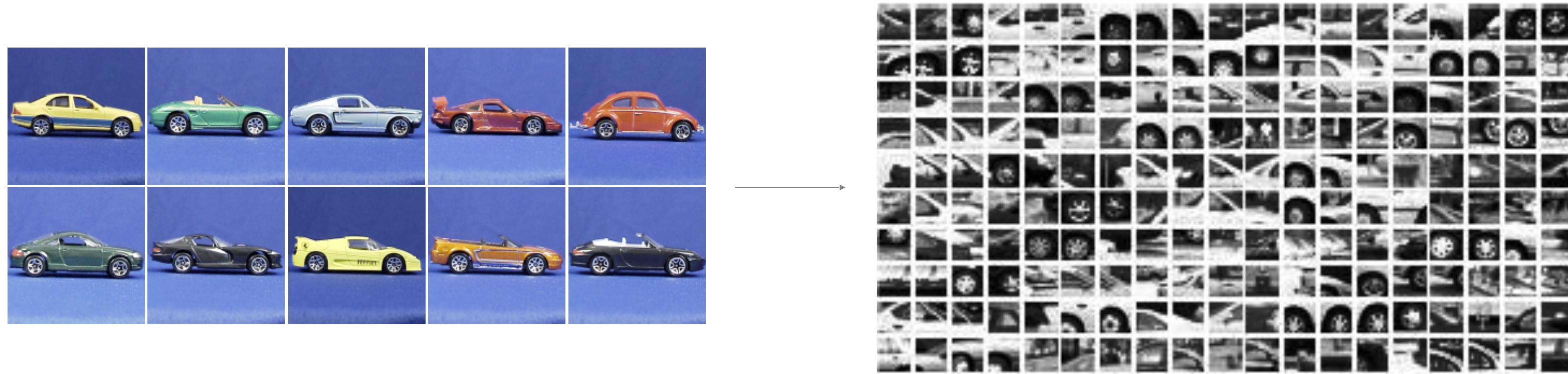
Clusters at iteration 3



Example 1: K-Means Clustering

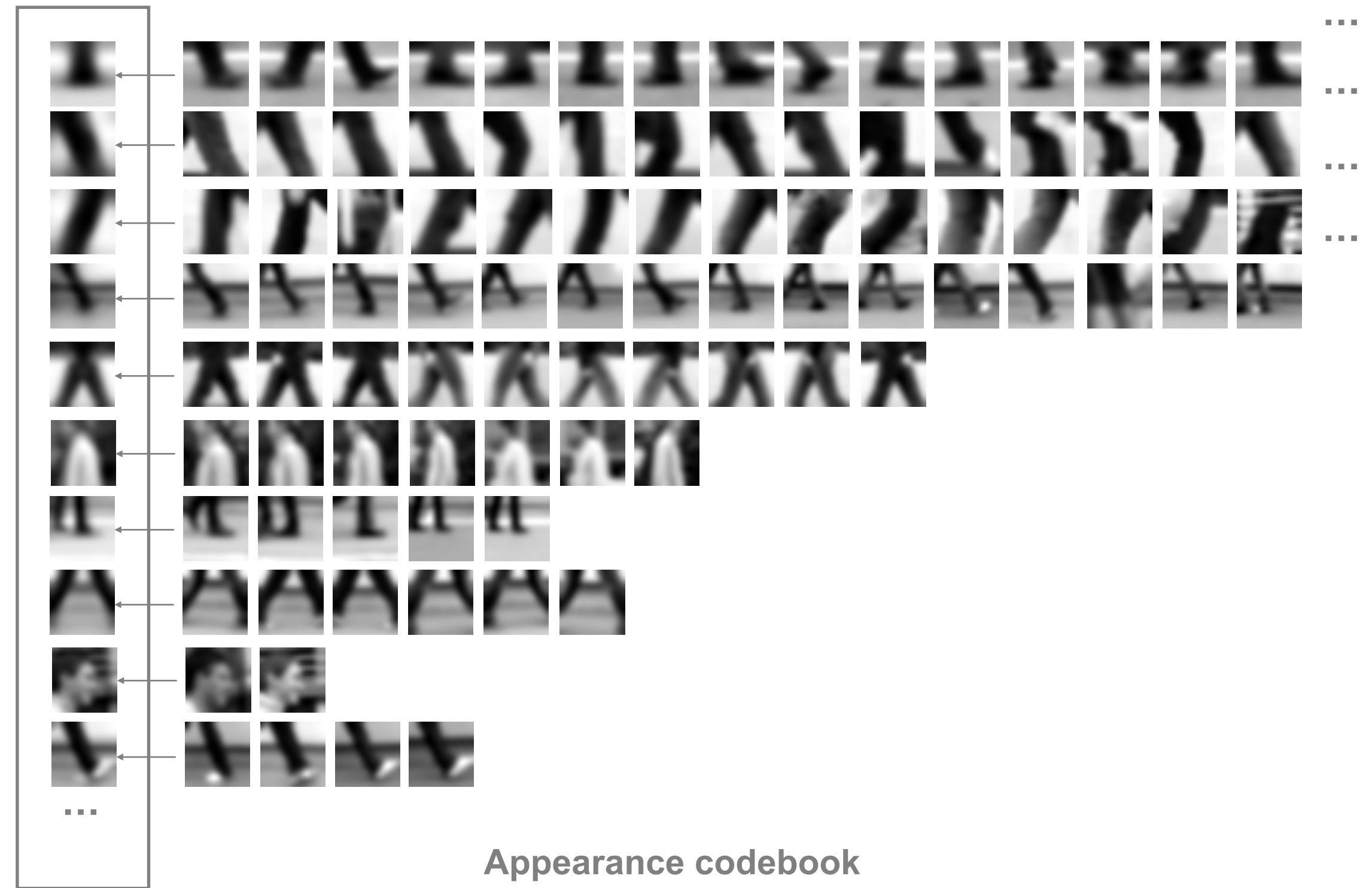


Example **Visual Dictionary**



Source: B. Leibe

Example **Visual Dictionary**



Appearance codebook

Source: B. Leibe

Standard **Bag-of-Words** Pipeline (for image classification)

Dictionary Learning:

Learn Visual Words using clustering

Encode:

build Bags-of-Words (BOW) vectors
for each image

Classify:

Train and test data using BOWs

2. **Encode:** build Bag-of-Words (BOW) vectors for each image

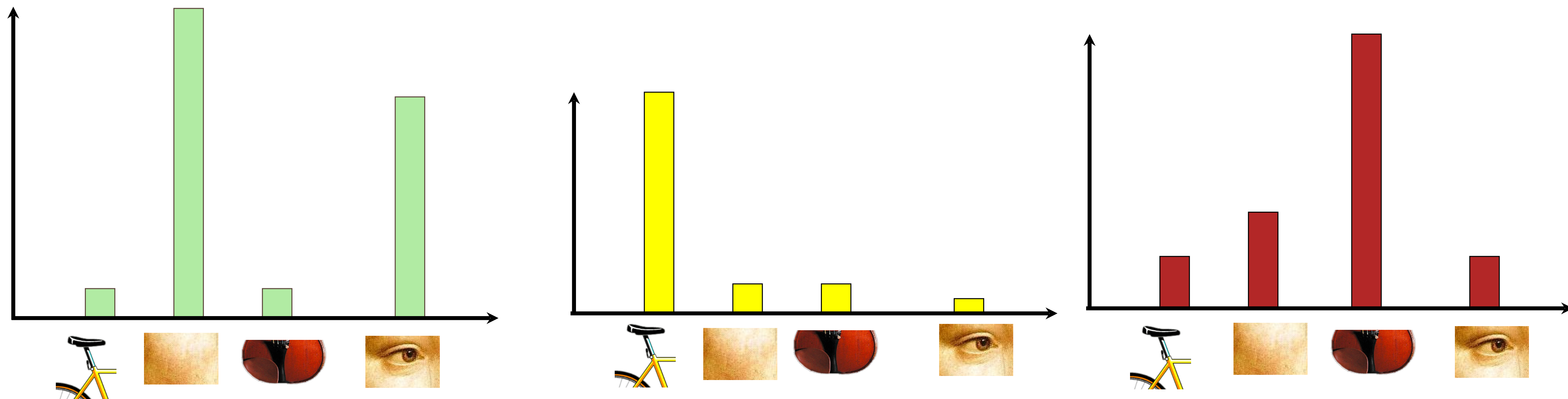


1. **Quantization:** image features gets associated to a visual word (nearest cluster center)

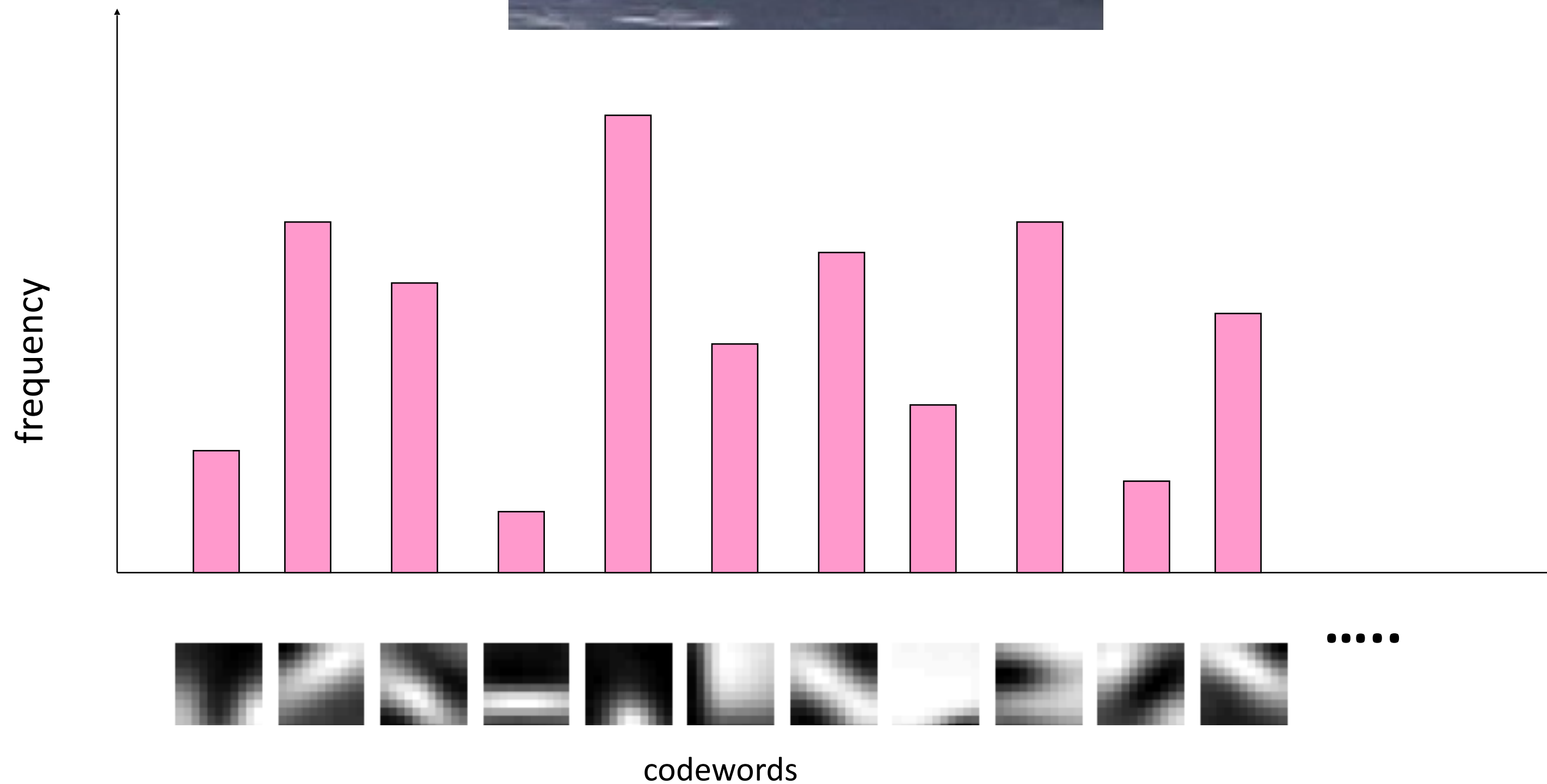


2. Encode: build Bag-of-Words (BOW) vectors for each image

2. **Histogram**: count the number of visual word occurrences



2. Encode: build Bag-of-Words (BOW) vectors for each image



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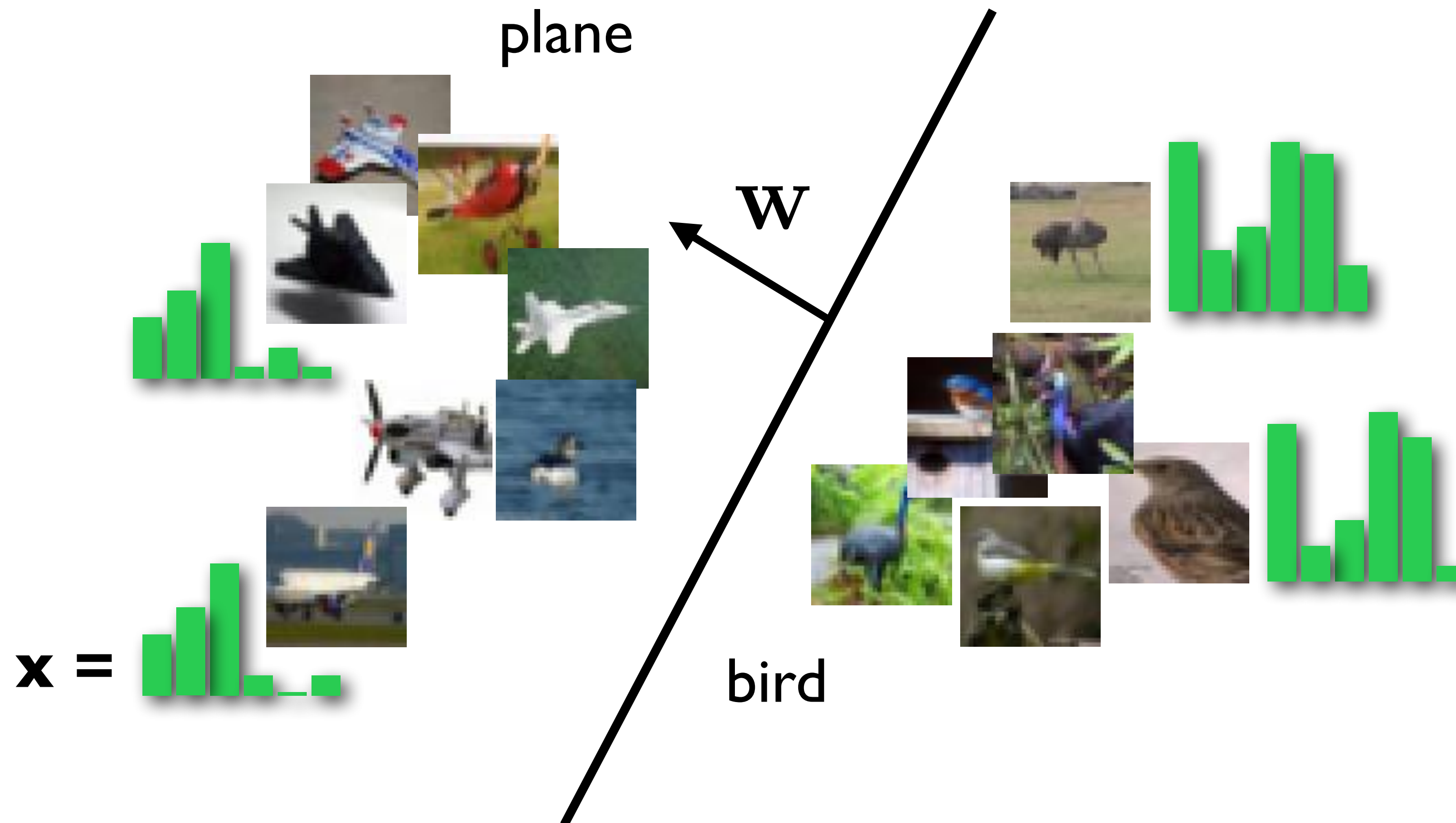
Classify:

Train and test data using BOWs

Classify Visual Word Histograms

e.g., bird vs plane classifier as linear classifier in space of histograms

Histograms of visual word frequencies = vector \mathbf{x} , linear classifier \mathbf{w}



Bayes Rule (Review and Definitions)

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

$$P(c|x) = \frac{P(x|c)p(c)}{P(x)}$$

posterior probability

Bayes Rule (Review and Definitions)

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

The diagram illustrates the Bayes Rule equation with color-coded components and labels:

- class-conditional probability (a.k.a. likelihood)**: $P(x|c)$ (blue box)
- prior probability**: $p(c)$ (green box)
- posterior probability**: $P(c|x)$ (purple box)
- unconditional probability (a.k.a. marginal likelihood)**: $P(x)$ (cyan box)

$$P(c|x) = \frac{P(x|c)p(c)}{P(x)}$$

Bayes Rule (Review and Definitions)

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

Simple case:

- binary classification; i.e., $c \in \{1, 2\}$
- features are 1D; i.e., $x \in \mathbb{R}$

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Classify \mathbf{x} as

1 if $p(1|\mathbf{x}) > p(2|\mathbf{x})$

2 if $p(1|\mathbf{x}) < p(2|\mathbf{x})$

Bayes Rule (Review and Definitions)

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

Simple case:

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General case:

- multi-class; i.e., $c \in \{1, \dots, 1000\}$
- features are high-dimensional; i.e., $x \in \mathbb{R}^{2,000+}$

Example: Discrete Bayes Classifier

Assume we have two classes: $c_1 = \mathbf{male}$ $c_2 = \mathbf{female}$

We have a person whose gender we don't know, whose name is *drew*

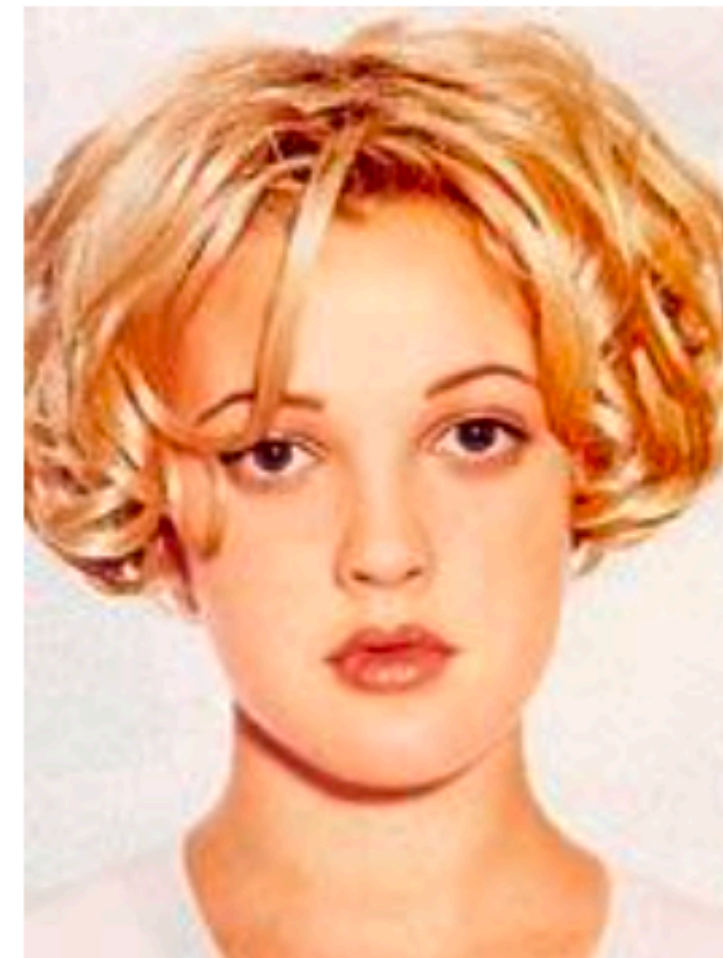
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Drew Carey



Drew Barrymore

Example: Discrete Bayes Classifier

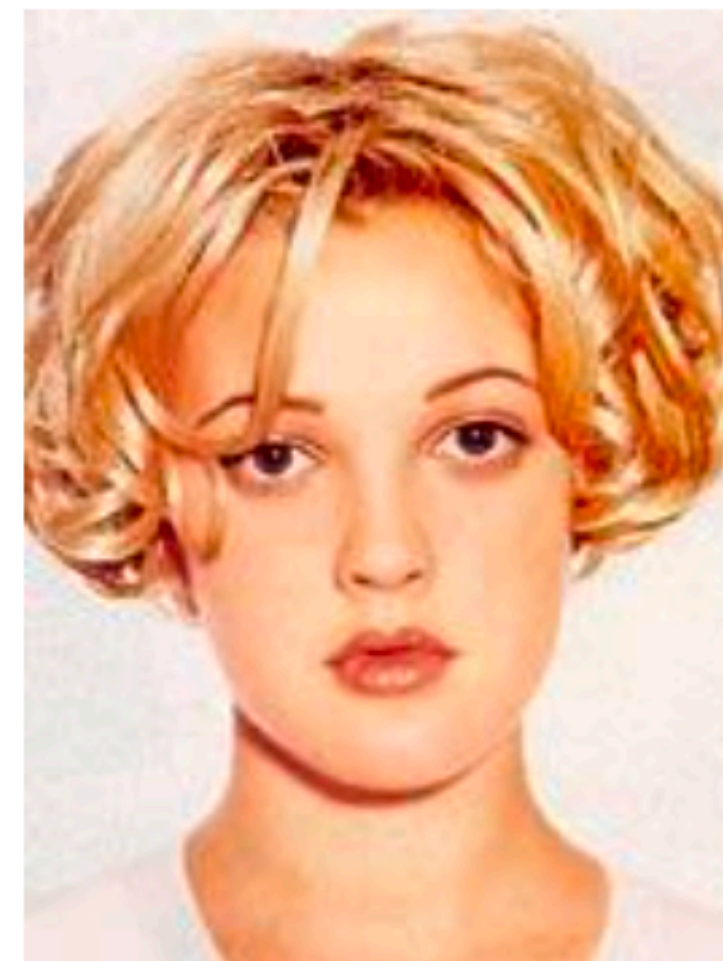
Assume we have two classes: $c_1 = \mathbf{male}$ $c_2 = \mathbf{female}$

We have a person whose gender we don't know, whose name is *drew*

Classifying *drew* as being male or female is equivalent to asking is it more probable that *drew* is male or female, i.e. which is greater $p(\mathbf{male}|drew)$
 $p(\mathbf{female}|drew)$



Drew Carey



Drew Barrymore

Example: Discrete Bayes Classifier

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Classifying *drew* as being male or female is equivalent to asking is it more probable that *drew* is male or female, i.e. which is greater $p(\mathbf{male}|drew)$
 $p(\mathbf{female}|drew)$

$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$$

Example: Discrete Bayes Classifier

Name	Gender
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male

$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$$

Example: Discrete Bayes Classifier

$$p(\mathbf{male}) =$$

$$p(drew|\mathbf{male}) =$$

$$p(drew) =$$

$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$$

Name	Gender
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male

Example: Discrete Bayes Classifier

$$p(\mathbf{male}) = \frac{3}{8}$$

$$p(drew|\mathbf{male}) =$$

$$p(drew) =$$

$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$$

Name	Gender
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male

Example: Discrete Bayes Classifier

$$p(\mathbf{male}) = \frac{3}{8}$$

$$p(drew|\mathbf{male}) = \frac{1}{3}$$

$$p(drew) =$$

$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$$

Name	Gender
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
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Example: Discrete Bayes Classifier

$$p(\mathbf{male}) = \frac{3}{8}$$

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$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$$

Name	Gender
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male

Example: Discrete Bayes Classifier

$$p(\mathbf{male}) = \frac{3}{8}$$

$$p(drew|\mathbf{male}) = \frac{1}{3}$$

~~$$p(drew) = \frac{3}{8}$$~~

$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{\cancel{p(drew)}} = 0.125$$

Name	Gender
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male

Example: Discrete Bayes Classifier

Name	Gender
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male

$$p(\mathbf{male}) = \frac{3}{8} \qquad p(\mathbf{female}) = \frac{5}{8}$$

$$p(drew|\mathbf{male}) = \frac{1}{3} \qquad p(drew|\mathbf{female}) = \frac{2}{5}$$

~~$$p(drew) = \frac{3}{8}$$~~

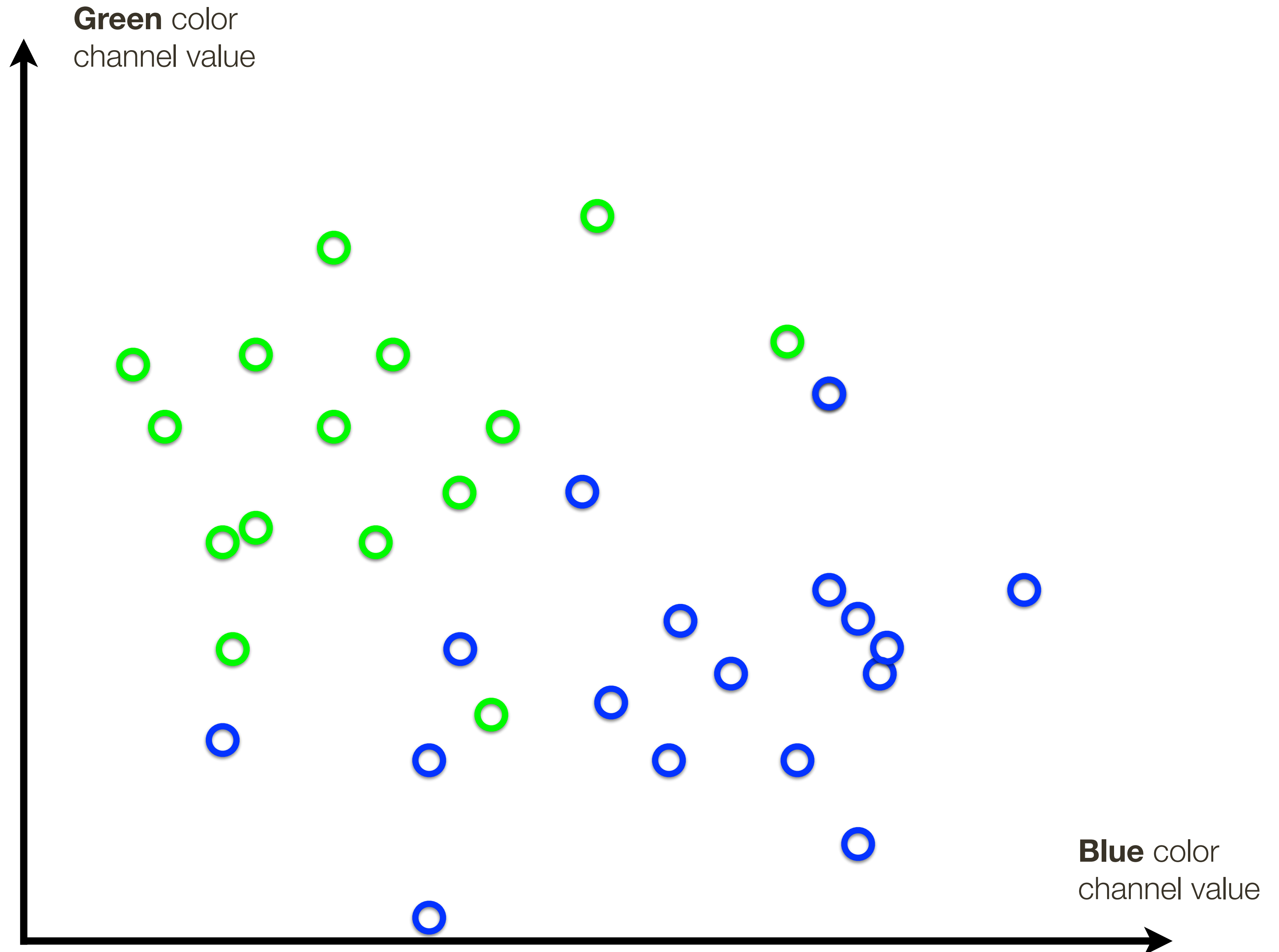
$$p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)} = 0.125$$

$$p(\mathbf{female}|drew) = \frac{p(drew|\mathbf{female})p(\mathbf{female})}{p(drew)} = 0.25$$

Example: 2D Bayes Classifier

Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

- 17 samples of grass
- 15 samples of sky

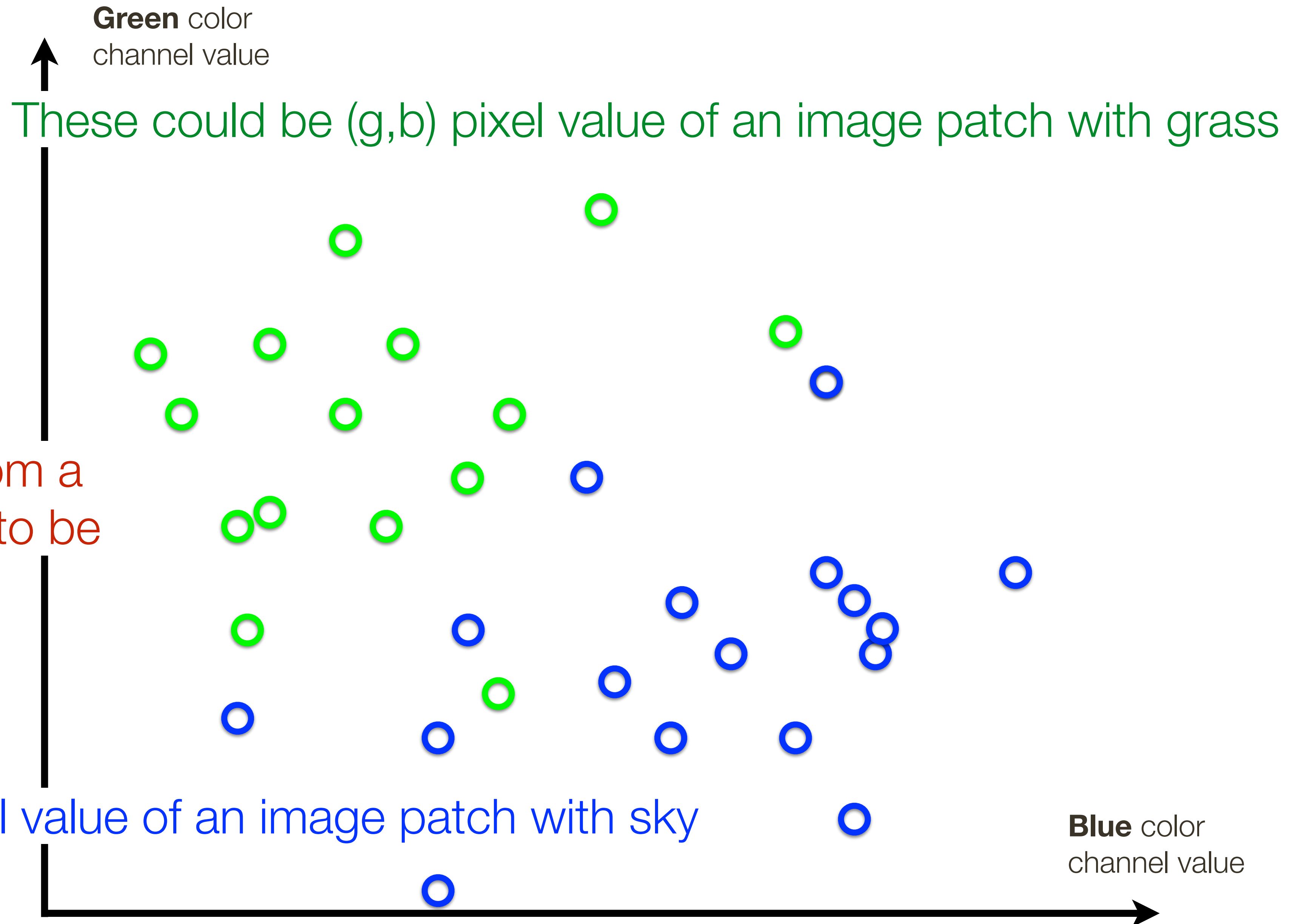


Example: 2D Bayes Classifier

Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

- 17 samples of grass
- 15 samples of sky

Given a (g,b) pixel value from a new patch is it more likely to be grass or sky?



Example: 2D Bayes Classifier

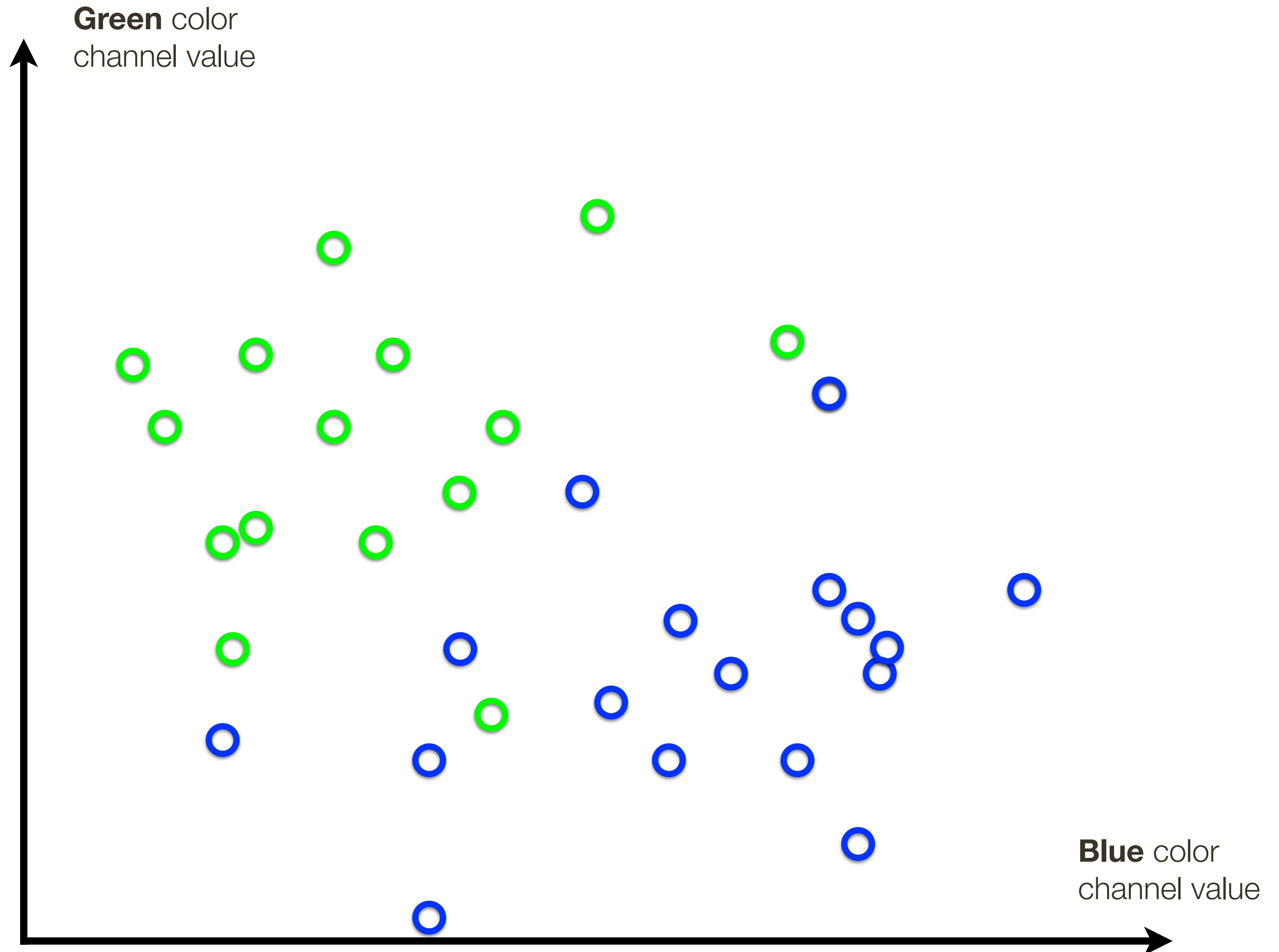
Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

○ 17 samples of grass

○ 15 samples of sky

$$p(\text{blue}) = \frac{17}{17 + 15}$$

$$p(\text{green}) = \frac{15}{17 + 15}$$



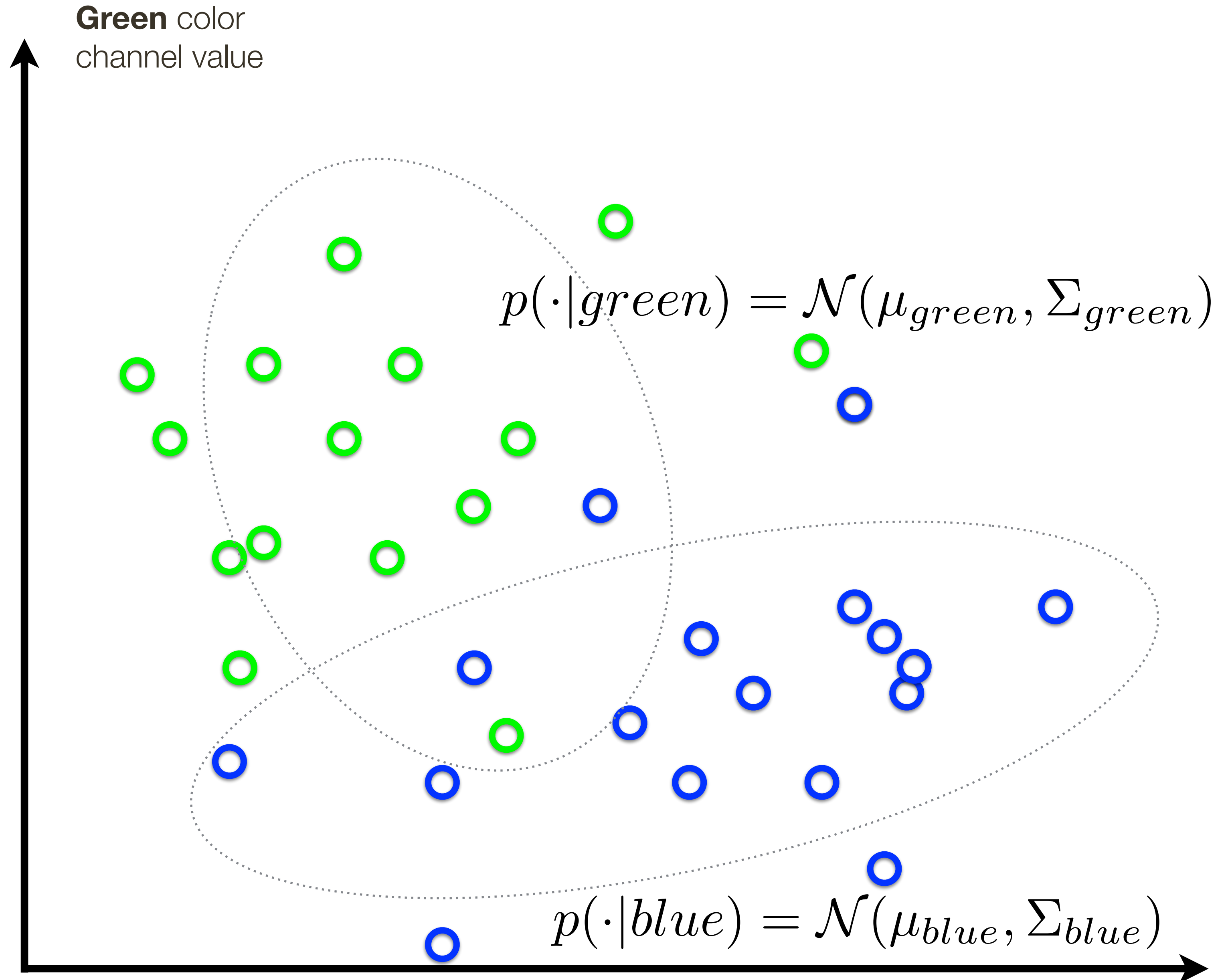
Example: 2D Bayes Classifier

Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

- 17 samples of grass
- 15 samples of sky

$$p(\text{blue}) = \frac{17}{17 + 15}$$

$$p(\text{green}) = \frac{15}{17 + 15}$$



Example: 2D Bayes Classifier

Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

$$p(\text{green}|\triangle) \propto \mathcal{N}(\triangle; \mu_{\text{green}}, \Sigma_{\text{green}})p(\text{green})$$

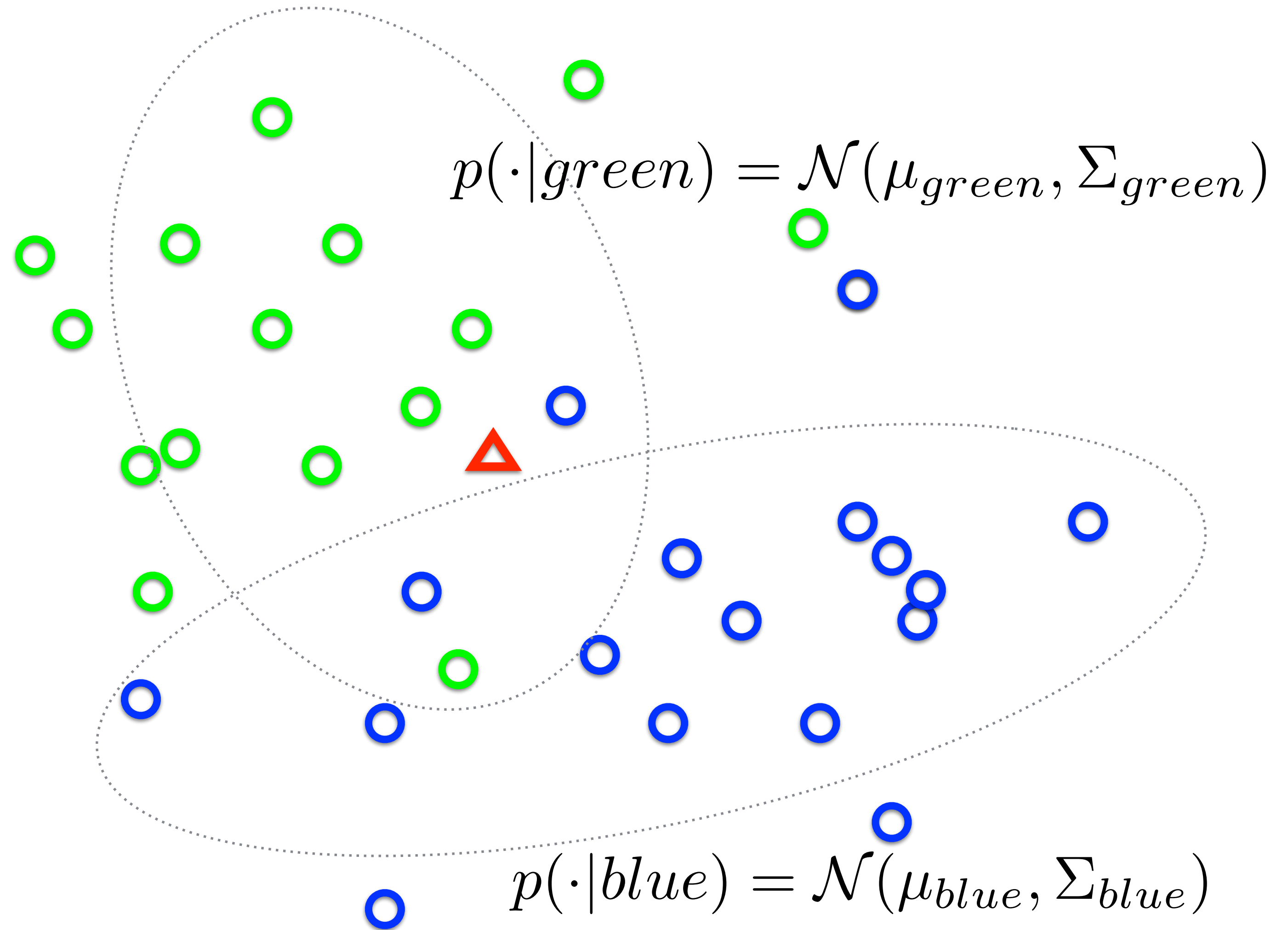
$$p(\text{blue}|\triangle) \propto \mathcal{N}(\triangle; \mu_{\text{blue}}, \Sigma_{\text{blue}})p(\text{blue})$$

○ 17 samples of grass

○ 15 samples of sky

$$p(\text{blue}) = \frac{17}{17 + 15}$$

$$p(\text{green}) = \frac{15}{17 + 15}$$



Bayes Rule (Review and Definitions)

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

Simple case:

- binary classification; i.e., $c \in \{1, 2\}$
- features are 1D; i.e., $x \in \mathbb{R}$

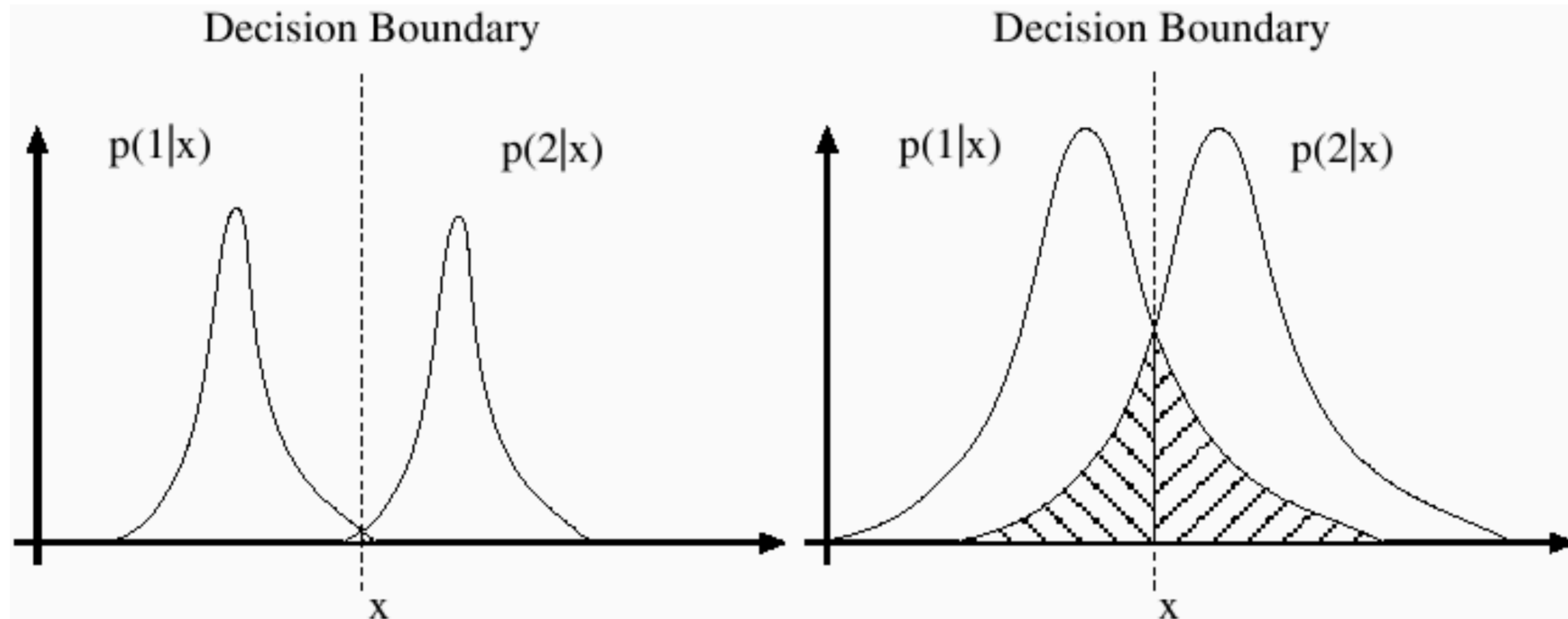
$$P(c|x) = \frac{P(x|c)p(c)}{P(x)}$$

General case:

- multi-class; i.e., $c \in \{1, \dots, 1000\}$
- features are high-dimensional; i.e., $x \in \mathbb{R}^{2,000+}$

Bayes' Risk

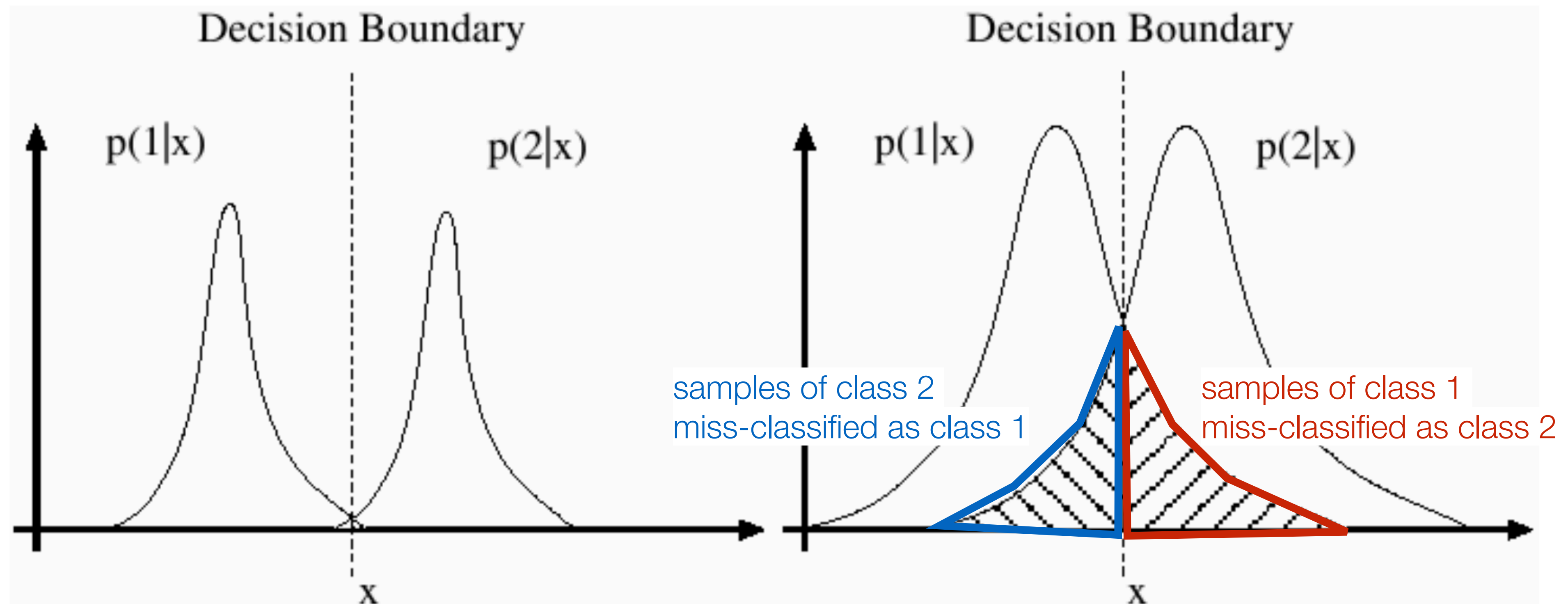
Some errors may be inevitable: the minimum risk (shaded area) is called the **Bayes' risk**



Forsyth & Ponce (2nd ed.) Figure 15.1

Bayes' Risk

Some errors may be inevitable: the minimum risk (shaded area) is called the **Bayes' risk**



Forsyth & Ponce (2nd ed.) Figure 15.1

Loss Functions and Classifiers

Loss

- Some errors may be more expensive than others

Example: A fatal disease that is easily cured by a cheap medicine with no side-effects. Here, false positives in diagnosis are better than false negatives

- We discuss two class classification:
 $L(1 \rightarrow 2)$ is the loss caused by calling 1 a 2

Total risk of using classifier \mathbf{s} is

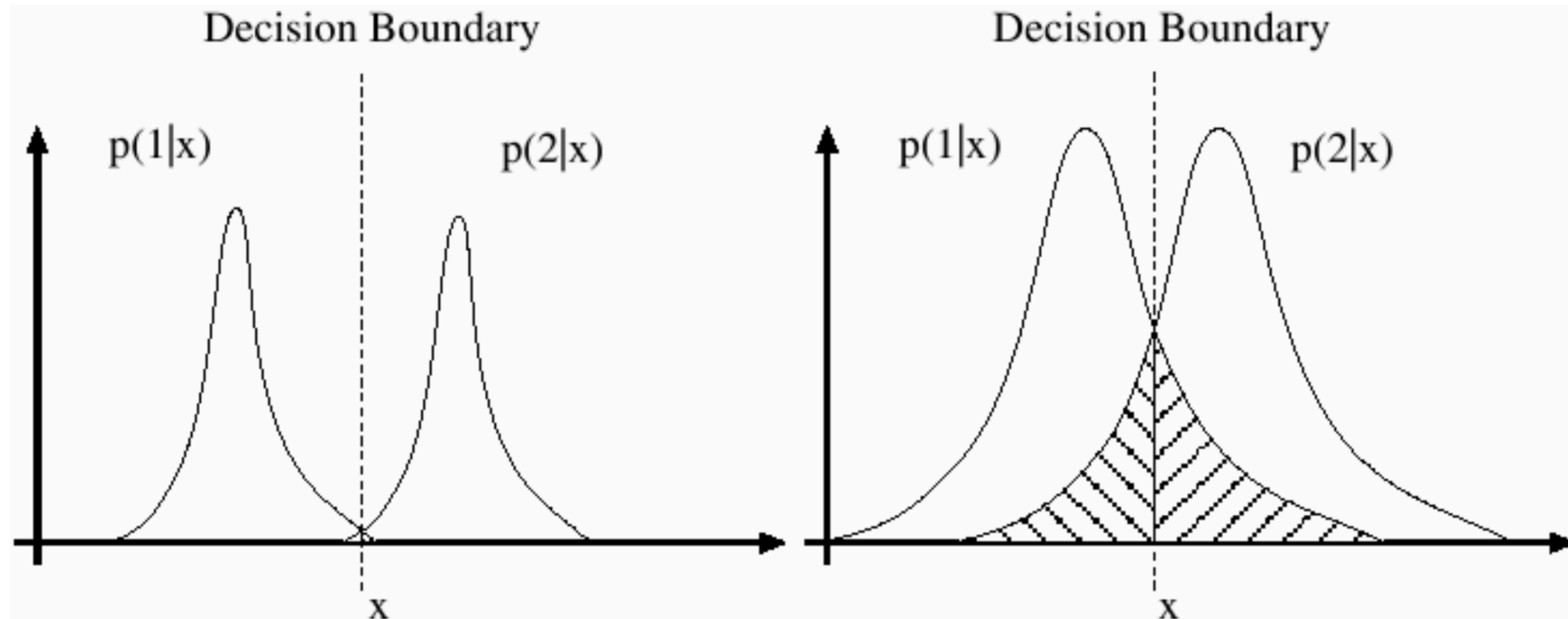
$$R(\mathbf{s}) = \underbrace{\Pr\{1 \rightarrow 2 \mid \text{using } \mathbf{s}\}}_{\text{Probability of Miss-classification}} \underbrace{L(1 \rightarrow 2)}_{\text{Loss}} + \underbrace{\Pr\{2 \rightarrow 1 \mid \text{using } \mathbf{s}\}}_{\text{Probability of Miss-classification}} \underbrace{L(2 \rightarrow 1)}_{\text{Loss}}$$

(i.e. cost of miss-classification)

(i.e. cost of miss-classification)

Bayes' Risk

Some errors may be inevitable: the minimum risk (shaded area) is called the **Bayes' risk**



Forsyth & Ponce (2nd ed.) Figure 15.1

Classifier Strategies

Classification strategies fall under two broad types: **parametric** and **non-parametric**.

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- fast, compact
- flexibility and accuracy depend on model assumptions

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Parametric classifiers are **model driven**. The parameters of the model are learned from training examples. New data points are classified by the learned model.

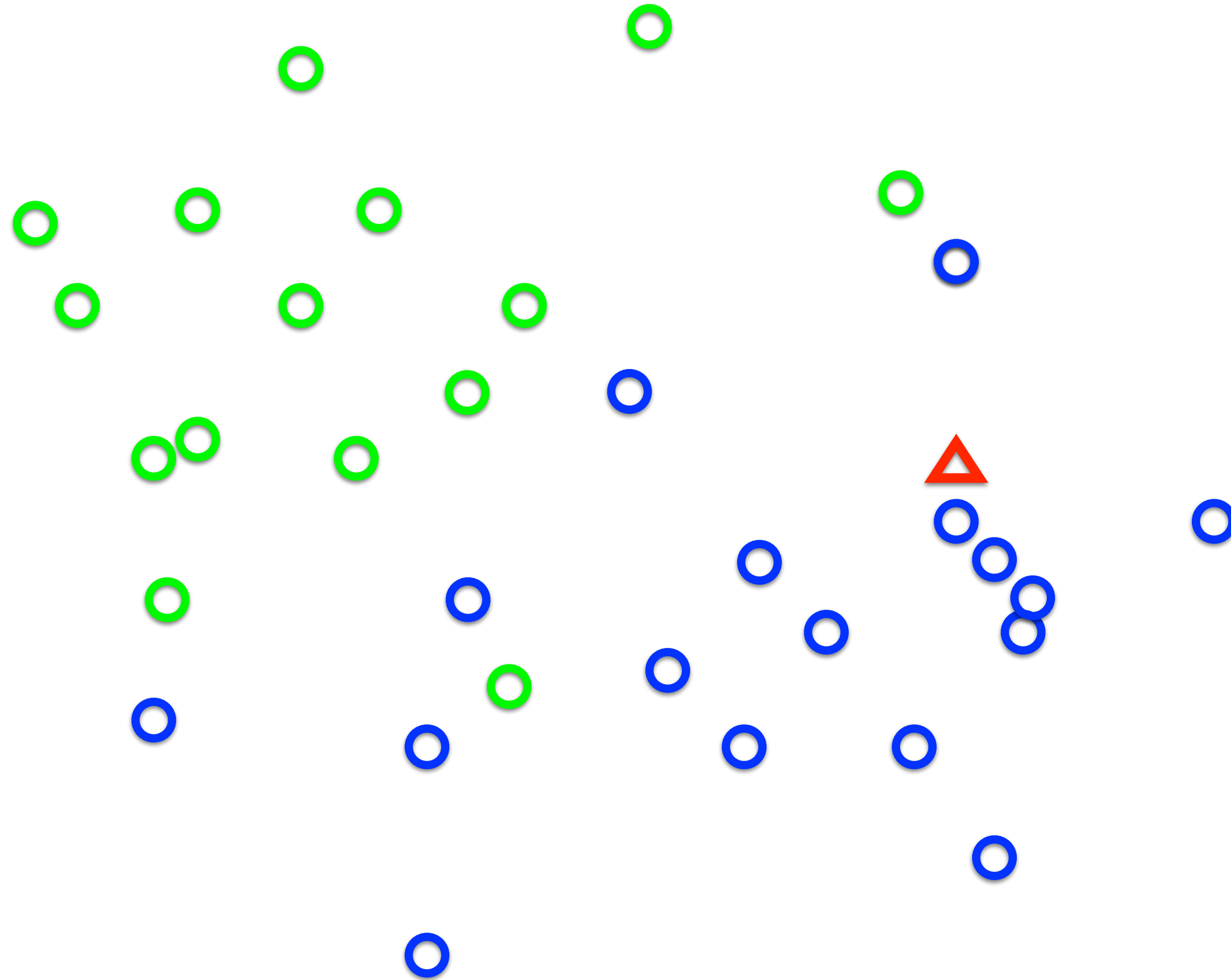
- fast, compact
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Non-parametric classifiers are **data driven**. New data points are classified by comparing to the training examples directly. "The data is the model".

- slow
- highly flexible decision boundaries

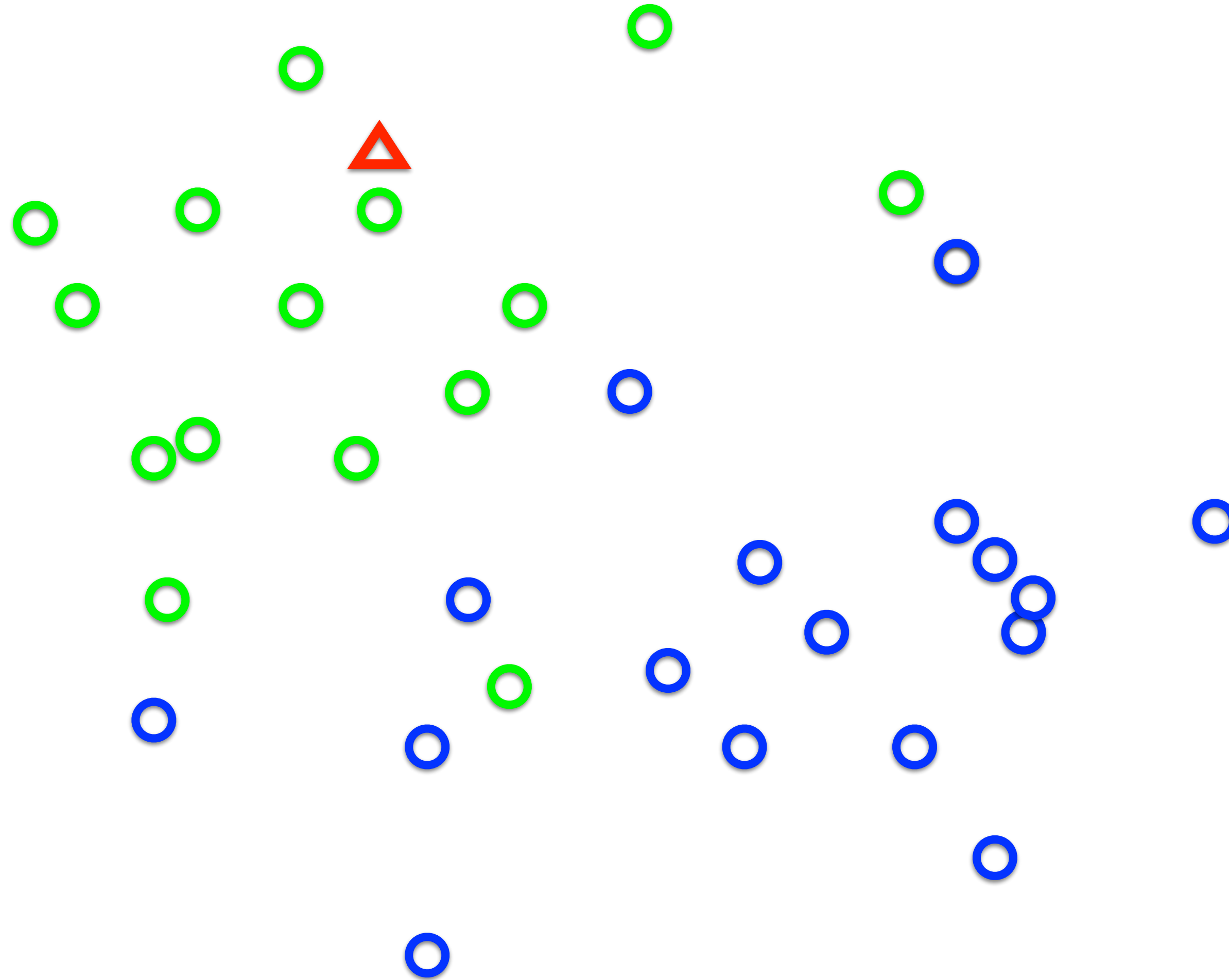
Nearest Neighbor Classifier

Given a new data point, assign the label of nearest training example in feature space.



Nearest Neighbor Classifier

Given a new data point, assign the label of nearest training example in feature space.



Nearest Neighbor Classifier

Find nearest neighbour in training set

$$i_{NN} = \arg \min_i |\mathbf{x}_q - \mathbf{x}_i|$$

Assign class to class of the nearest neighbour

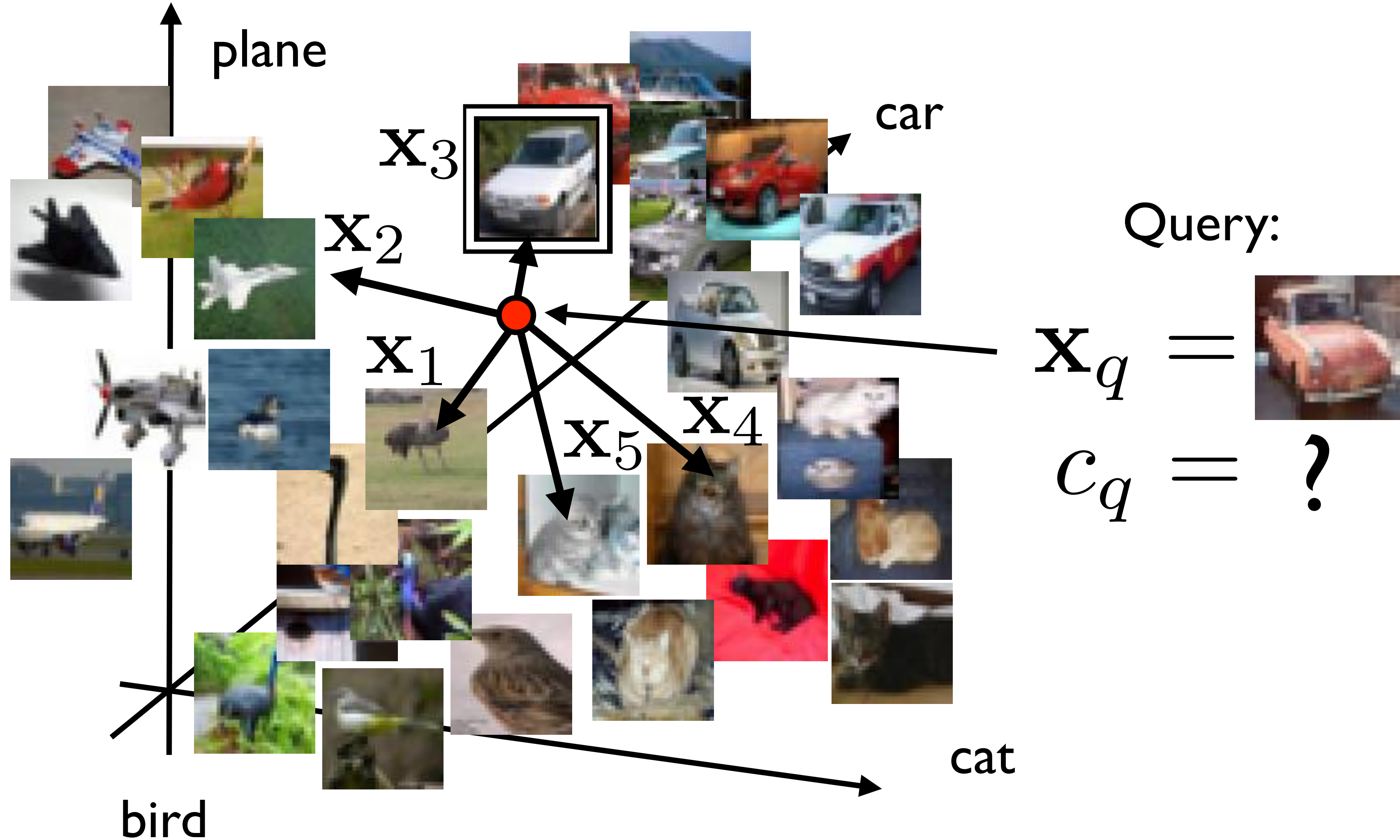
$$\hat{y}(\mathbf{x}_q) = y(\mathbf{x}_{i_{NN}})$$




Calculate $|\mathbf{x}_q - \mathbf{x}_i|$
for all training data

Nearest Neighbor Classifier

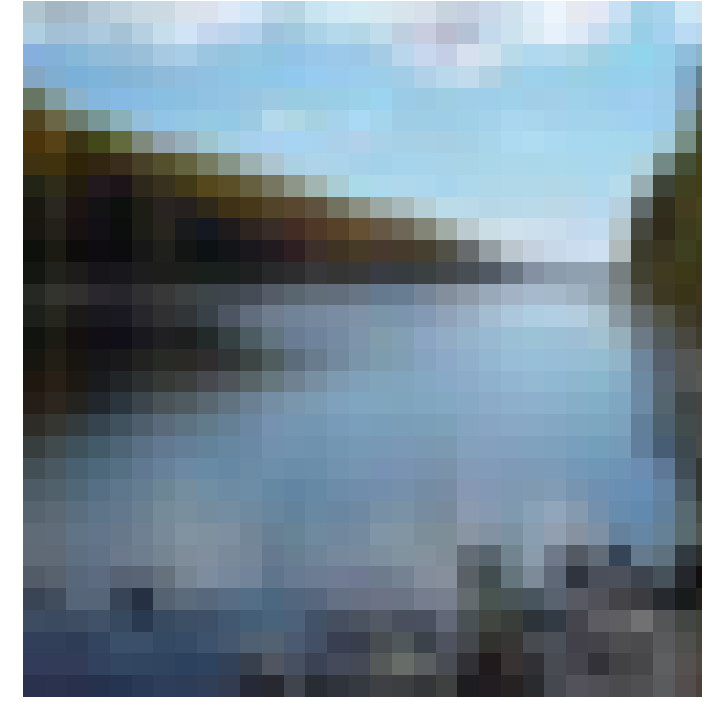
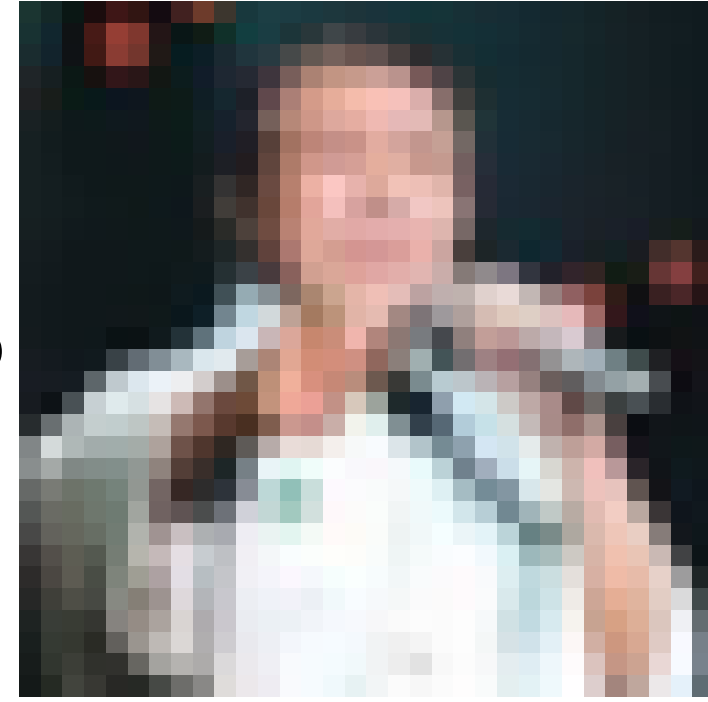
We can view each image as a point in a high dimensional space



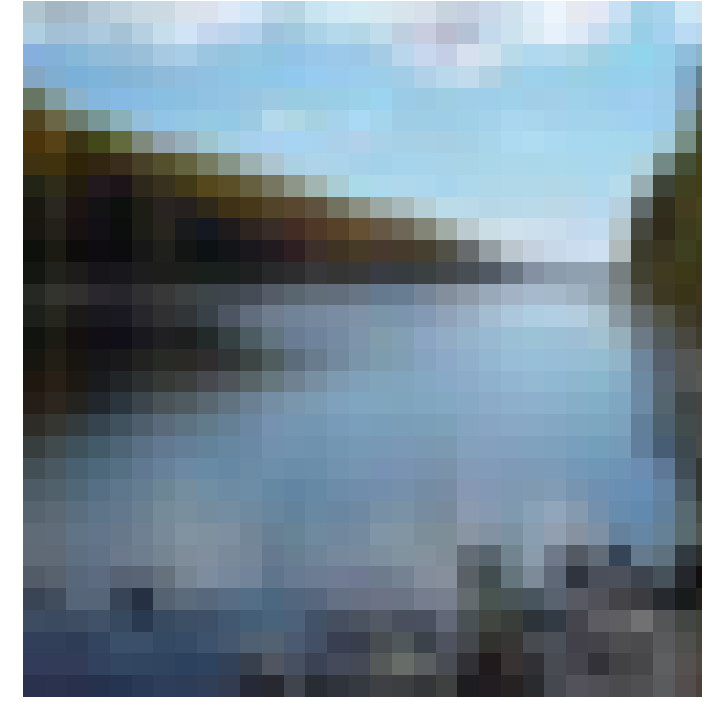
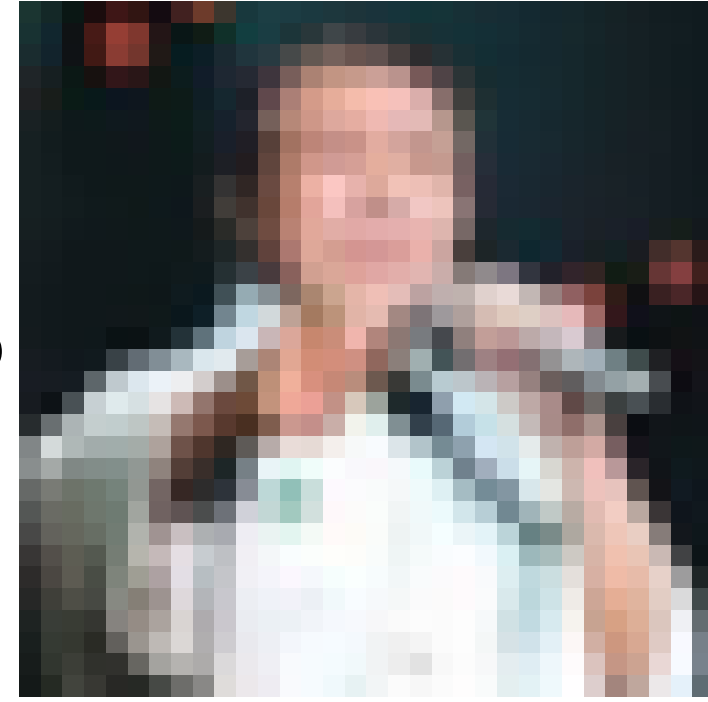


What do nearest neighbours
look like with 80 million images?

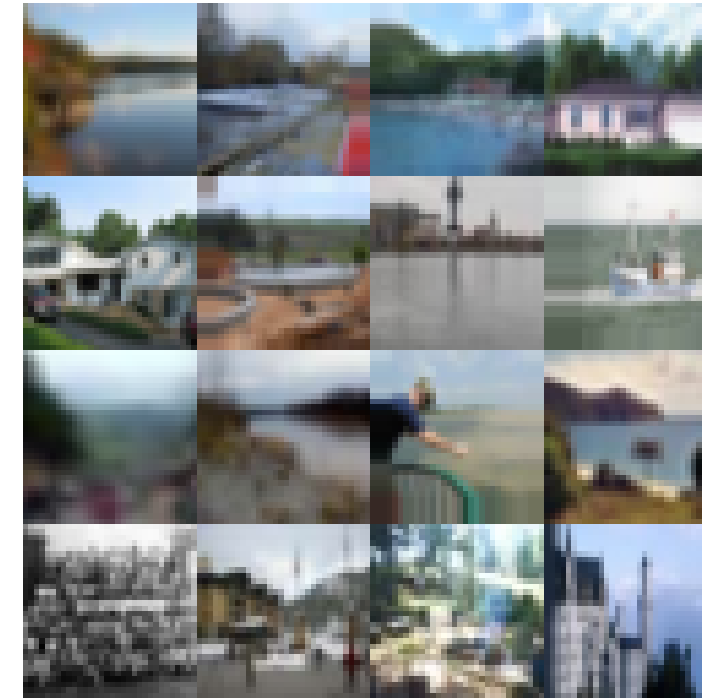
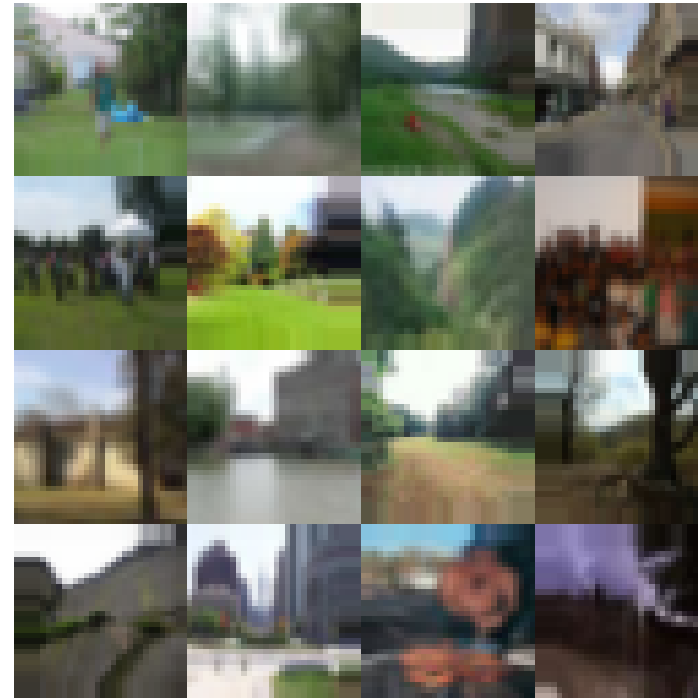
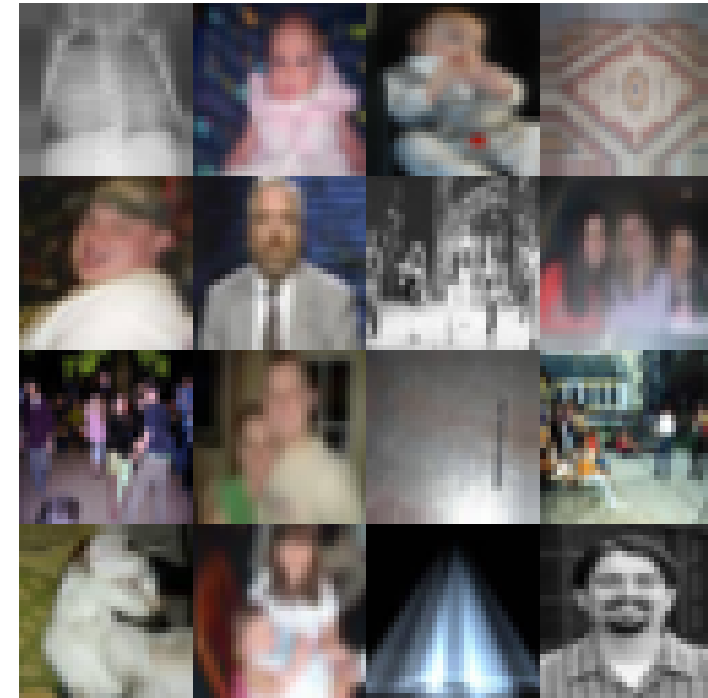
[Torralba, Fergus, Freeman '08]



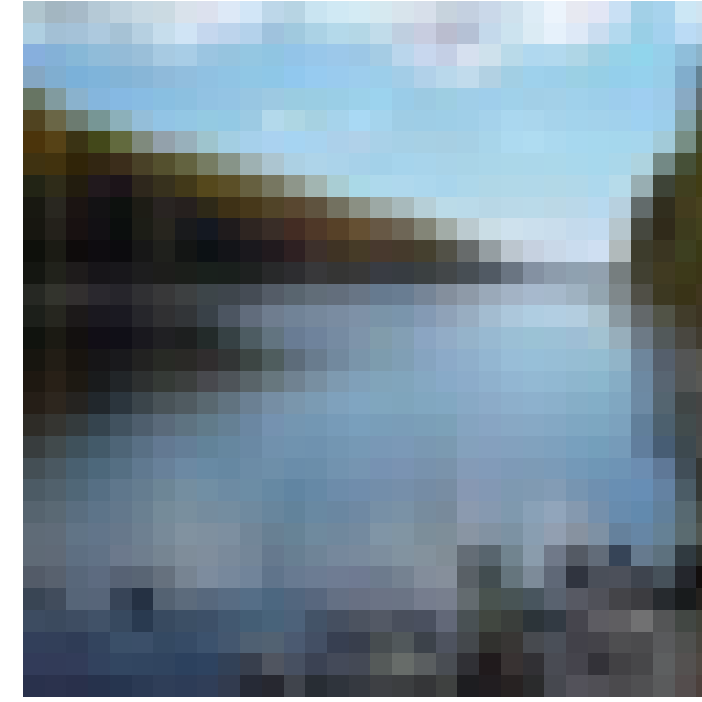
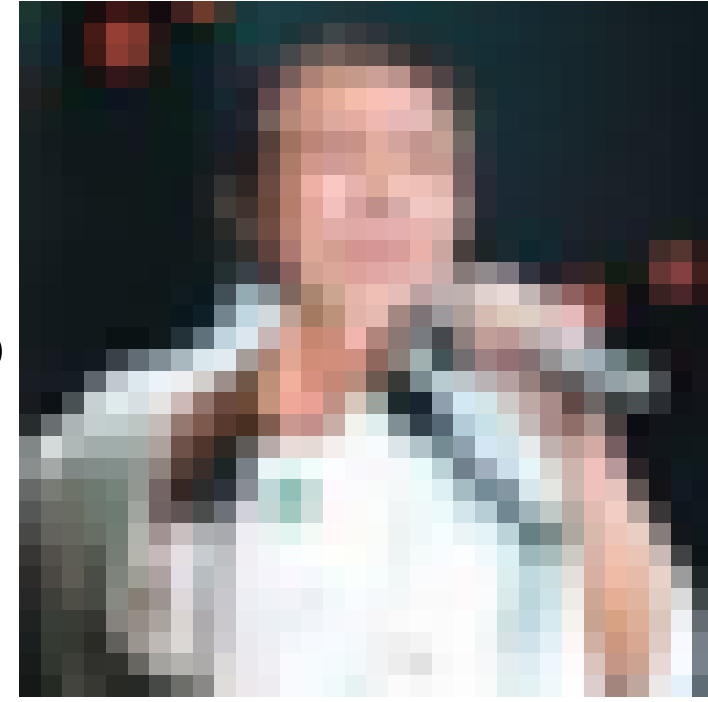
Query



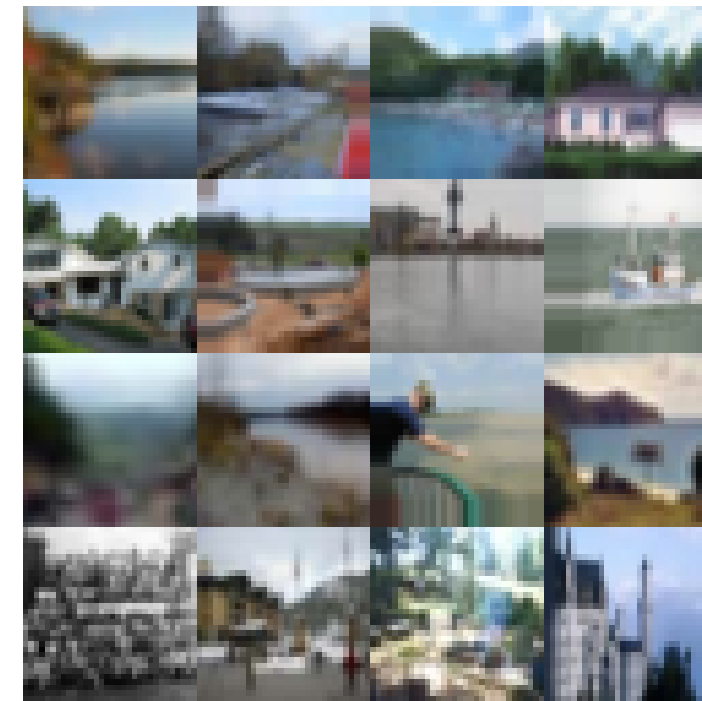
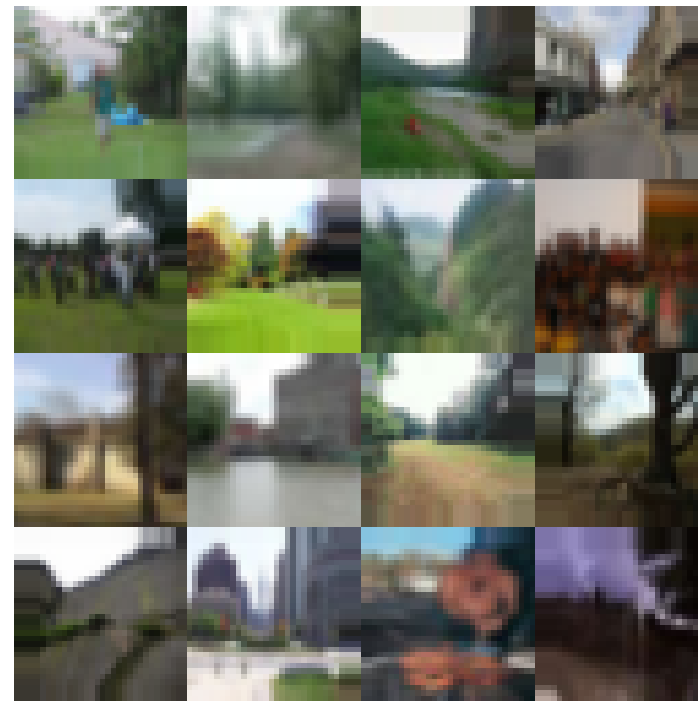
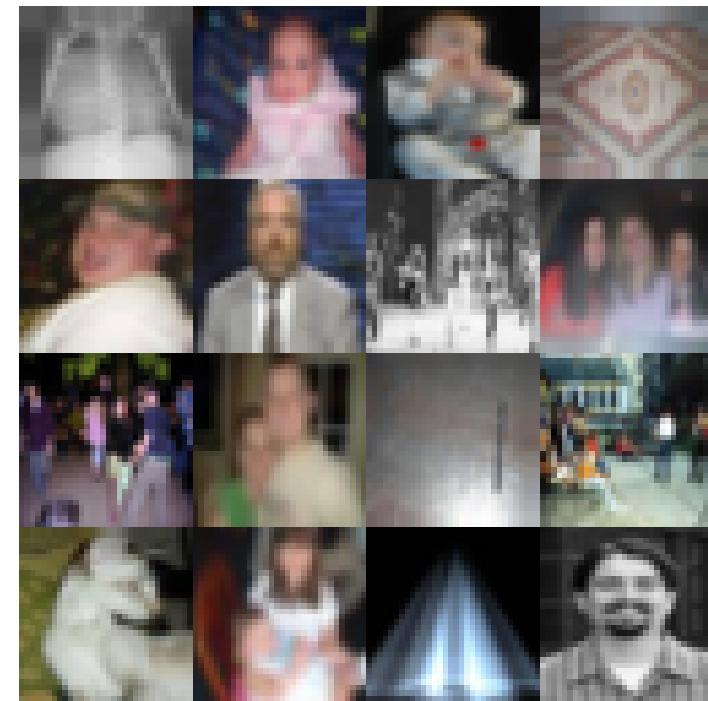
Query



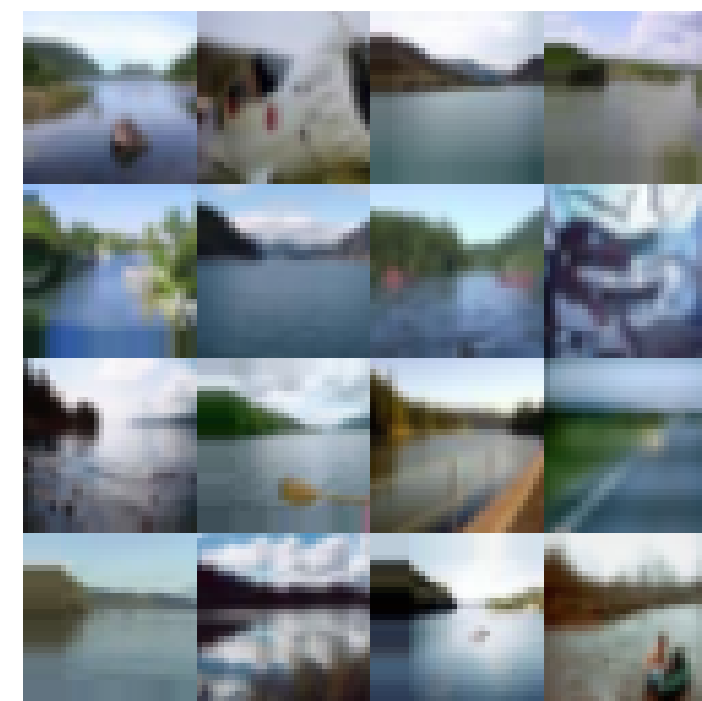
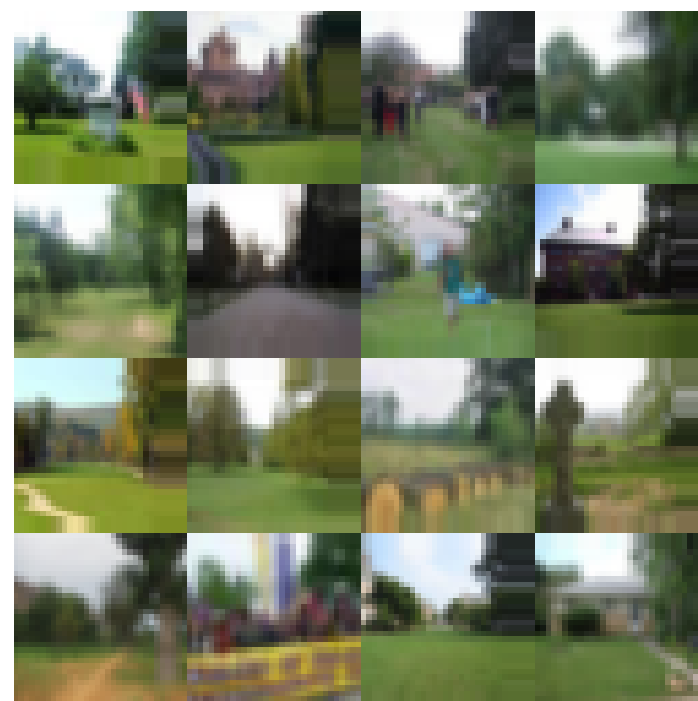
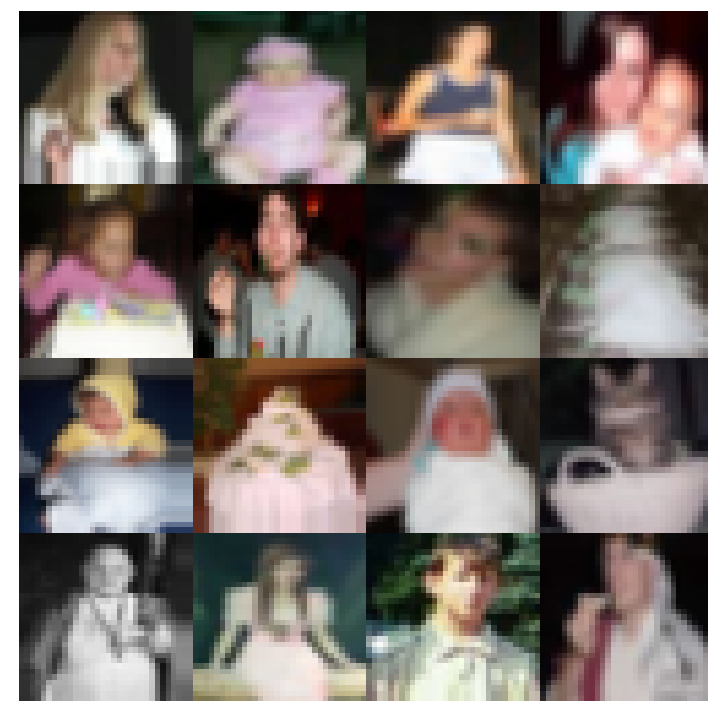
7900



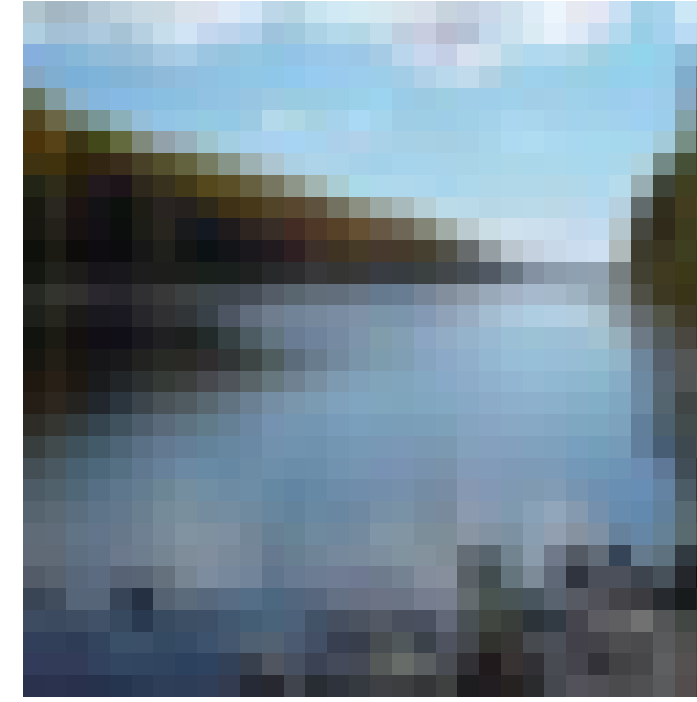
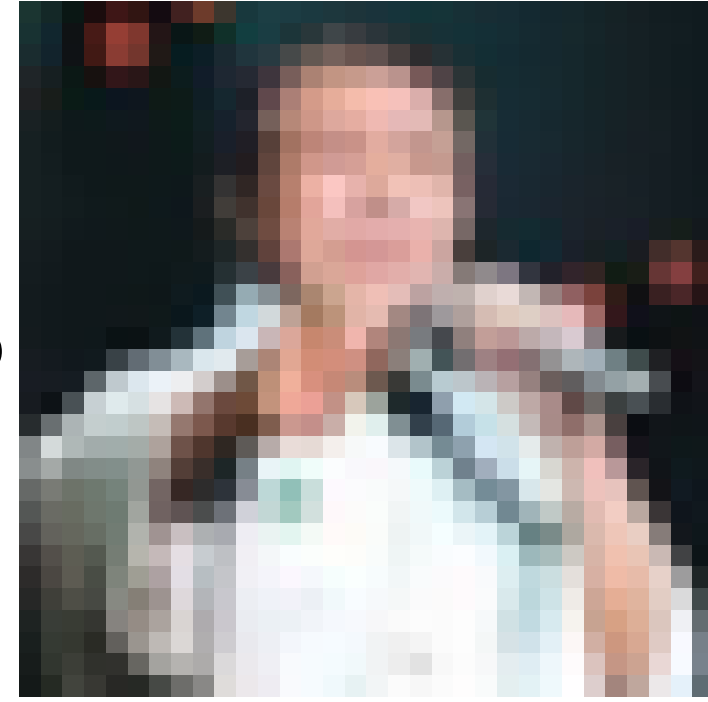
Query



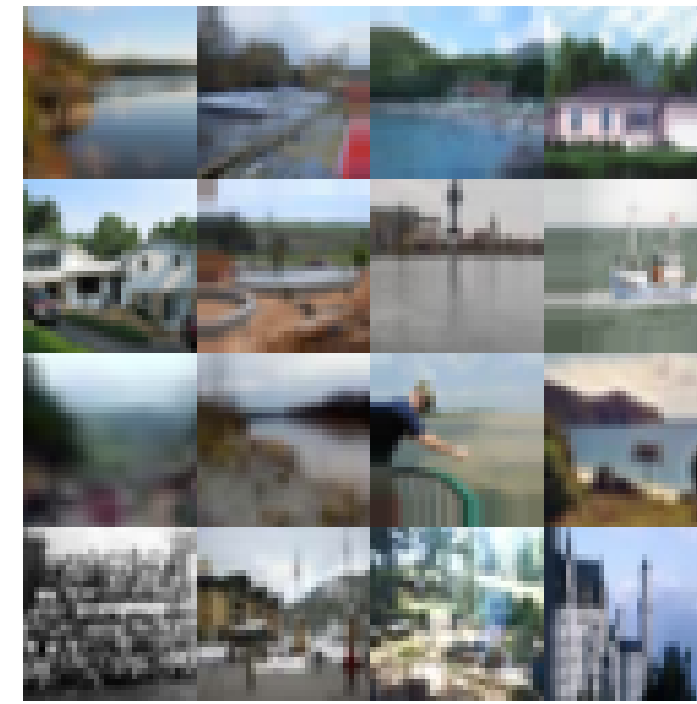
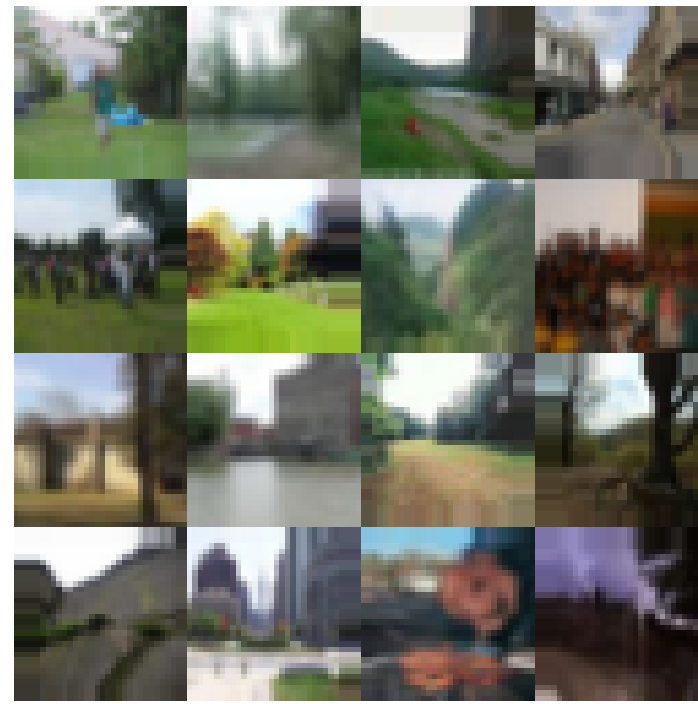
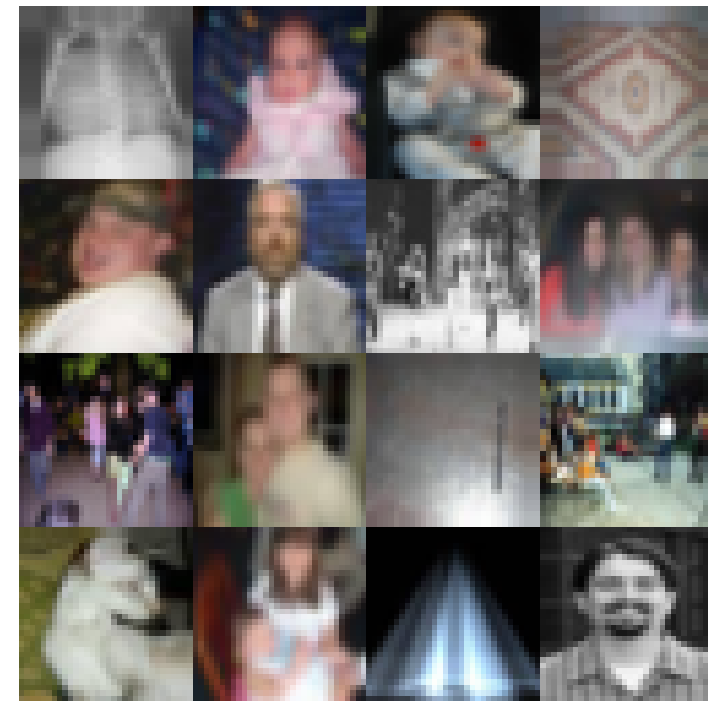
7900



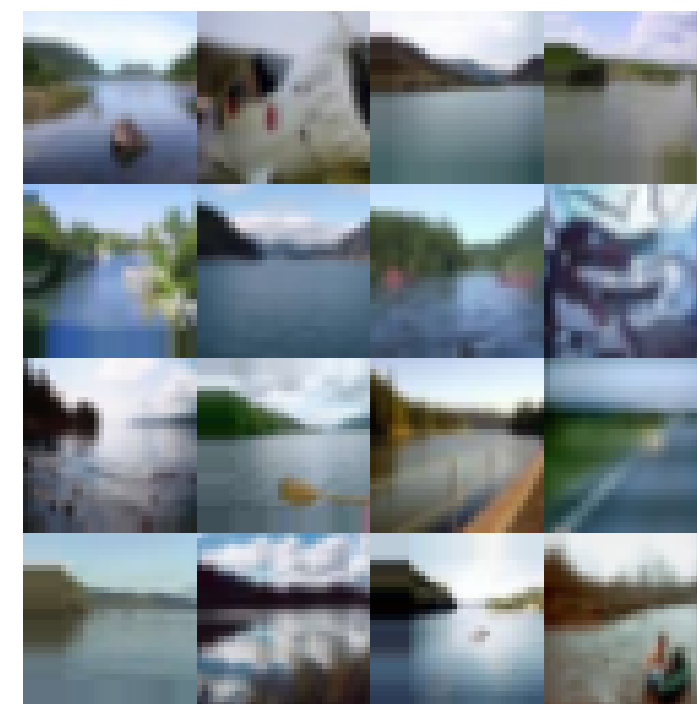
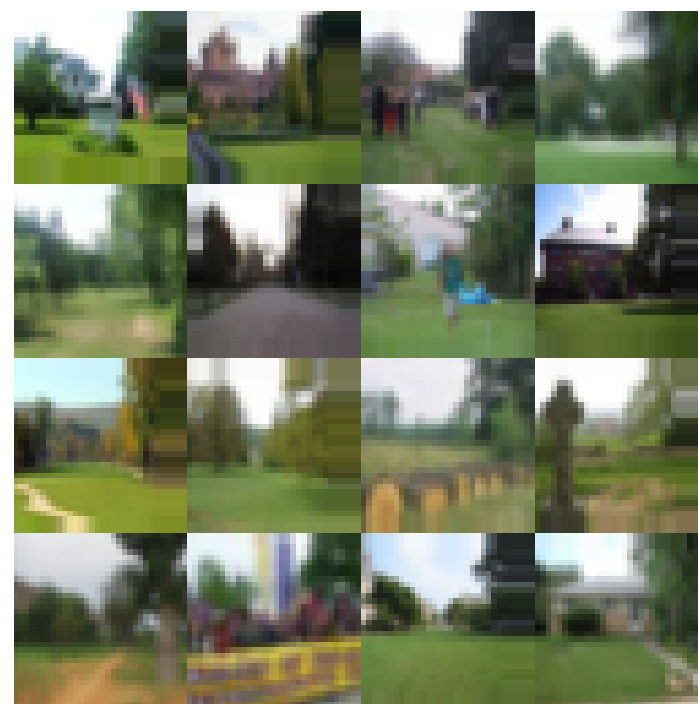
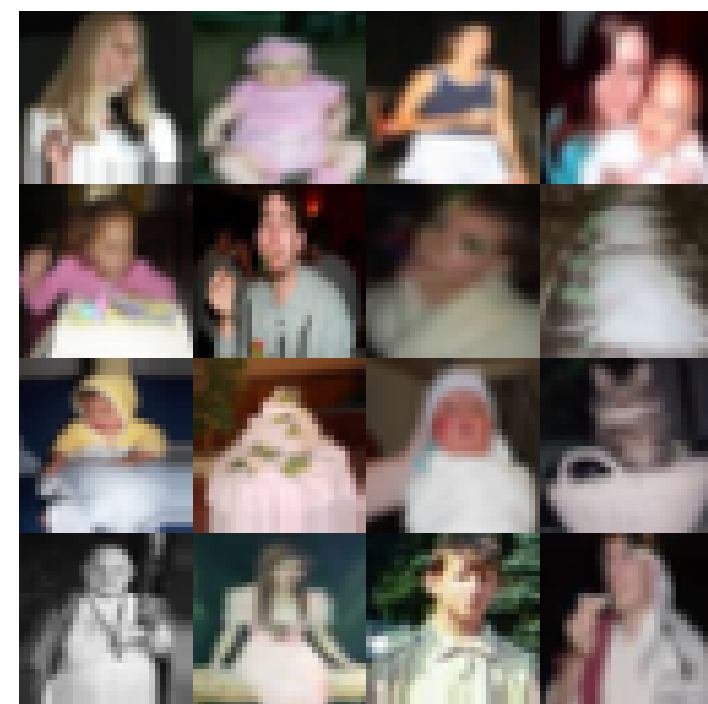
790,000



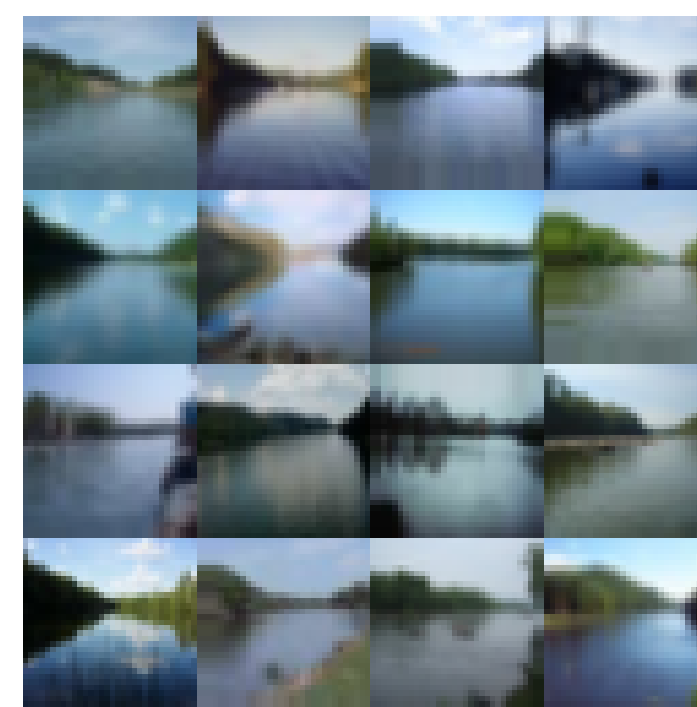
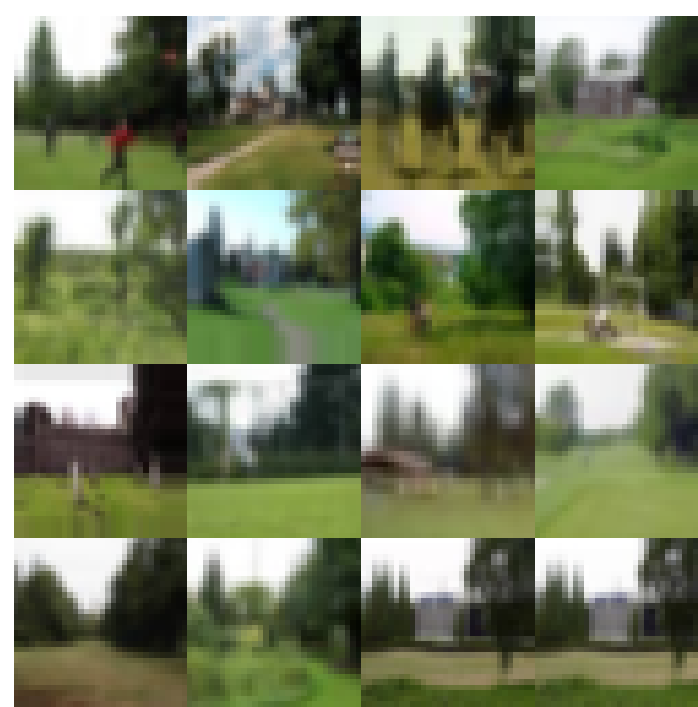
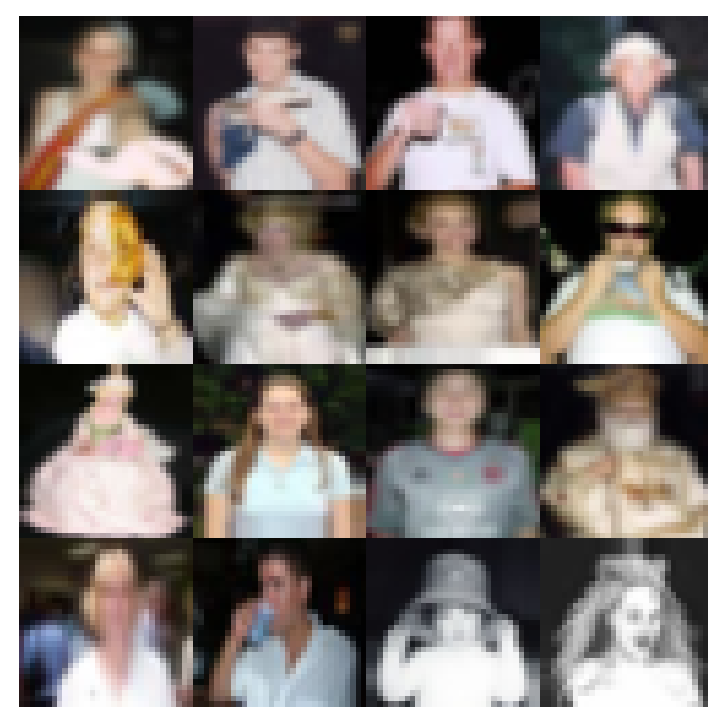
Query



7900



790,000



79,000,000

k-Nearest Neighbor (kNN) Classifier

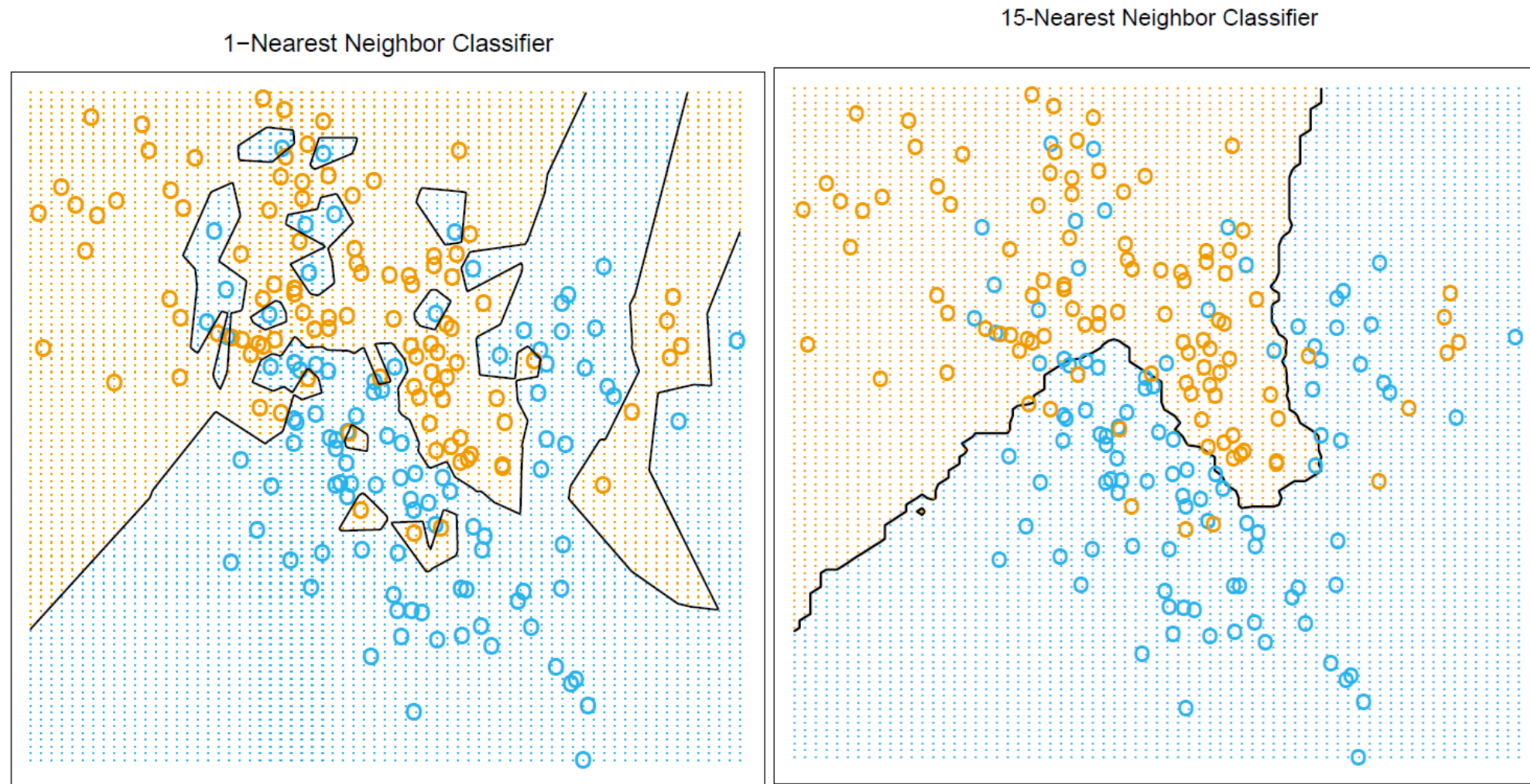
We can gain some robustness to noise by voting over **multiple** neighbours.

Given a **new** data point, find the k nearest training examples. Assign the label by **majority vote**.

Simple method that works well if the **distance measure** correctly weights the various dimensions

For **large data sets**, as k increases kNN approaches optimality in terms of minimizing probability of error

k-Nearest Neighbor (kNN) Classifier



kNN decision boundaries respond to local clusters where one class dominates

Figure credit: Hastie, Tibshirani & Friedman (2nd ed.)

Classifier Strategies

Classification strategies fall under two broad types: **parametric** and **non-parametric**.

Parametric classifiers are **model driven**. The parameters of the model are learned from training examples. New data points are classified by the learned model.

- fast, compact
- flexibility and accuracy depend on model assumptions

Non-parametric classifiers are **data driven**. New data points are classified by comparing to the training examples directly. "The data is the model".

- slow
- highly flexible decision boundaries

Support Vector Machines (SVM)

Idea: Try to obtain the decision boundary directly

The decision boundary is parameterized as a **separating hyperplane** in feature space.

— e.g. a separating line in 2D

We choose the hyperplane that is as far as possible from each class - that maximizes the distance to the closest point from either class.

Linear Classifier

Defines a score function:

$$f(\mathbf{x}_i, \mathbf{W}, \mathbf{b}) = \mathbf{W}\mathbf{x}_i + \mathbf{b}$$

image features

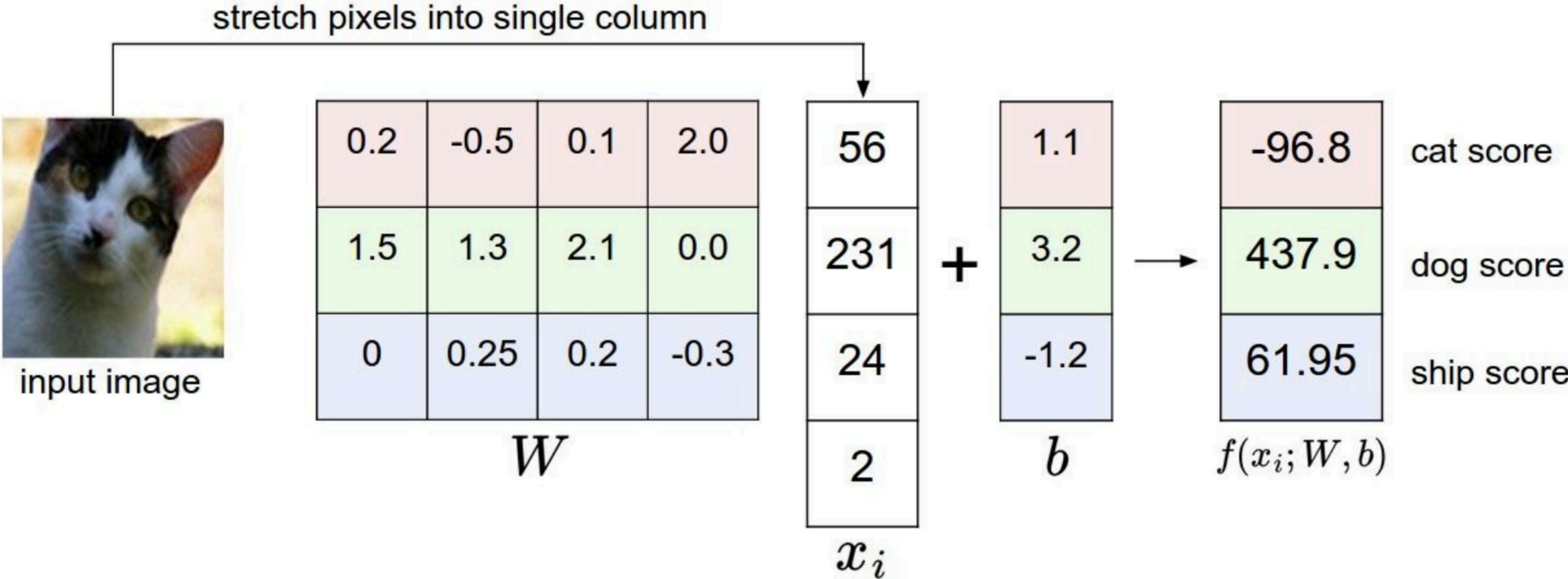
weights

(parameters)

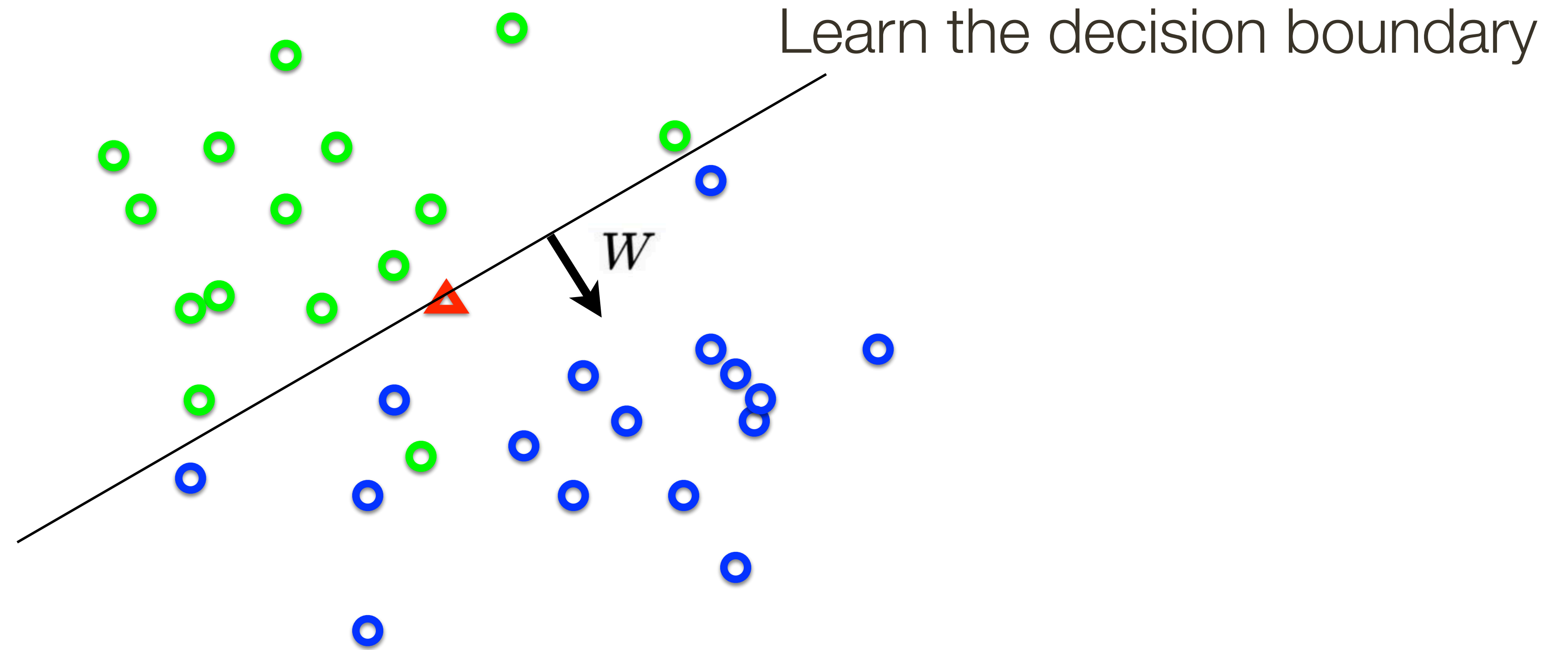
bias vector

Linear Classifier

Example with an image with 4 pixels, and 3 classes (cat/dog/ship)

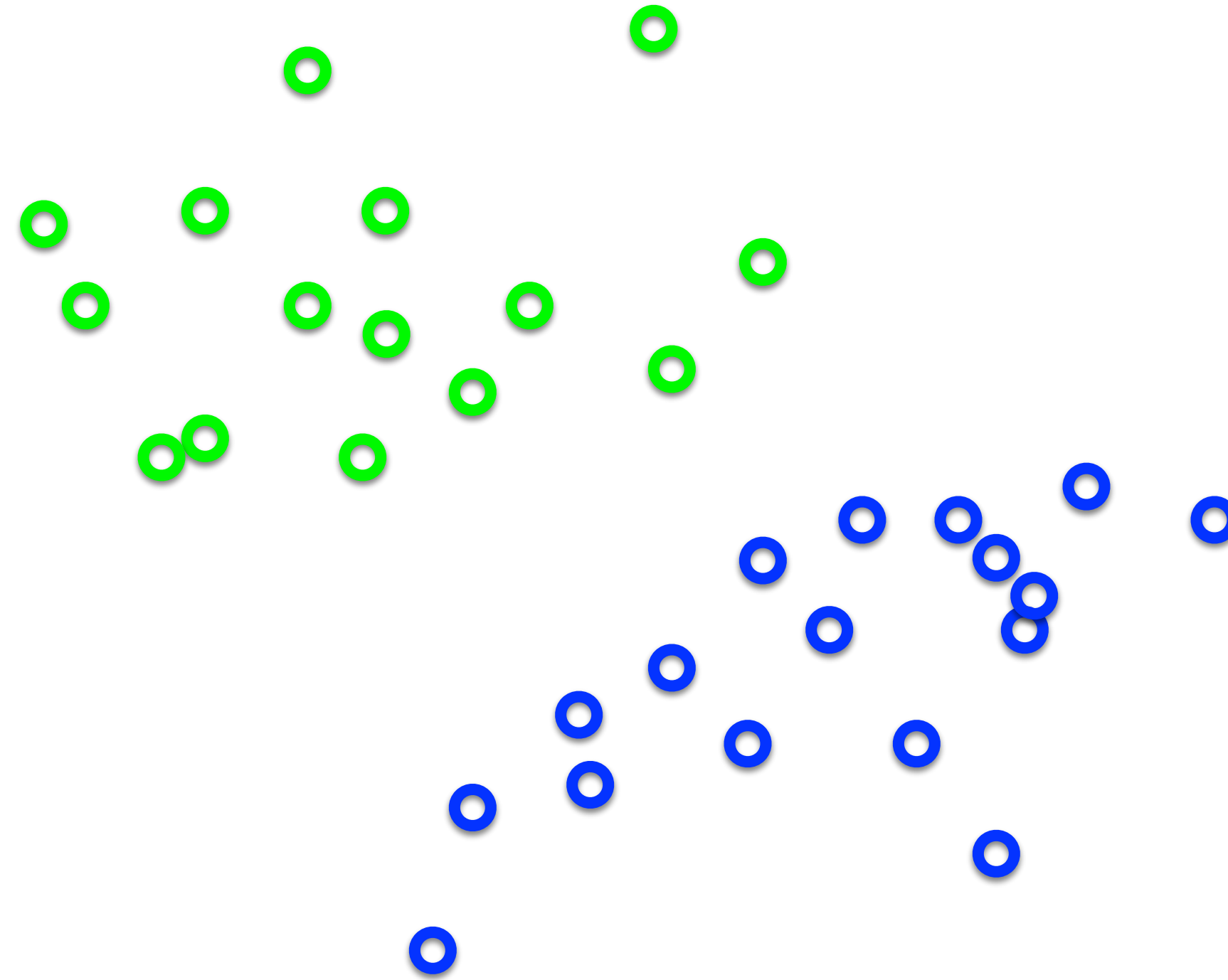


Support Vector Machines (SVM)



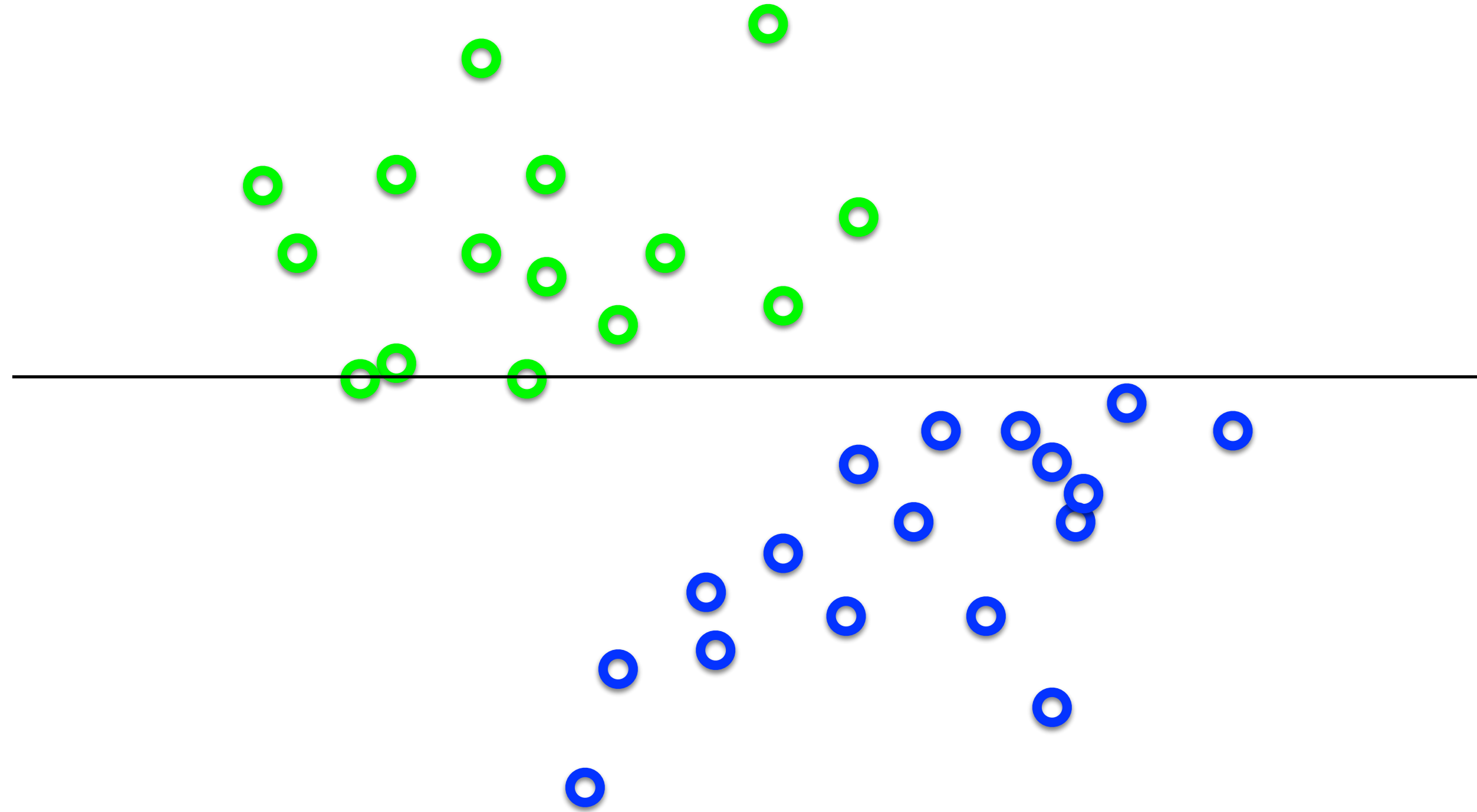
Support Vector Machines (SVM)

What's the best \mathbf{w} ?



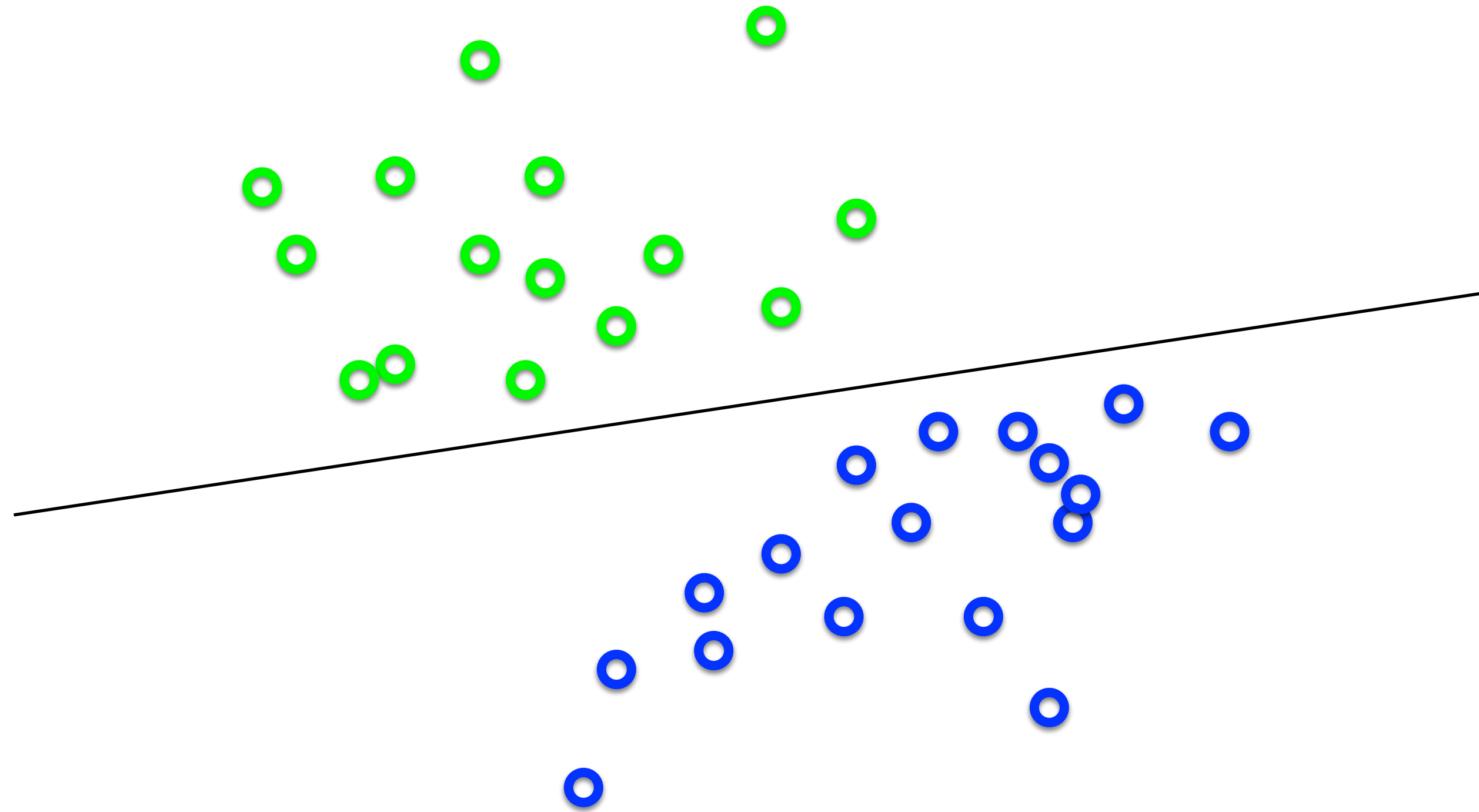
Support Vector Machines (SVM)

What's the best w ?



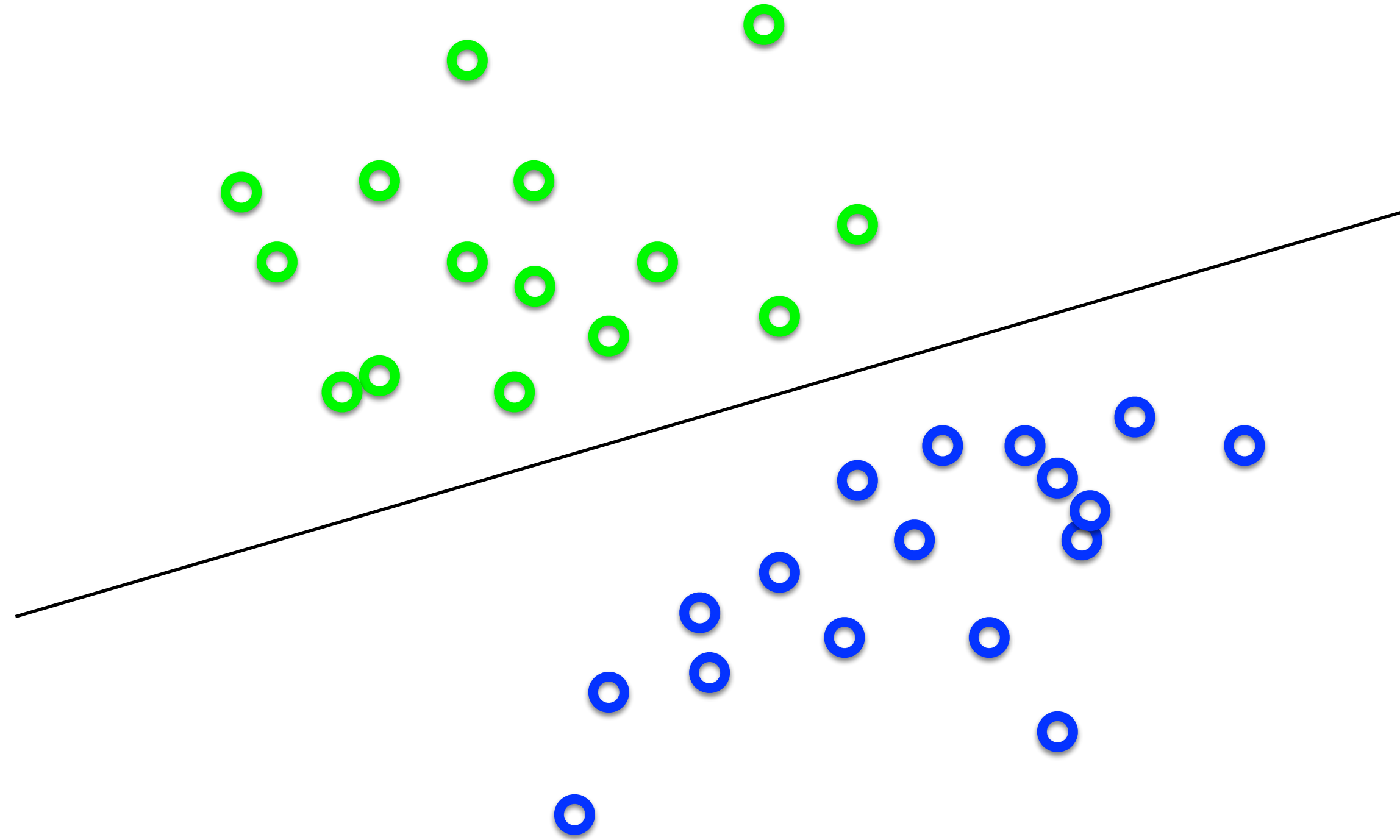
Support Vector Machines (SVM)

What's the best \mathbf{w} ?



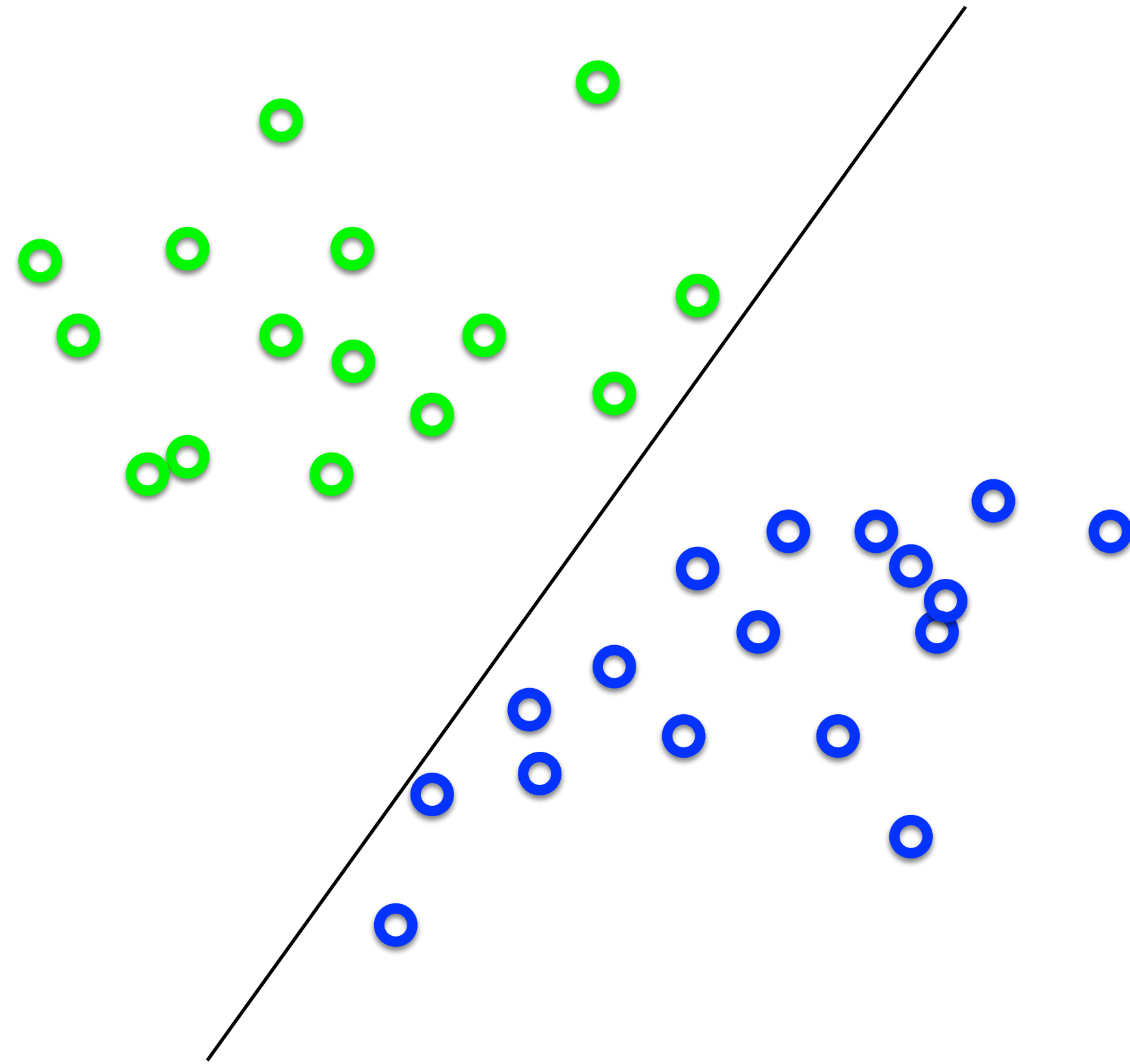
Support Vector Machines (SVM)

What's the best \mathbf{w} ?



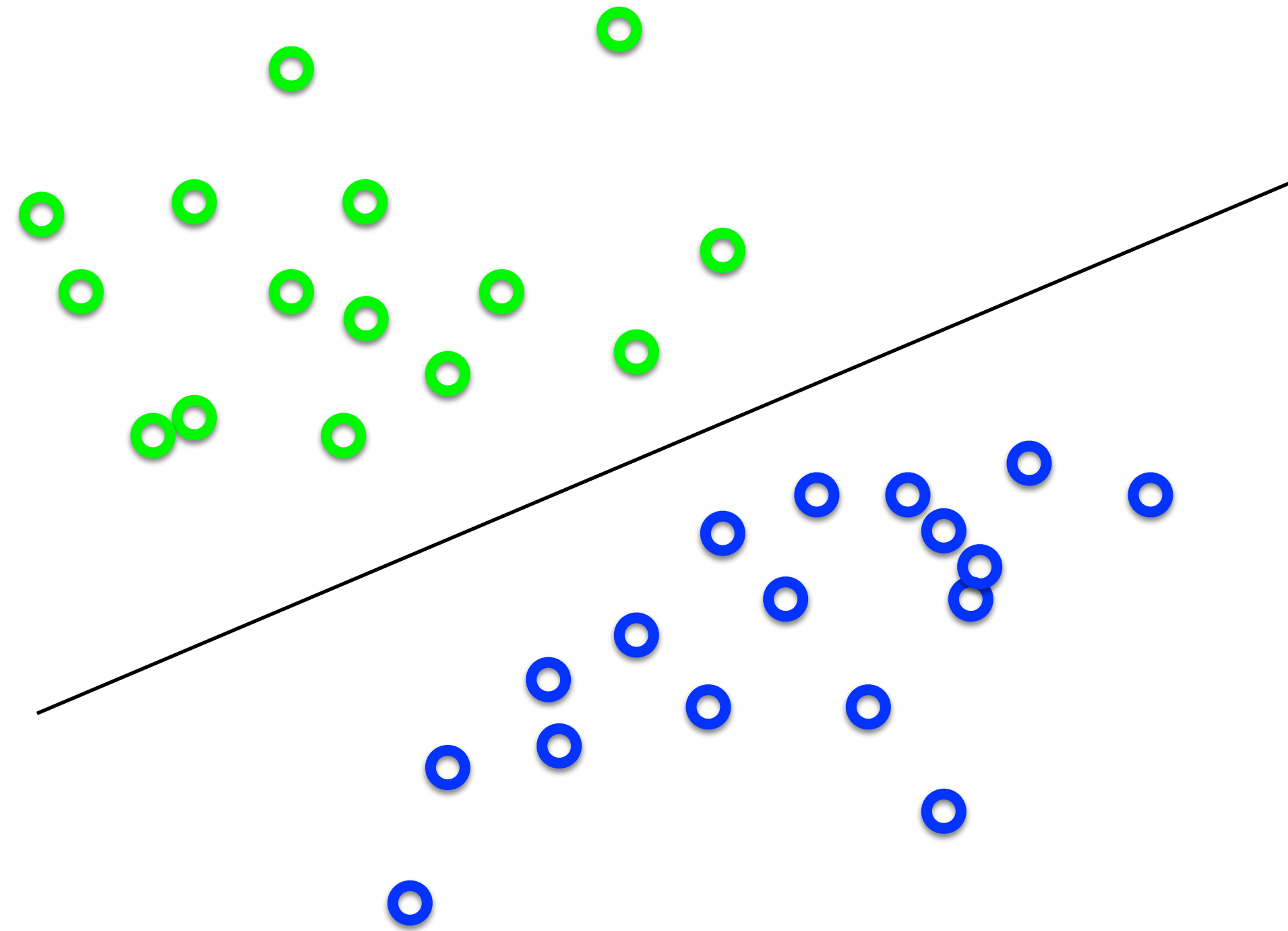
Support Vector Machines (SVM)

What's the best \mathbf{w} ?



Support Vector Machines (SVM)

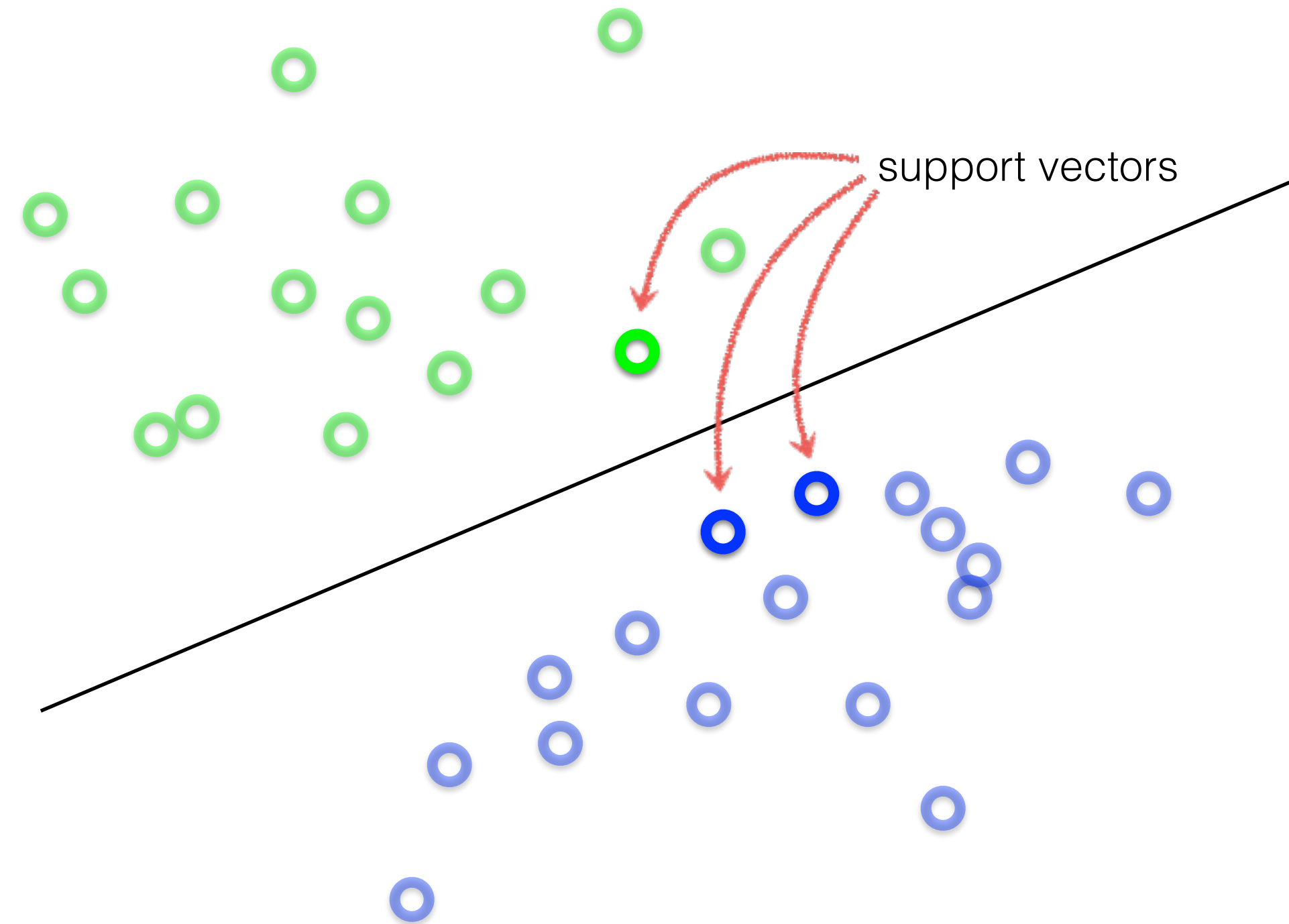
What's the best \mathbf{w} ?



Intuitively, the line that is the farthest from all interior points

Support Vector Machines (SVM)

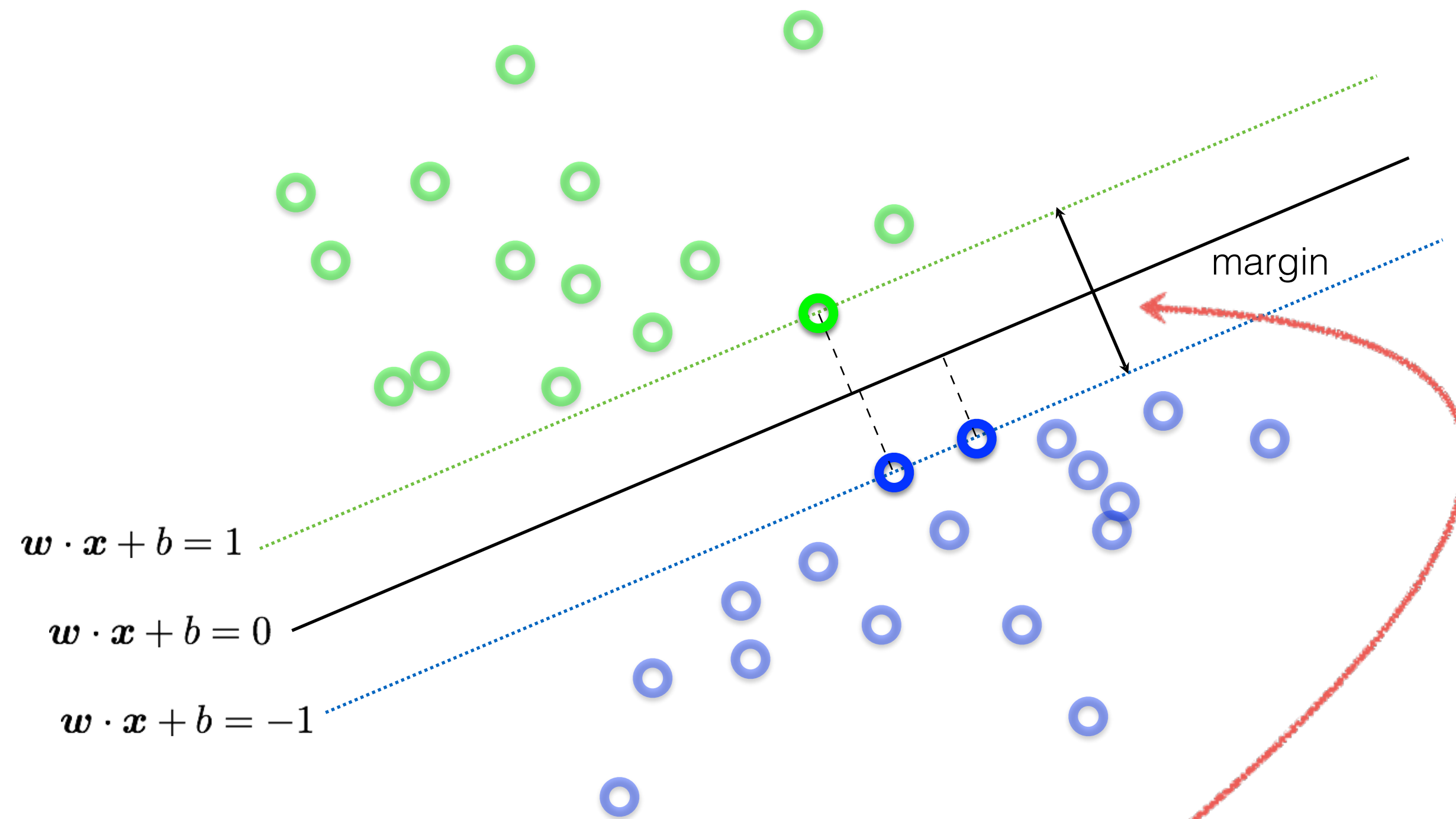
What's the best \mathbf{w} ?



Want a hyperplane that is far away from 'inner points'

Support Vector Machines (SVM)

Find hyperplane \mathbf{w} such that ...



the gap between parallel hyperplanes $\frac{2}{\|\mathbf{w}\|}$ is maximized

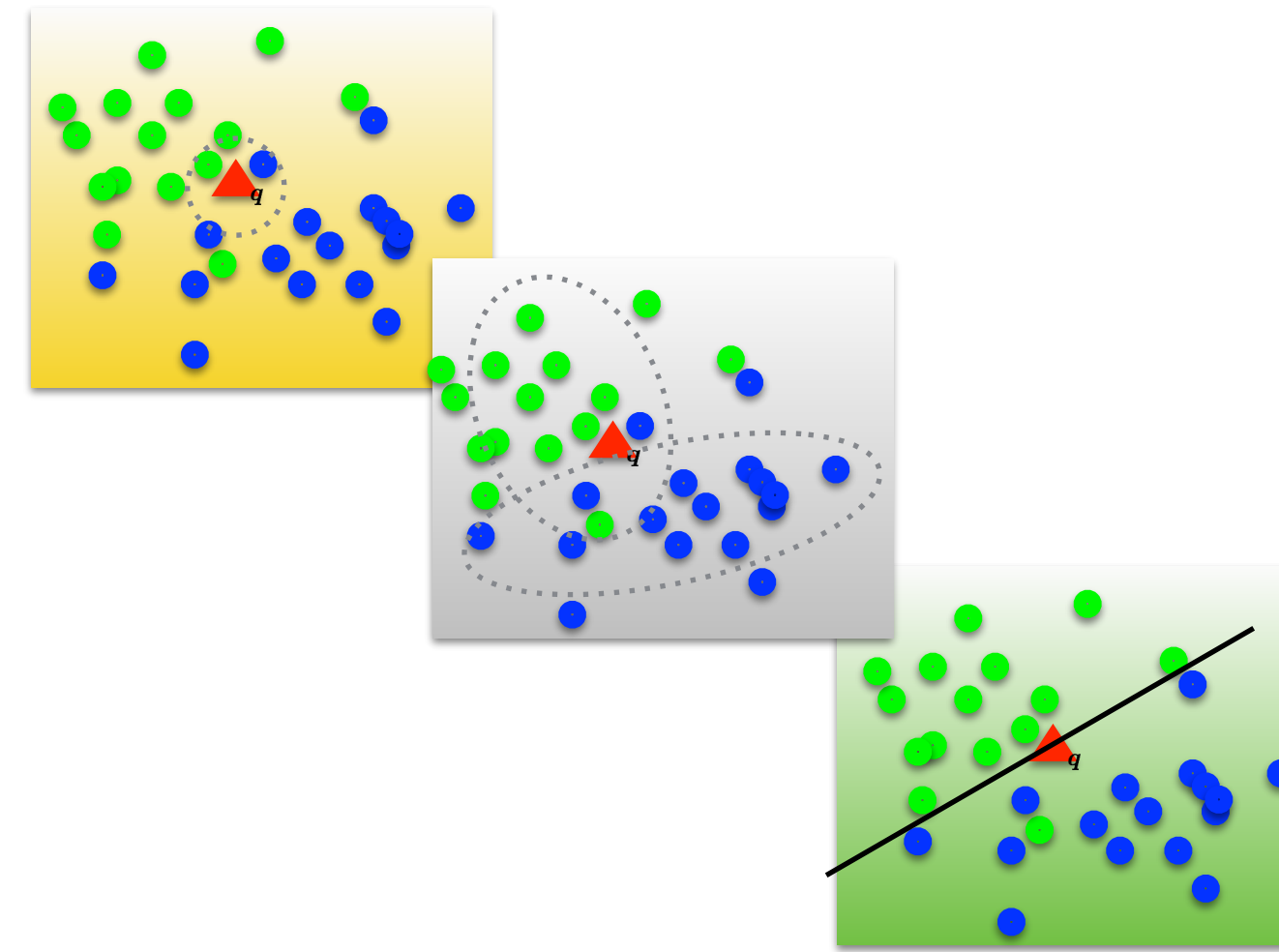
Image Classification

Classification Algorithms

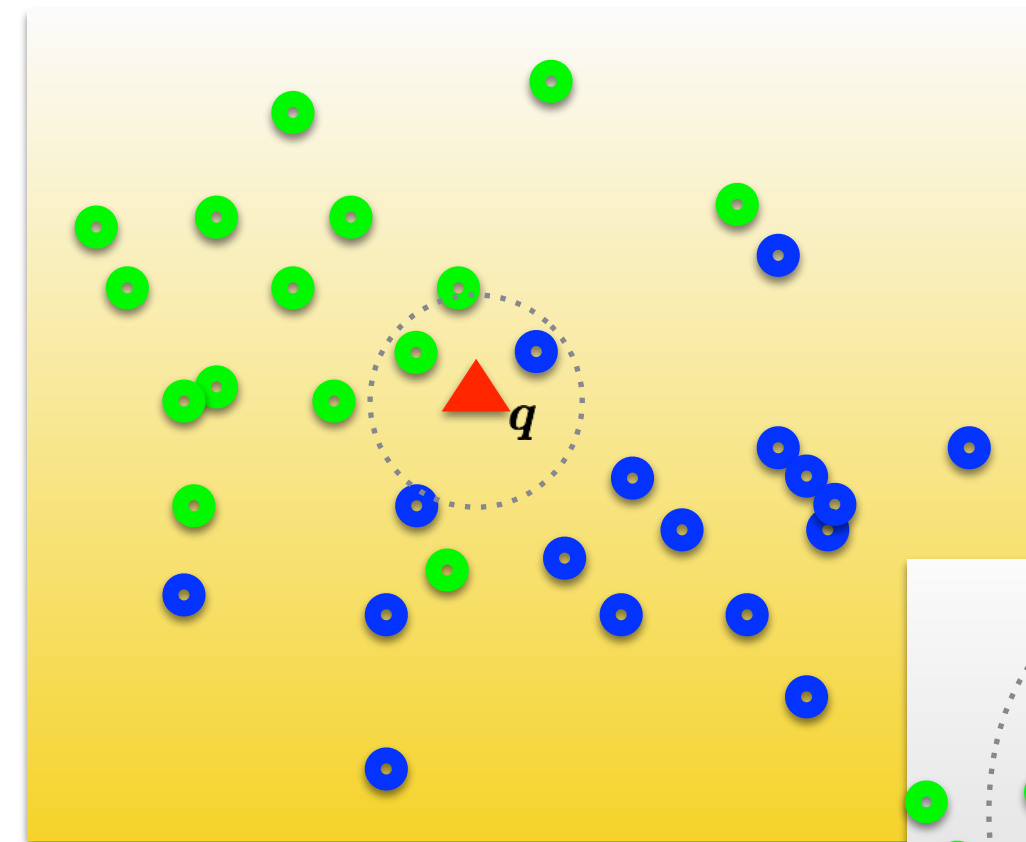
- Bayes' Classifier
- Nearest Neighbor Classifier
- SVM Classifier

Representation of Images

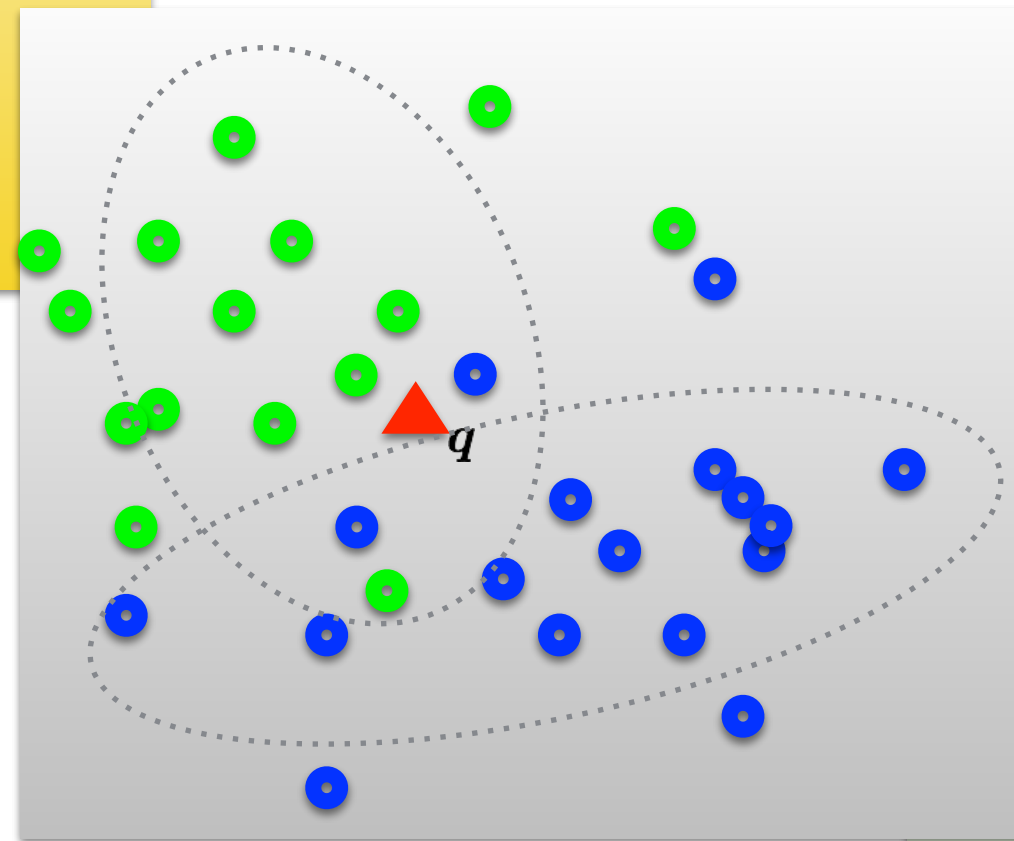
- Image pixels directly
- Bag of Words



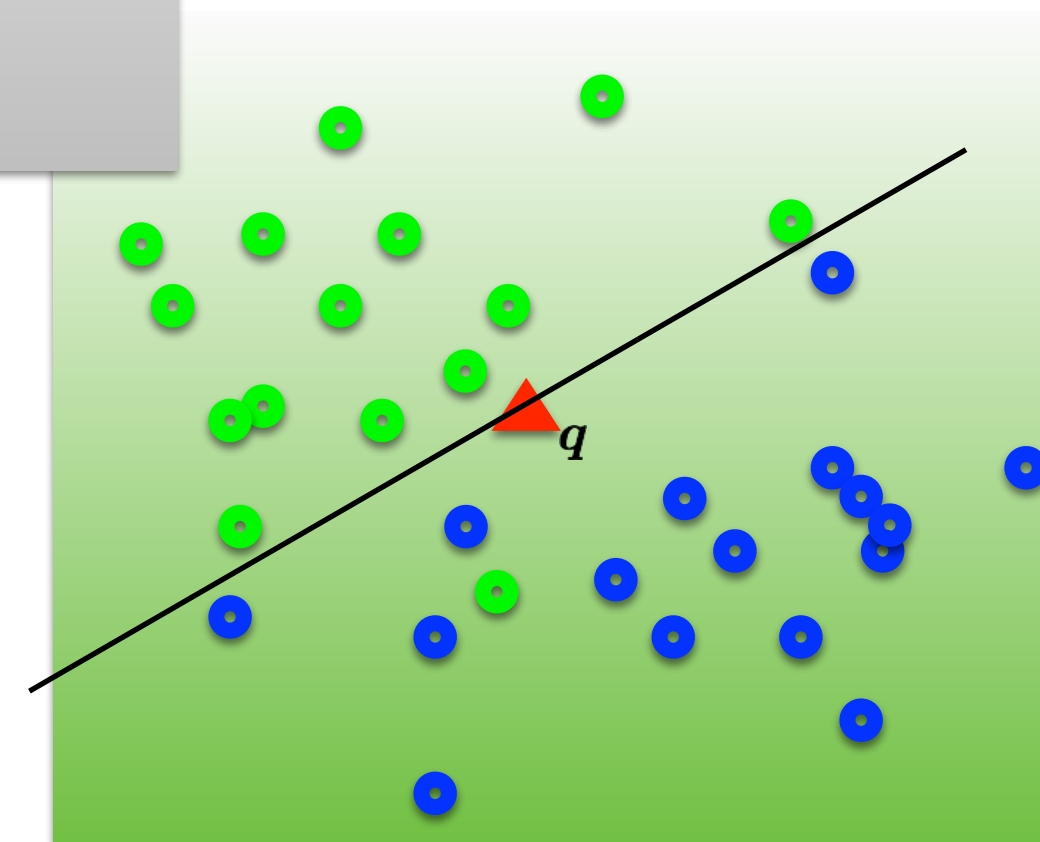
3. Classify: Train and text classifier using BOWs



K nearest neighbors



Naïve Bayes



Support Vector Machine

Bag-of-Words Representation

Algorithm:

Initialize an empty K -bin histogram, where K is the number of codewords

Extract local descriptors (e.g. SIFT) from the image

For each local descriptor \mathbf{x}

 Map (Quantize) \mathbf{x} to its closest codeword $\rightarrow \mathbf{c}(\mathbf{x})$

 Increment the histogram bin for $\mathbf{c}(\mathbf{x})$

Return histogram

We can then classify the histogram using a trained classifier, e.g. a support vector machine or k -Nearest Neighbor classifier

Spatial Pyramid

The bag of words representation does not preserve any spatial information

The **spatial pyramid** is one way to incorporate spatial information into the image descriptor.

A spatial pyramid partitions the image and counts codewords within each grid box; this is performed at multiple levels

Spatial Pyramid

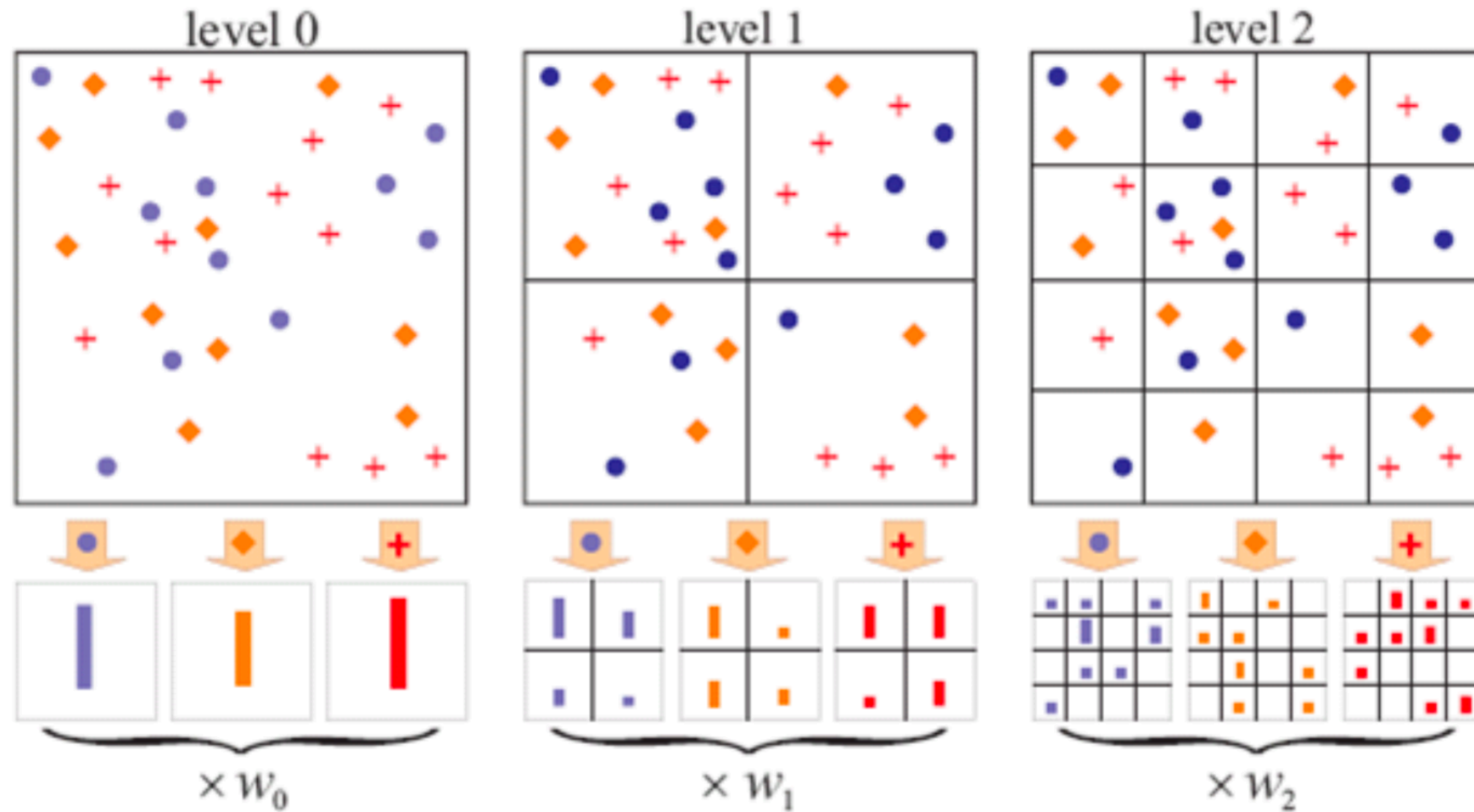


Fig. 16.8 in Forsyth & Ponce (2nd ed.).
Original credit: Lazebnik et al., 2006

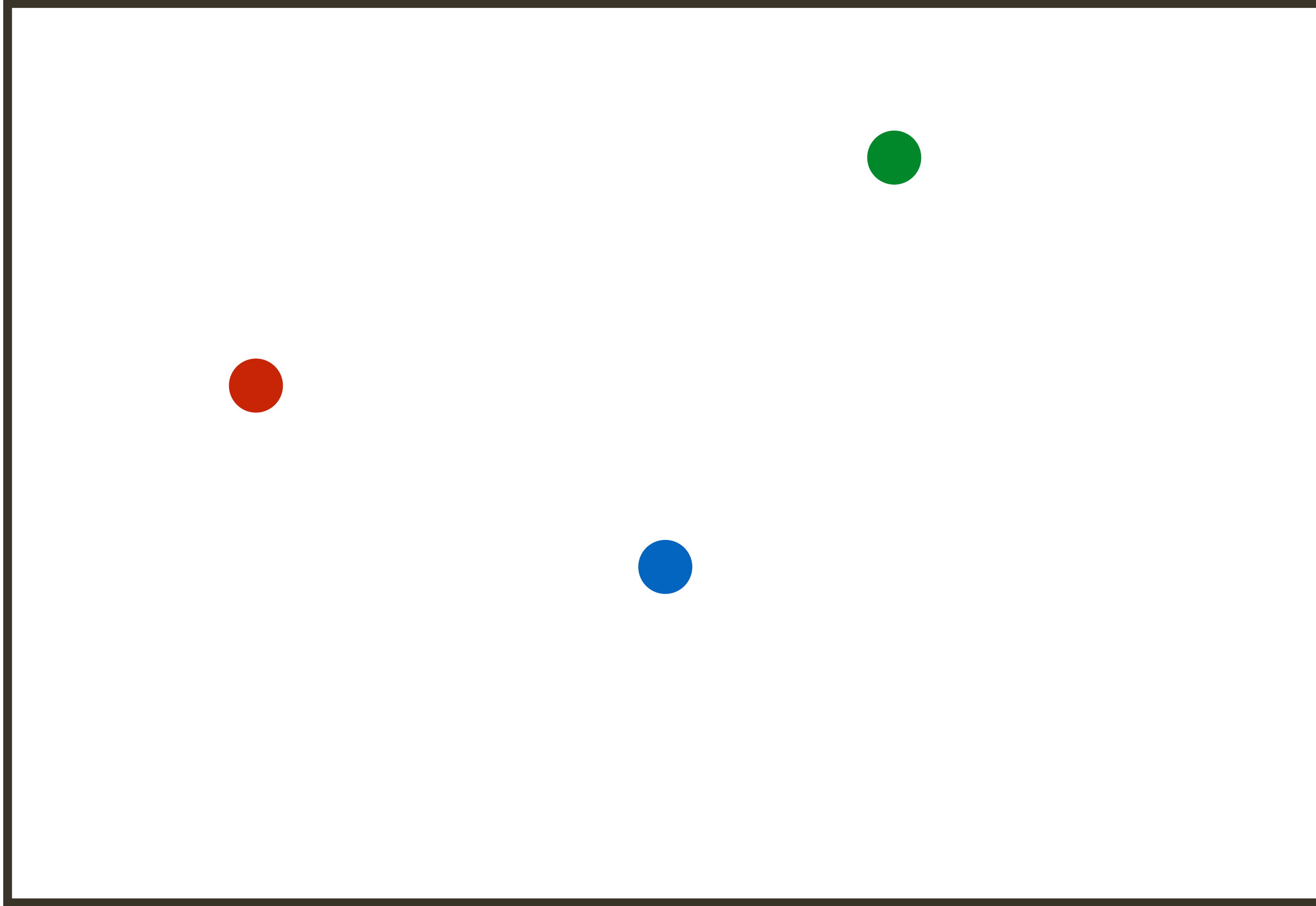
VLAD (Vector of Locally Aggregated Descriptors)

There are more advanced ways to 'count' visual words than incrementing its histogram bin

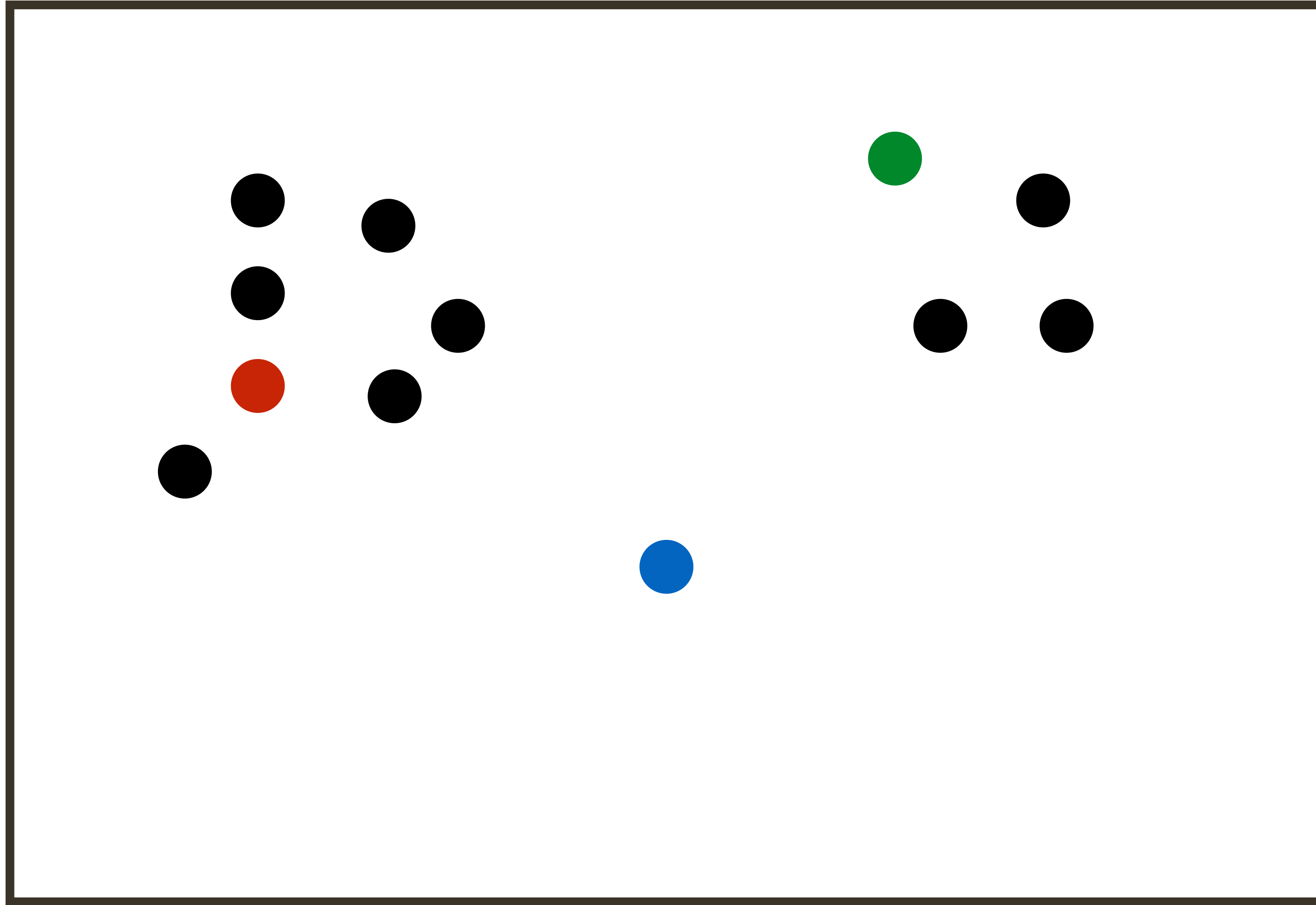
For example, it might be useful to describe how local descriptors are quantized to their visual words

In the VLAD representation, instead of incrementing the histogram bin by one, we increment it by the **residual** vector $\mathbf{x} - \mathbf{c}(\mathbf{x})$

Example: VLAD



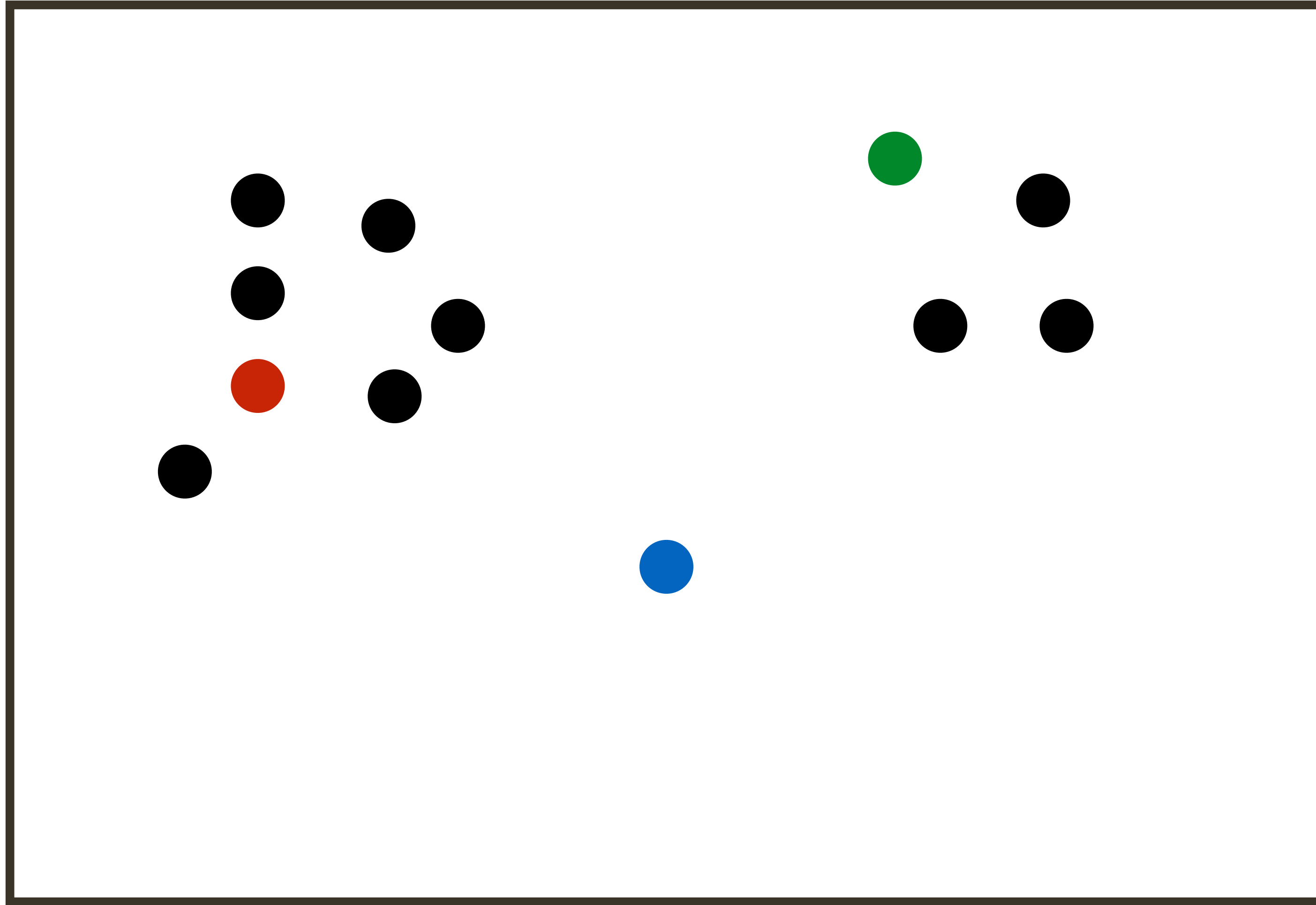
Example: VLAD



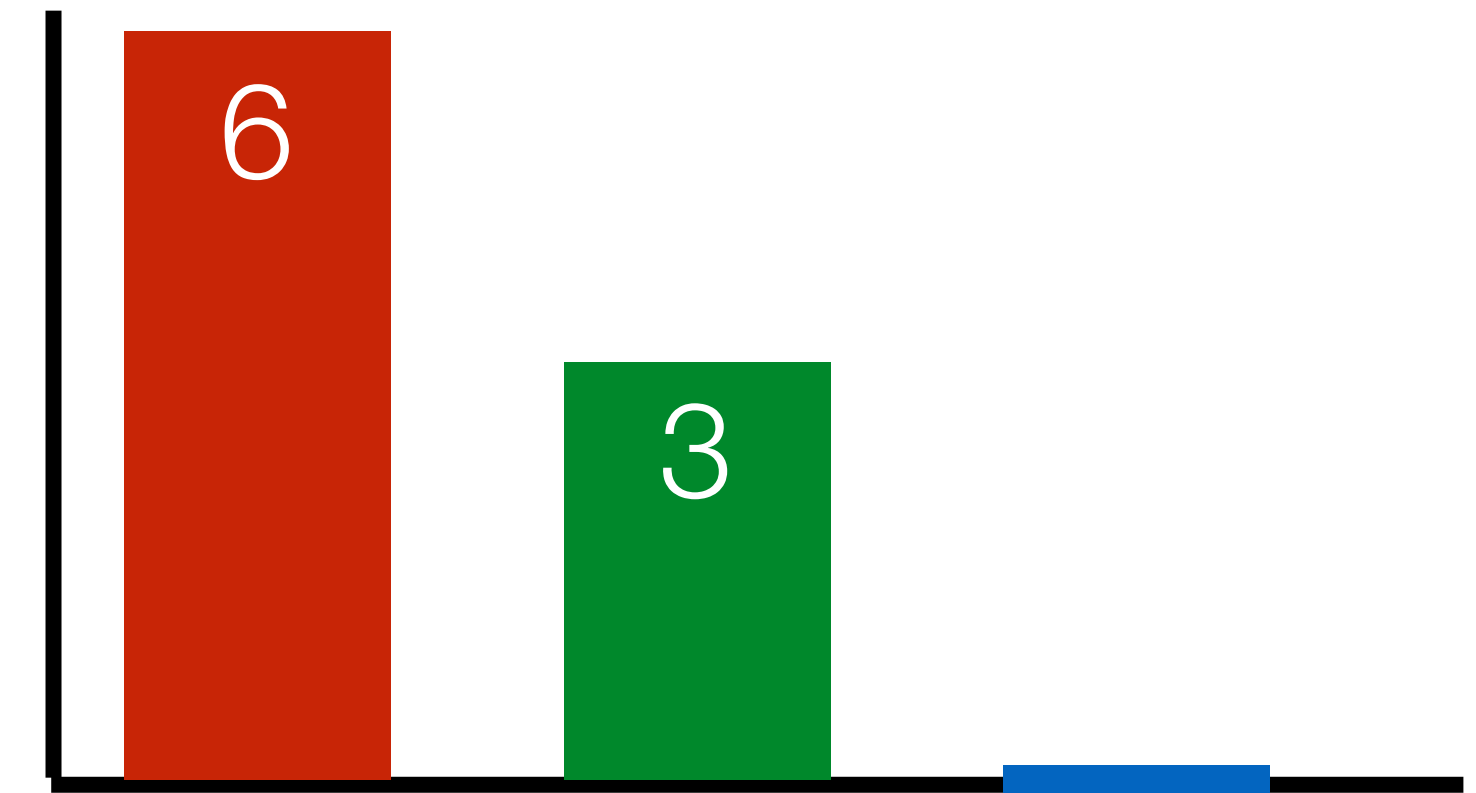
Bag of Word



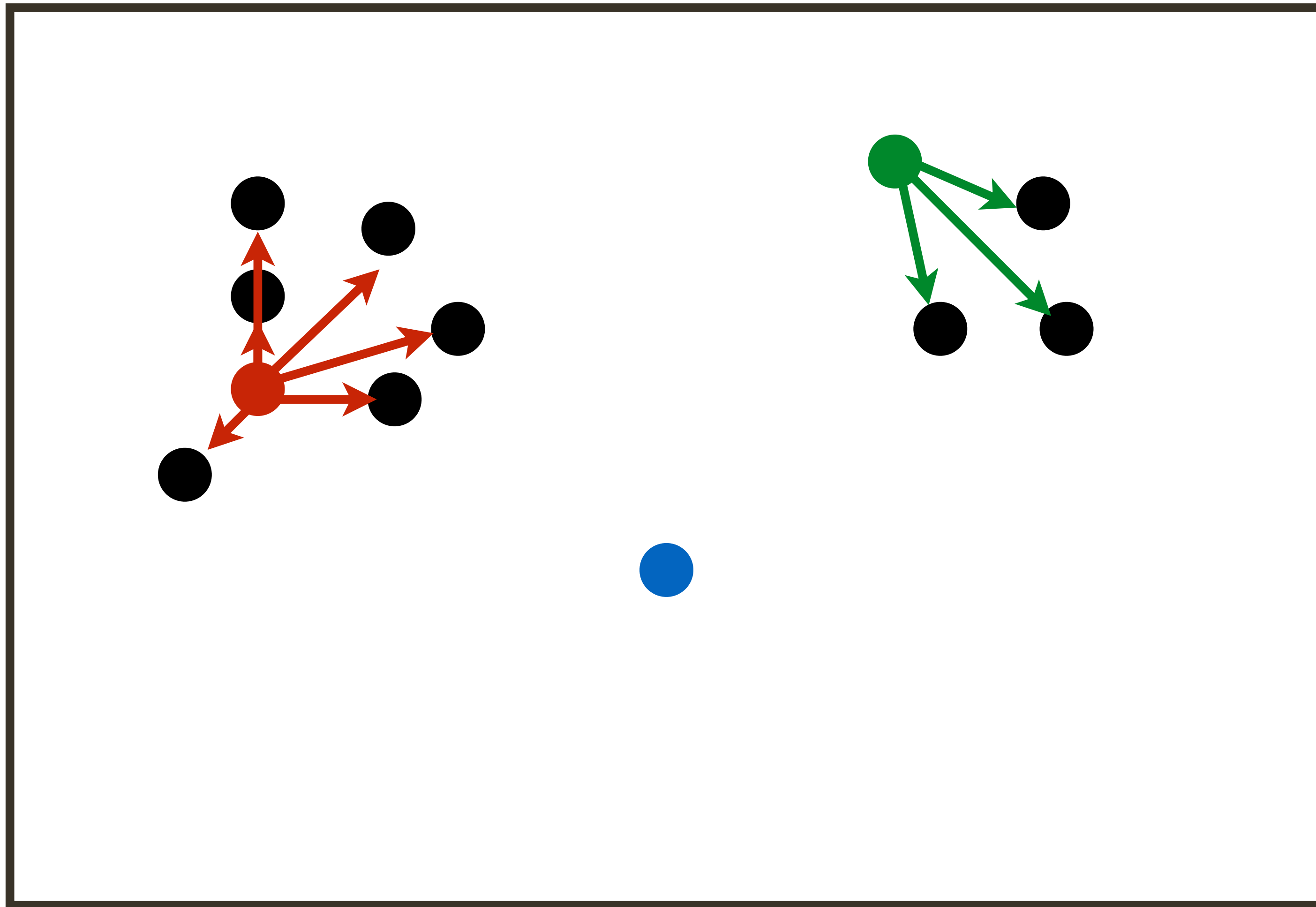
Example: VLAD



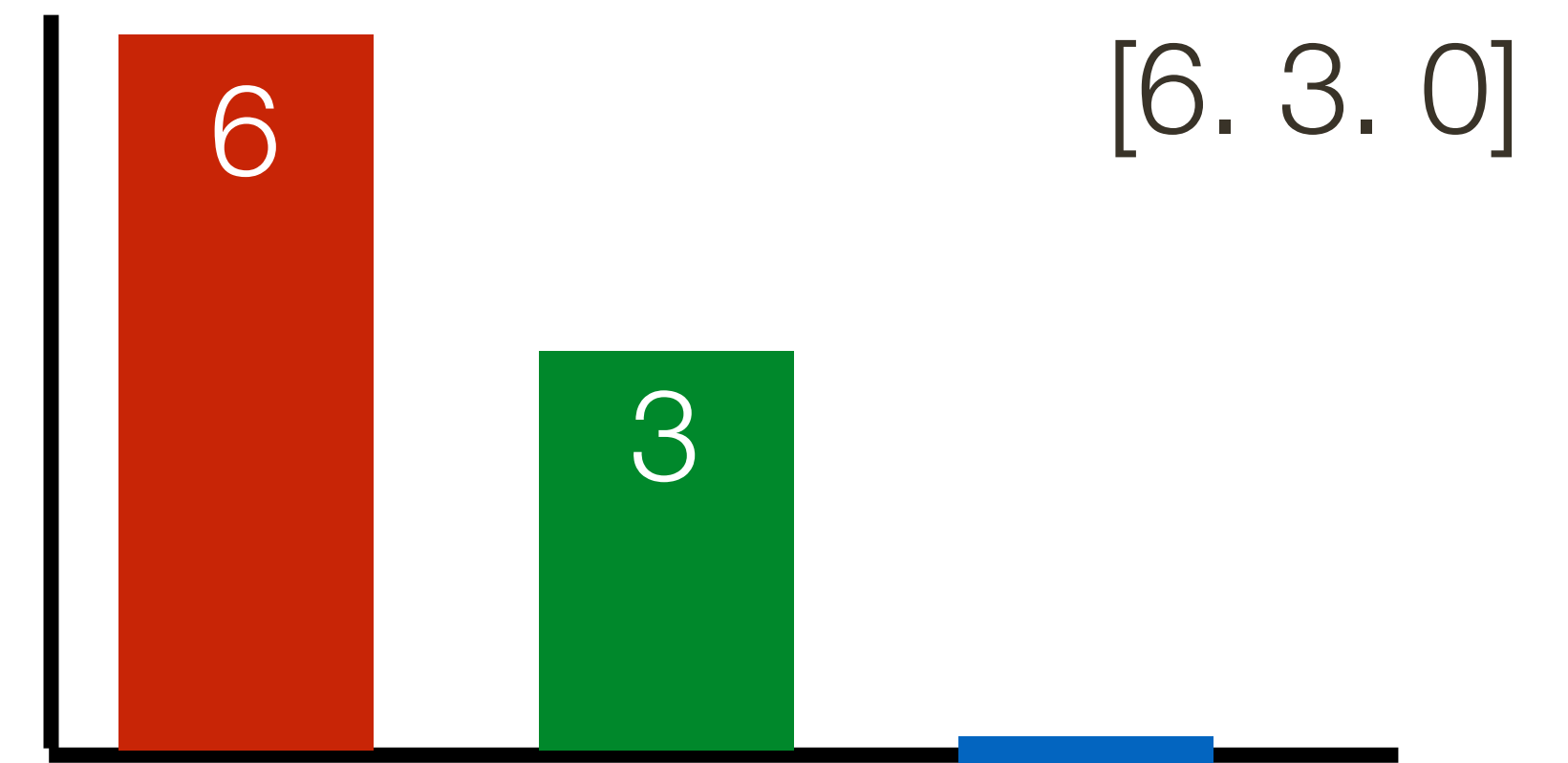
Bag of Word



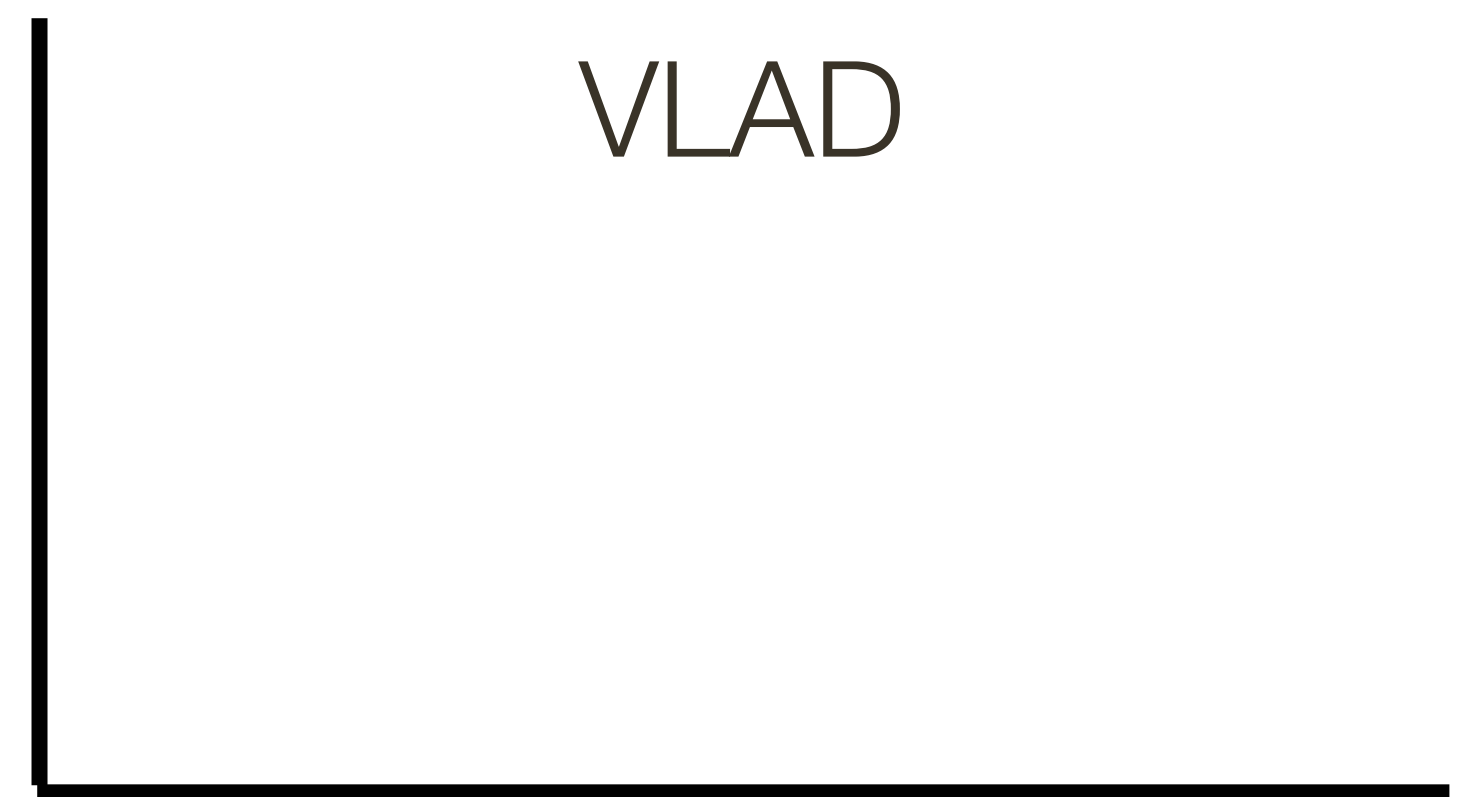
Example: VLAD



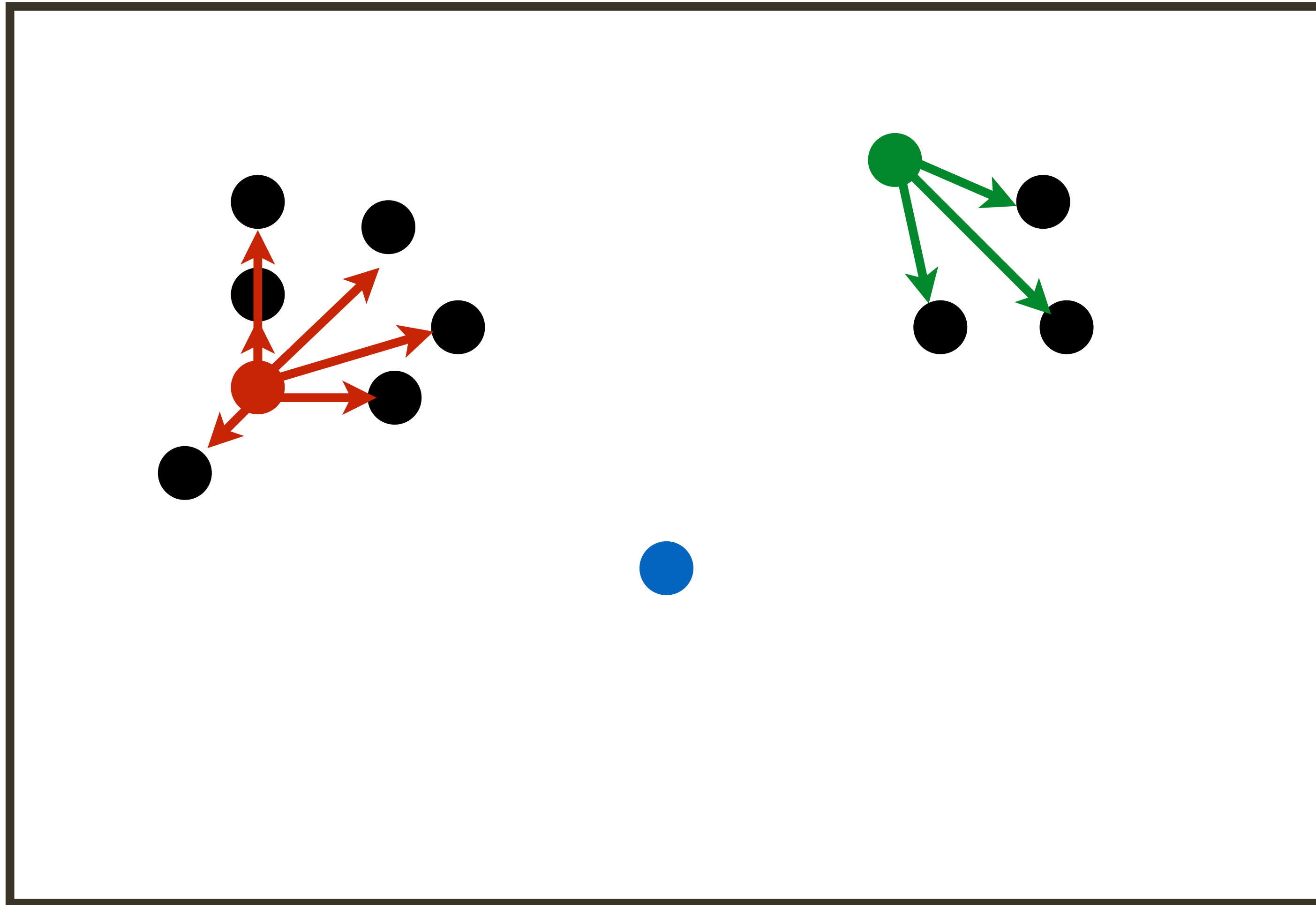
Bag of Word



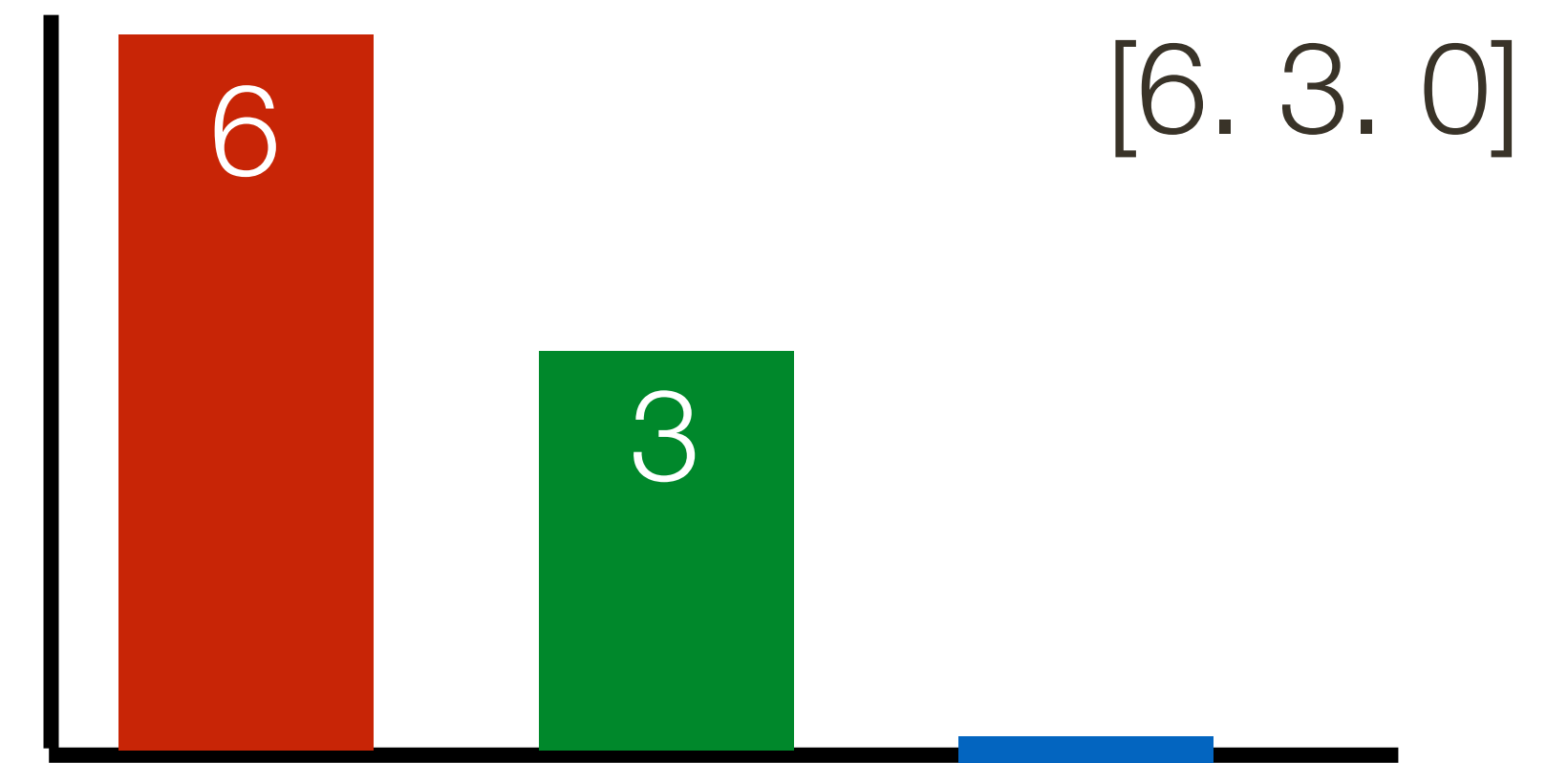
VLAD



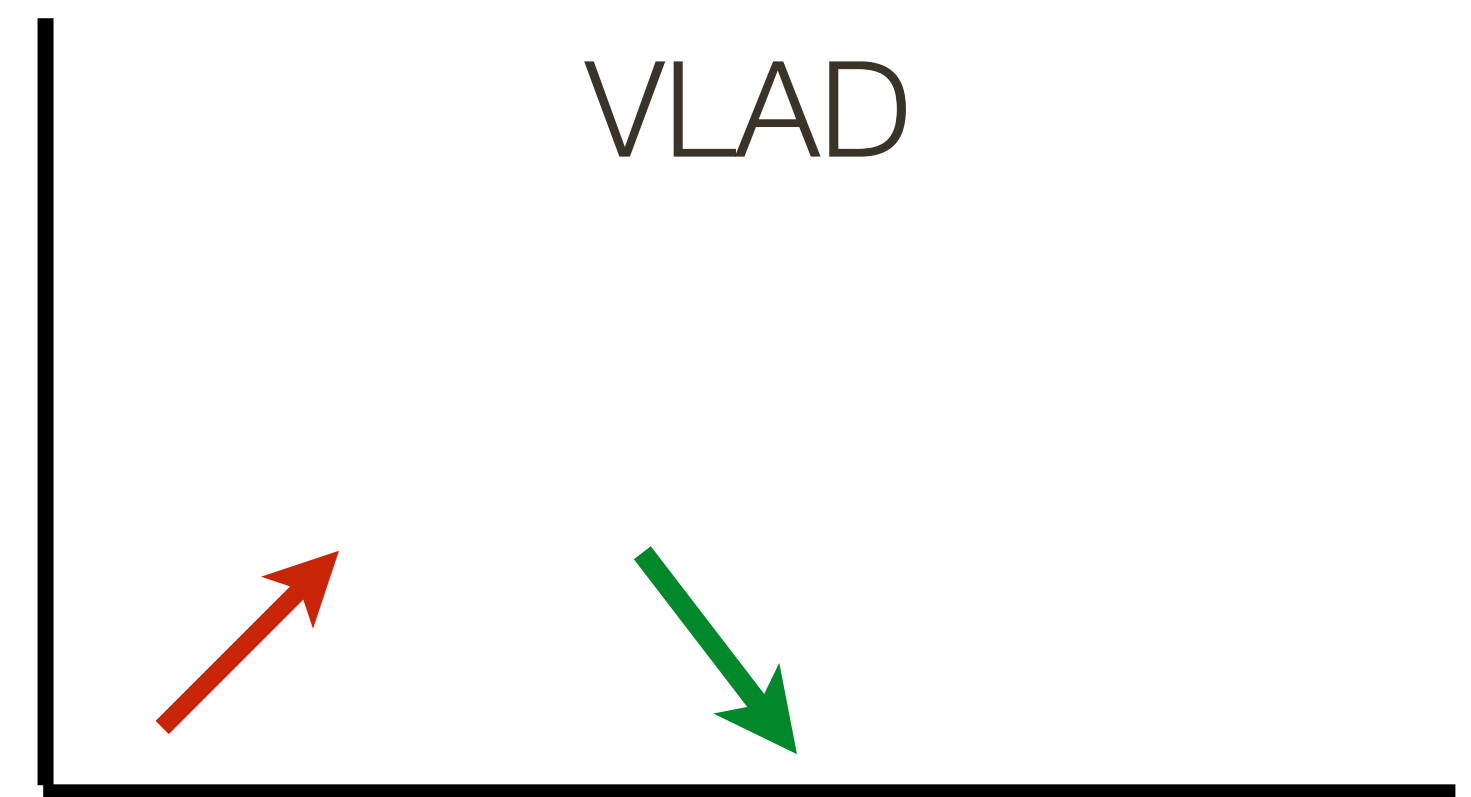
Example: VLAD



Bag of Word



VLAD



VLAD (Vector of Locally Aggregated Descriptors)

The dimensionality of a **VLAD** descriptor is Kd

- K : number of codewords
- d : dimensionality of the local descriptor

VLAD characterizes the distribution of local descriptors with respect to the codewords

Summary

Factors that make image classification hard

— intra-class variation, viewpoint, illumination, clutter, occlusion...

A codebook of **visual words** contains representative local patch descriptors

— can be constructed by clustering local descriptors (e.g. SIFT) in training images

The **bag of words** model accumulates a histogram of occurrences of each visual word

The **spatial pyramid** partitions the image and counts visual words within each grid box; this is repeated at multiple levels