

CPSC 340: Machine Learning and Data Mining

Deep Learning
Summer 2021

In This Lecture

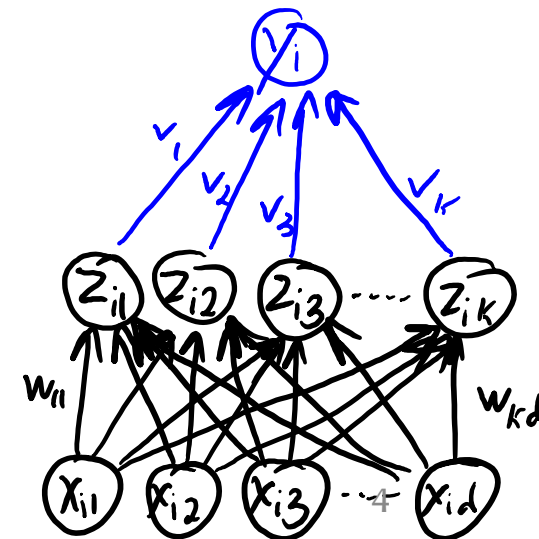
1. Encoder-Predictor Learning
 - aka deep learning
2. Artificial Neural Networks
3. “Biological” Motivations for Deep Learning
4. History of Deep Learning

Part 5: Deep Learning



Supervised Learning Roadmap

- Part 1: “Direct” Supervised Learning.
 - We learned parameters ‘ w ’ based on the original features x_i and target y_i .
- Part 3: Change of Basis.
 - We learned parameters ‘ v ’ based on a change of basis z_i and target y_i .
- Part 4: Latent-Factor Models.
 - We learned parameters ‘ W ’ for basis z_i based on only on features x_i .
 - You can then learn ‘ v ’ based on change of basis z_i and target y_i .
- Part 5: Neural Networks.
 - Jointly learn ‘ W ’ and ‘ v ’ based on x_i and y_i .
 - Learn features z_i that is good for supervised learning.



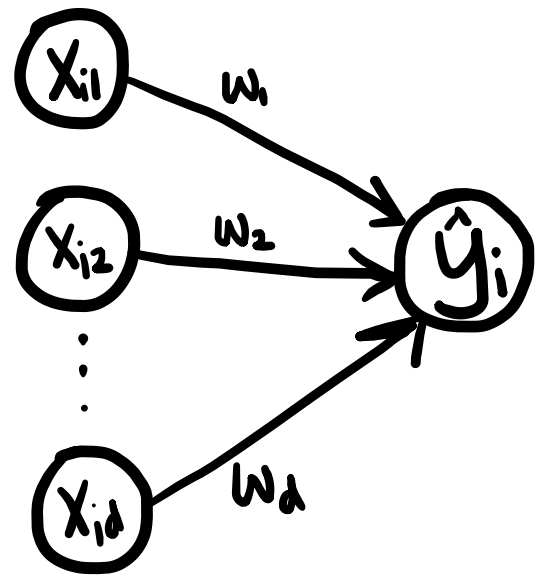
Coming Up Next

ENCODER-PREDICTOR LEARNING

"Graph" View of Matrix Multiplication

$$\hat{y}_i = W^T x_i$$

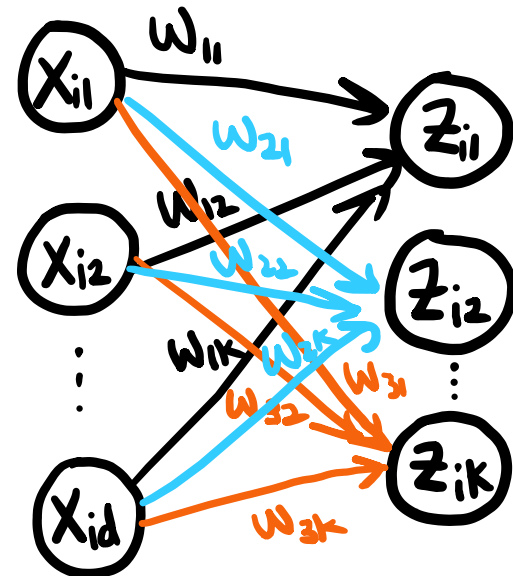
"target" node edge weights "input" nodes



$$\hat{y}_i = [w_1 \ w_2 \ \dots \ w_d] \begin{bmatrix} x_{i1} \\ x_{i2} \\ \vdots \\ x_{id} \end{bmatrix}$$

$$z_i = W x_i$$

"output" nodes edge weights "input" nodes

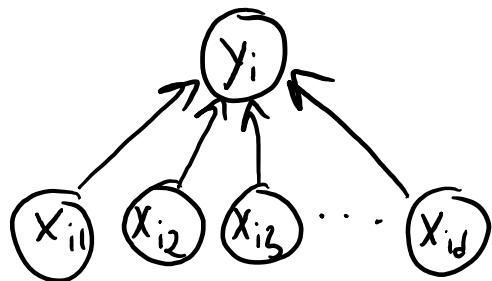


$$\begin{bmatrix} z_{i1} \\ z_{i2} \\ \vdots \\ z_{ik} \end{bmatrix} = \begin{bmatrix} -w_1- \\ -w_2- \\ \vdots \\ -w_k- \end{bmatrix} \begin{bmatrix} x_{i1} \\ x_{i2} \\ \vdots \\ x_{id} \end{bmatrix}$$

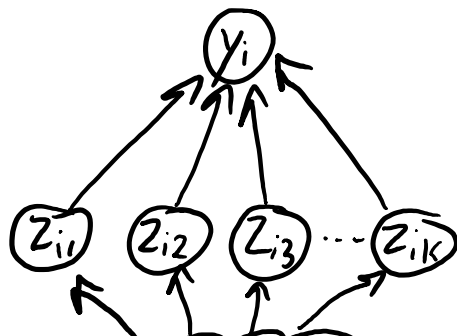
d

A Graphical Summary of CPSC 340 Parts 1-5

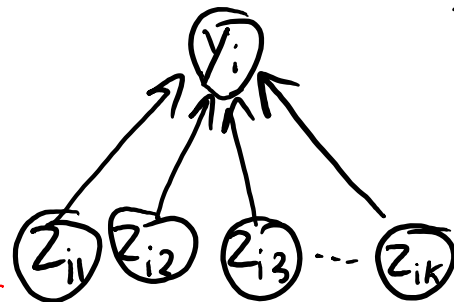
Part 1: "I have features x_i "



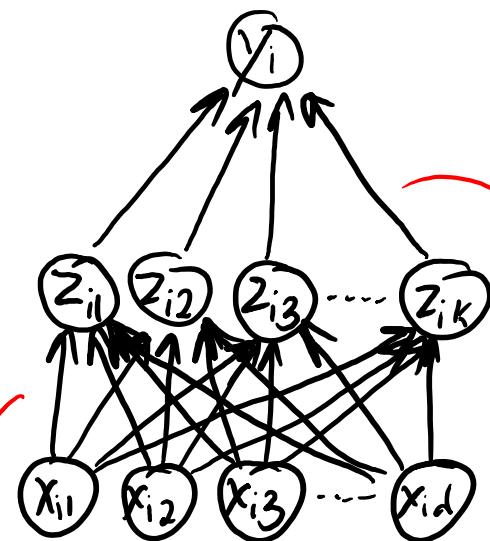
Part 3: change of basis



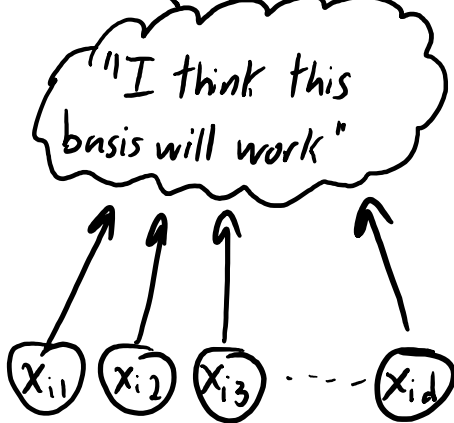
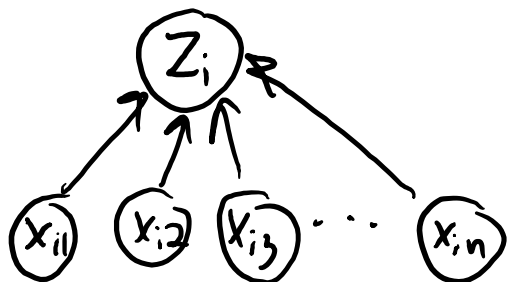
Part 4: basis from latent-factor model



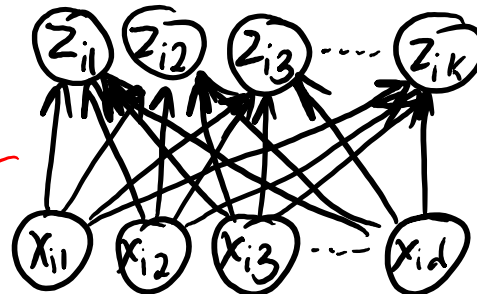
Part 5: Neural networks



Part 2: "What is the group of x_i ?"



"PCA will give me good features"

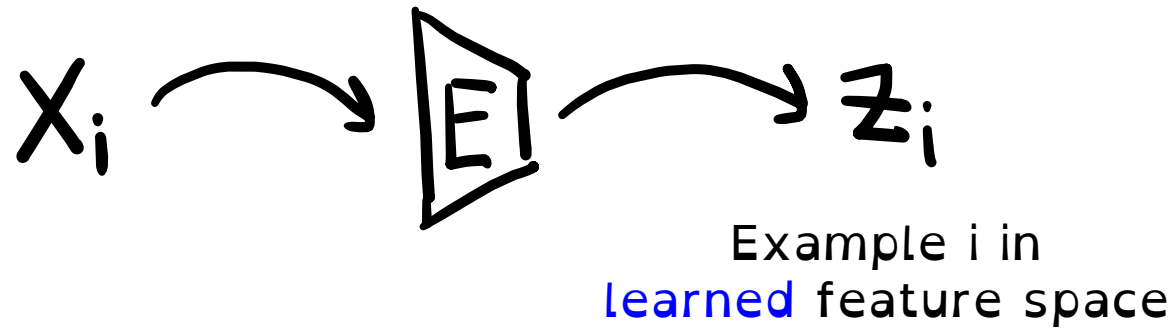
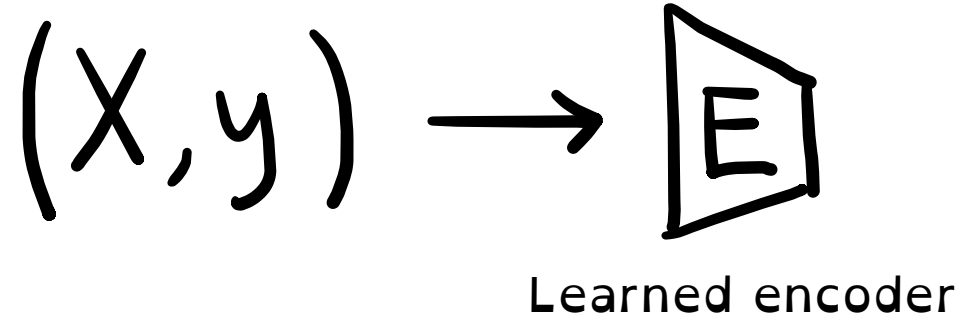


"What are the 'parts' of x_i ?"

Trained separately

Learn features and classifier at the same time.

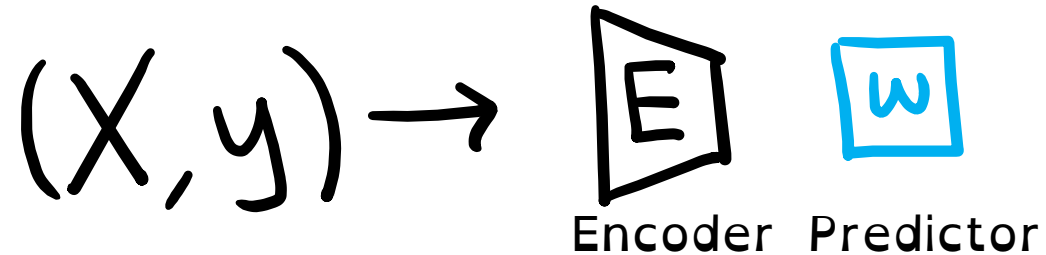
Recall: Encoder Learning



“Encoder-Predictor Learning”

- **Encoder-Predictor Learning** problem:

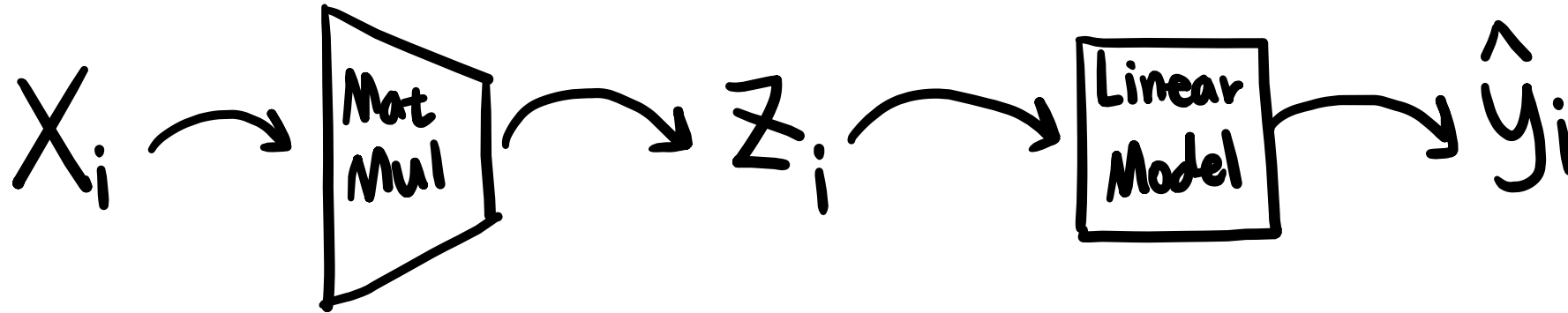
- Input: Labeled examples
- Output: Encoder E and predictor w



- Using learned encoder and predictor:

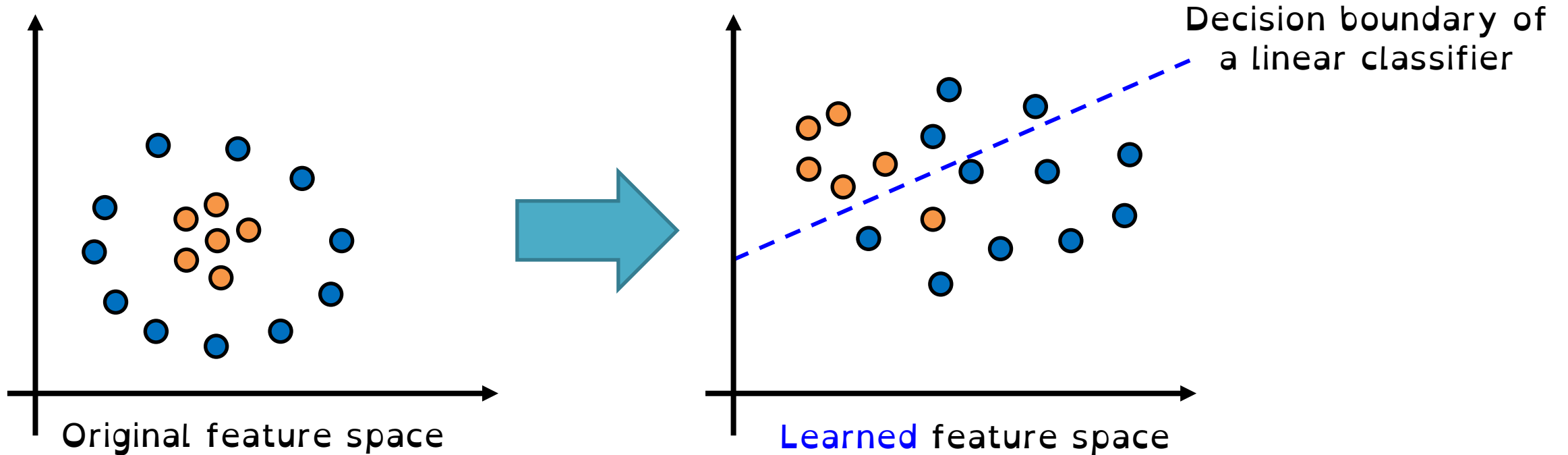


“Artificial Neural Networks”



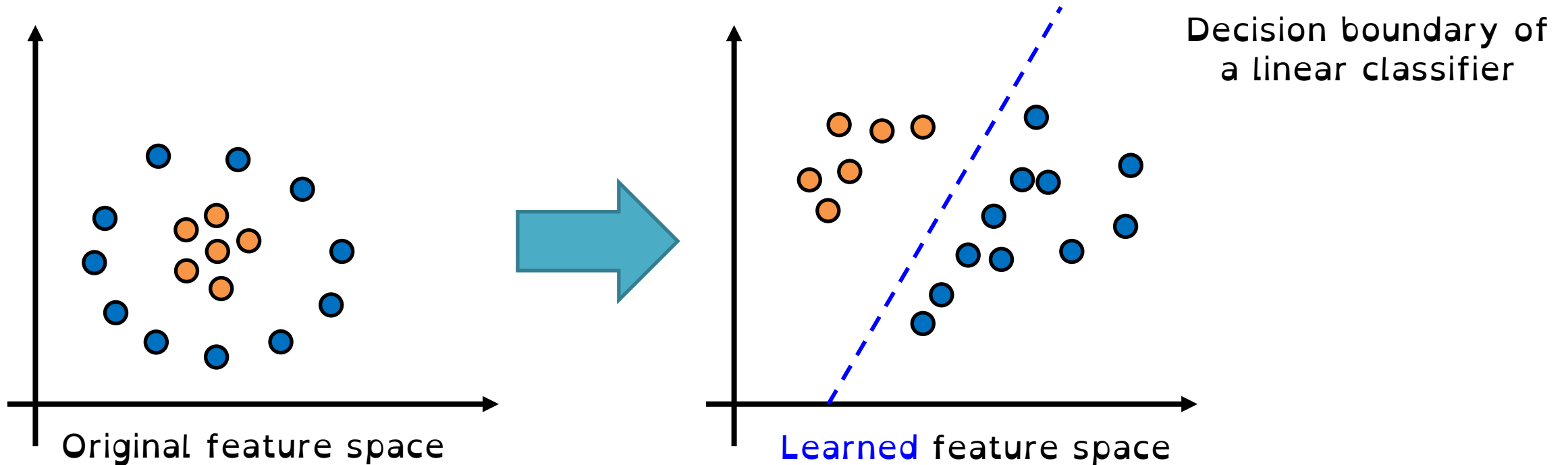
- “**Artificial neural network**” := encoder-predictor model using matrix multiplication for encoder
 - Must use non-linear activations (soon)
 - Usually use linear model as predictor
- “**Deep neural network**” := artificial neural network that uses **more than one matrix multiplication**

Visualizing Encoder-Predictor

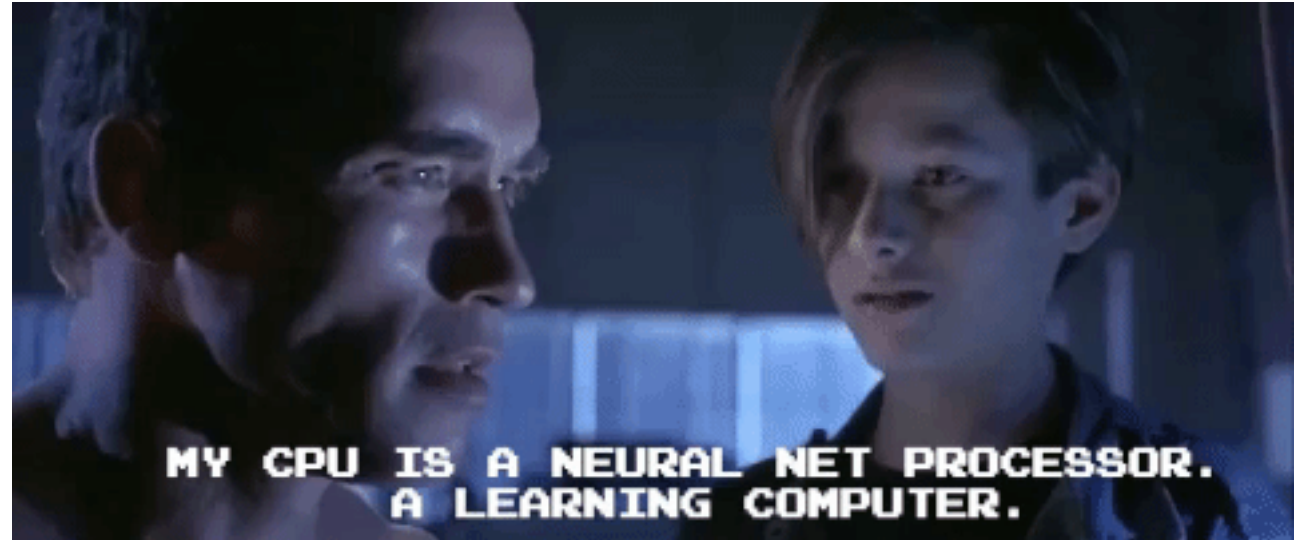


Q: How can we make our model better than this?

Visualizing Encoder-Predictor



- Intuition: **supervised latent factor model**
 - Loss function based on labels
 - Encourage encoder to produce more linearly separable results



Coming Up Next

MORE FORMAL DETAILS ON NEURAL NETWORKS

Notation for Neural Networks (MEMORIZE)

We have our usual supervised learning notation:

$$X = \begin{bmatrix} \text{---} x_1^T \text{---} \\ \text{---} x_2^T \text{---} \\ \vdots \\ \text{---} x_n \text{---} \end{bmatrix} \quad y = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

$n \times d$ $n \times 1$

We have our latent features:

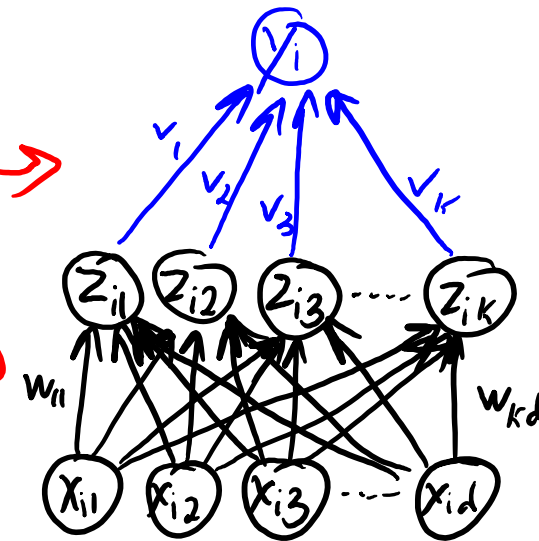
$$Z = \begin{bmatrix} \text{---} z_1^T \text{---} \\ \text{---} z_2^T \text{---} \\ \vdots \\ \text{---} z_n^T \text{---} \end{bmatrix}$$

$n \times k$

We have two sets of parameters:

$$V = \begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_k \end{bmatrix} \quad W = \begin{bmatrix} \text{---} w_1 \text{---} \\ \text{---} w_2 \text{---} \\ \vdots \\ \text{---} w_k \text{---} \end{bmatrix}$$

$k \times 1$ $k \times d$



Linear-Linear Neural Net

- Obvious choice: **linear latent-factor** encoder with **linear regression** predictor

Use features from latent-factor model: $z_i = Wx_i$

Make predictions using a linear model: $y_i = v^T z_i$

- We want to train 'W' and 'v' jointly, so we could minimize:

$$f(W, v) = \frac{1}{2} \sum_{i=1}^n \underbrace{(v^T z_i - y_i)^2}_{\text{linear regression with } z_i \text{ as features}} = \frac{1}{2} \sum_{i=1}^n \underbrace{(v^T (Wx_i) - y_i)^2}_{z_i \text{ come from latent-factor model}}$$

Q: What can go wrong with this?

Linear-Linear Neural Net

- Obvious choice: **linear latent-factor** encoder with **linear regression** predictor

Use features from latent-factor model: $z_i = Wx_i$

Make predictions using a linear model: $y_i = v^T z_i$

- We want to **train 'W' and 'v' jointly**, so we could minimize:

$$f(W, v) = \frac{1}{2} \sum_{i=1}^n \underbrace{(v^T z_i - y_i)^2}_{\text{linear regression with } z_i \text{ as features}} = \frac{1}{2} \sum_{i=1}^n \underbrace{(v^T (Wx_i) - y_i)^2}_{z_i \text{ come from latent-factor model}}$$

- **This is just a linear model:**

$$y_i = v^T z_i = v^T (Wx_i) = \overbrace{(v^T W)}^{1 \times d} x_i = \underbrace{w^T}_{\text{some vector 'w'}} x_i$$

Introducing Non-Linearity

- To increase flexibility, something needs to be **non-linear**.
- Typical choice: **transform z_i by non-linear function 'h'**.

$$z_i = Wx_i \quad y_i = v^T h(z_i)$$

- Here the function 'h' transforms 'k' inputs to 'k' outputs.
- Common choice for 'h': applying **sigmoid** function element-wise:

$$h(z_{ic}) = \frac{1}{1 + \exp(-z_{ic})}$$

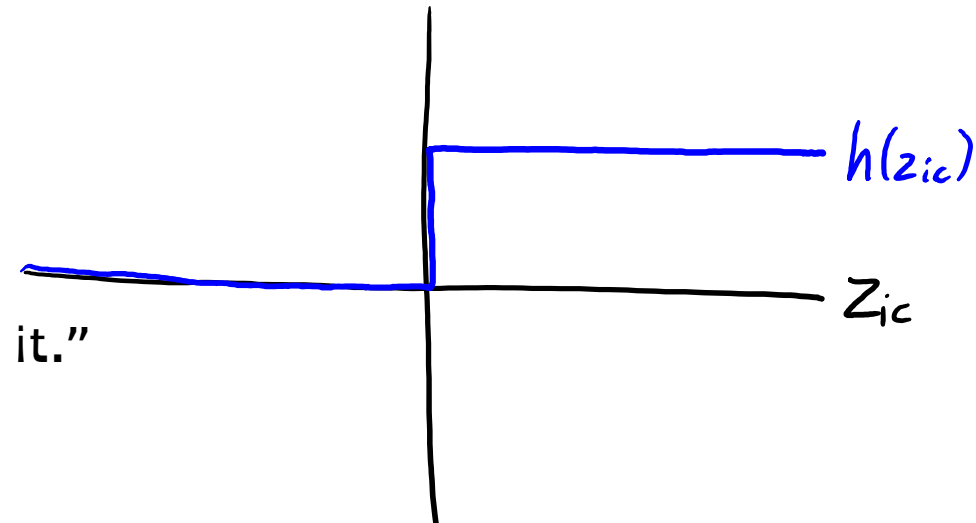
- So this takes the z_{ic} in $(-\infty, \infty)$ and maps it to _____.

Why Sigmoid?

- Consider setting 'h' to define **binary features** z_i using:

$$h(z_{ic}) = \begin{cases} 1 & \text{if } z_{ic} \geq 0 \\ 0 & \text{if } z_{ic} < 0 \end{cases}$$

- Each $h(z_i)$ can be viewed as binary feature.
 - “You either have this ‘part’ or you don’t have it.”
- We can make 2^k objects by all the possible “part combinations”.



Motivation: Pixels vs. Parts

- We could represent other digits as different combinations of “parts”:

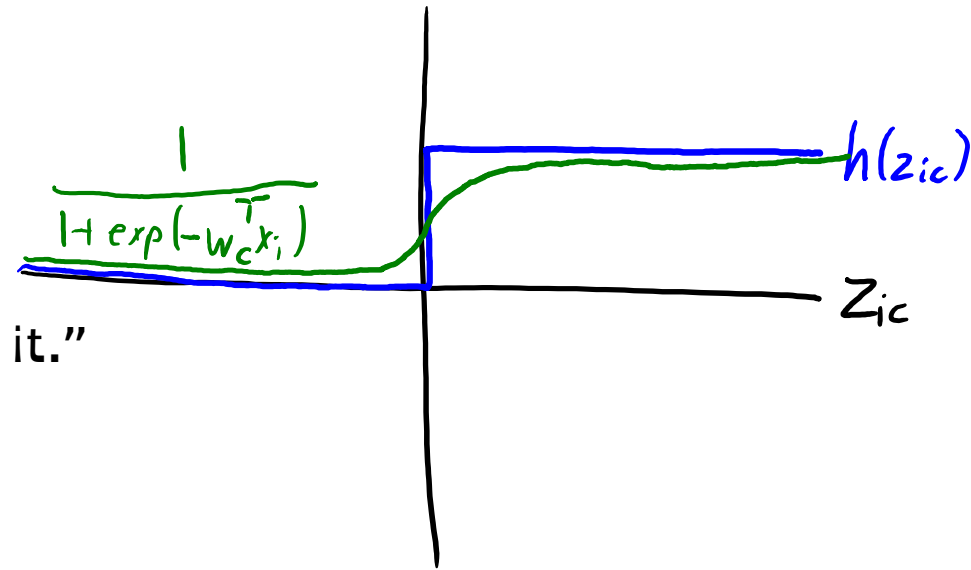
	=	+		+		+		+		+		+		+		+	
	=	+		+		+		+		+		+		+		+	
	=	+		+		+		+		+		+		+		+	

Why Sigmoid?

- Consider setting 'h' to define **binary features** z_i using:

$$h(z_{ic}) = \begin{cases} 1 & \text{if } z_{ic} \geq 0 \\ 0 & \text{if } z_{ic} < 0 \end{cases}$$

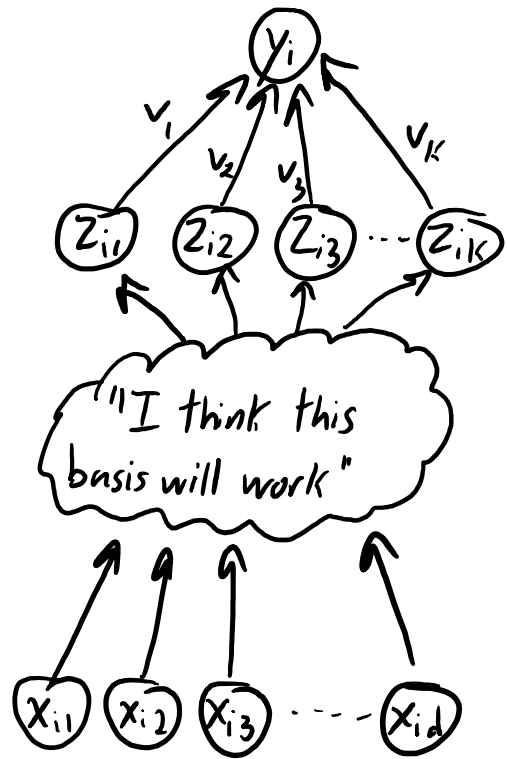
- Each $h(z_i)$ can be viewed as binary feature.
 - “You either have this ‘part’ or you don’t have it.”



- But this is hard to optimize (**non-differentiable, discontinuous**).
- **Sigmoid is a smooth approximation** to these binary features.
 - Non-parametric version is a **universal approximator**:
 - If ‘k’ grows appropriately with ‘n’, can model any continuous function.

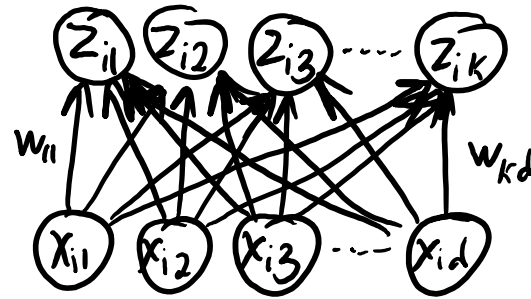
Supervised Learning Roadmap

Hand-engineered features:

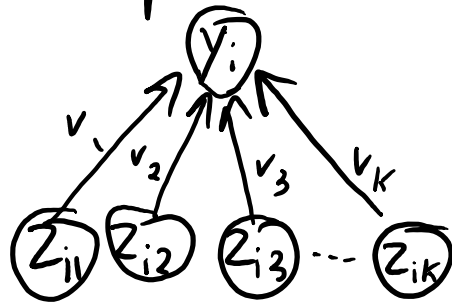


Requires domain knowledge and can be time-consuming

Learn a latent-factor model:

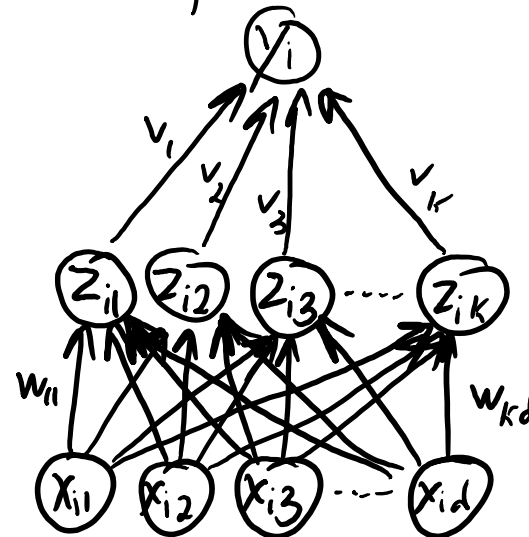


Use latent features in supervised model:



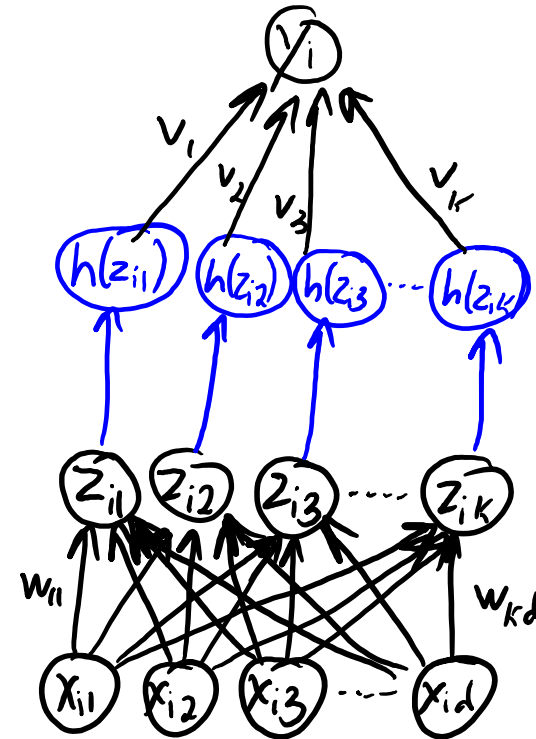
Good representation of x_i might be bad for predicting y_i

Learn ' v ' and ' W ' together:



But still gives a linear model.

Neural network:



Extra non-linear transformation h !

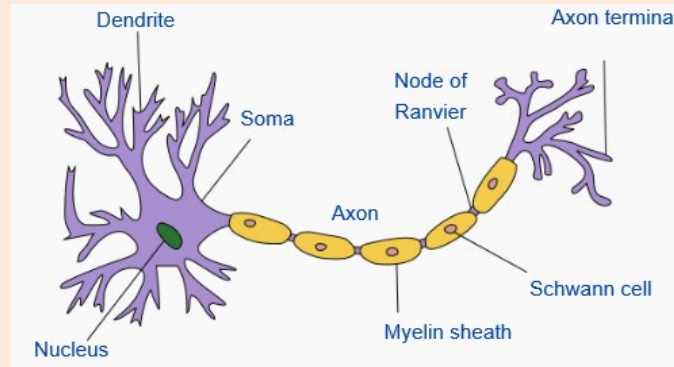


Coming Up Next

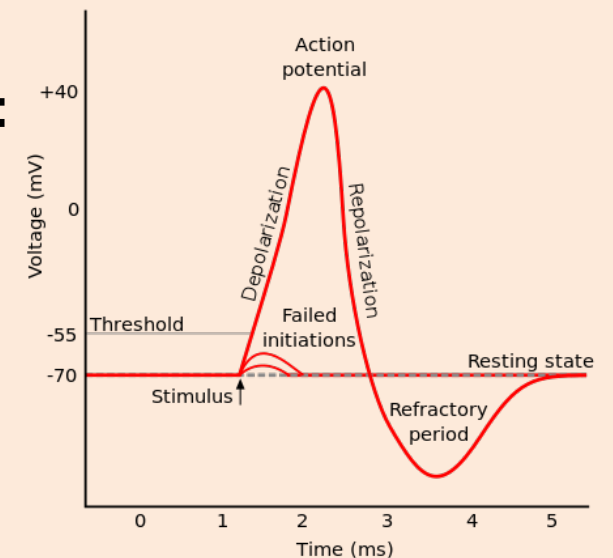
(SUPPOSEDLY) BIOLOGICAL MOTIVATION FOR ARTIFICIAL NEURAL NETWORKS

Why “Neural Network”?

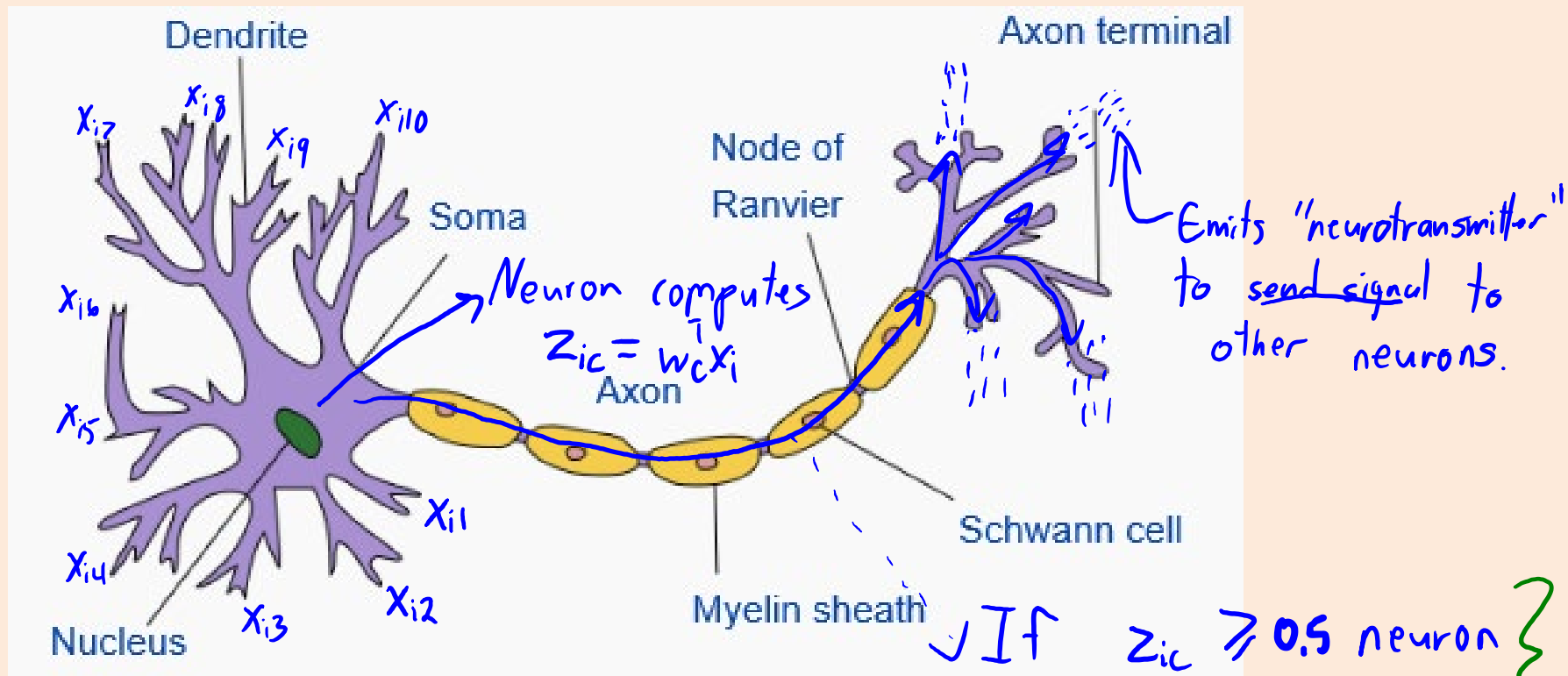
- Cartoon of “typical” neuron:



- Neuron has many “dendrites”, which take an input signal.
- Neuron has a single “axon”, which sends an output signal.
- With the right input to dendrites:
 - “Action potential” along axon (like a binary signal):

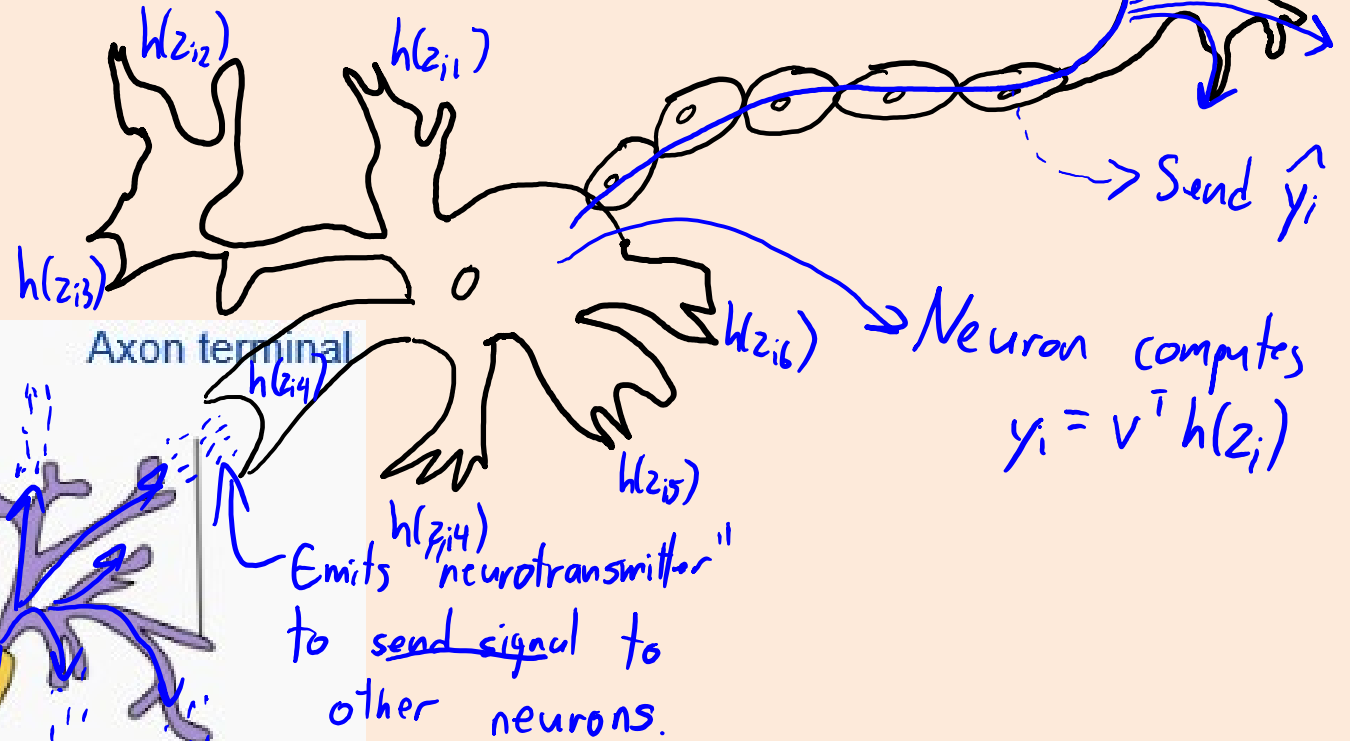
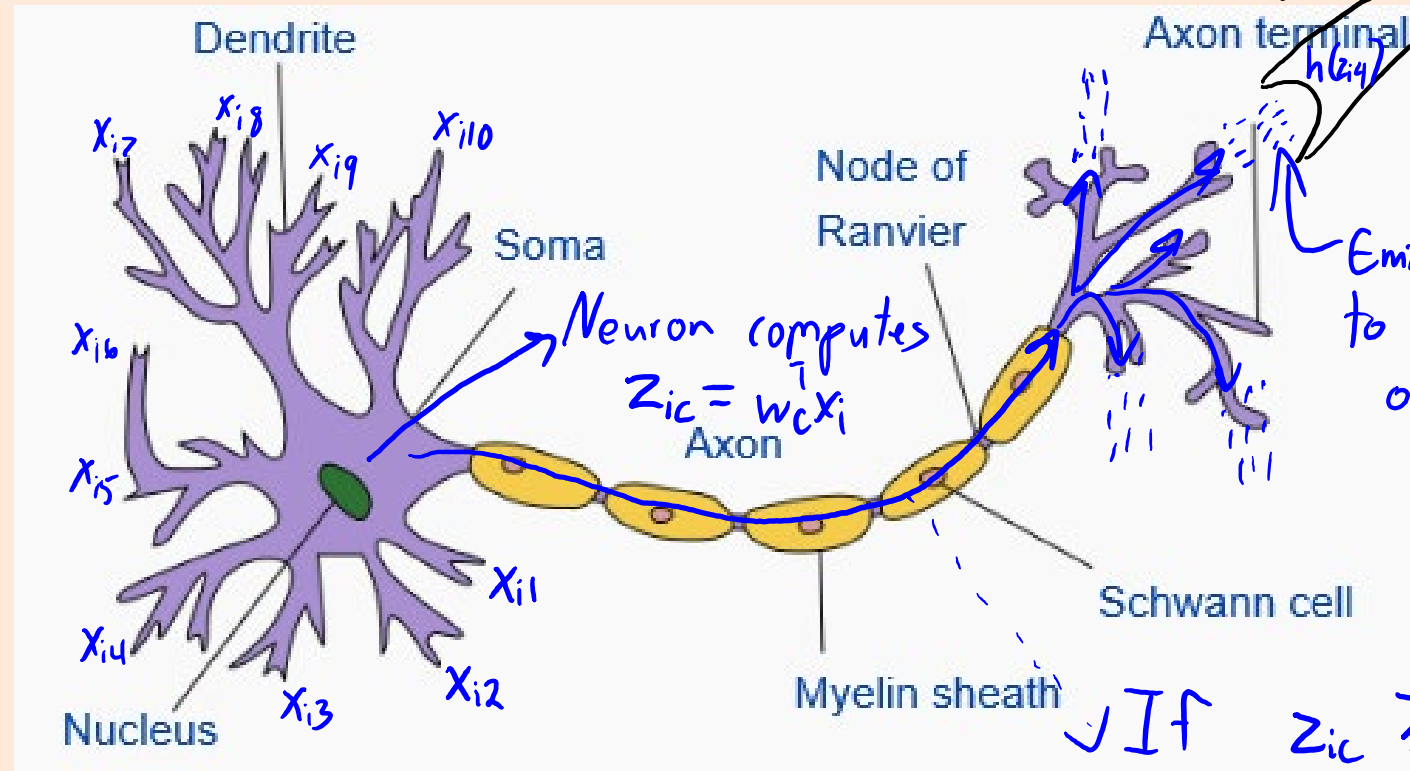


Why "Neural Network"?



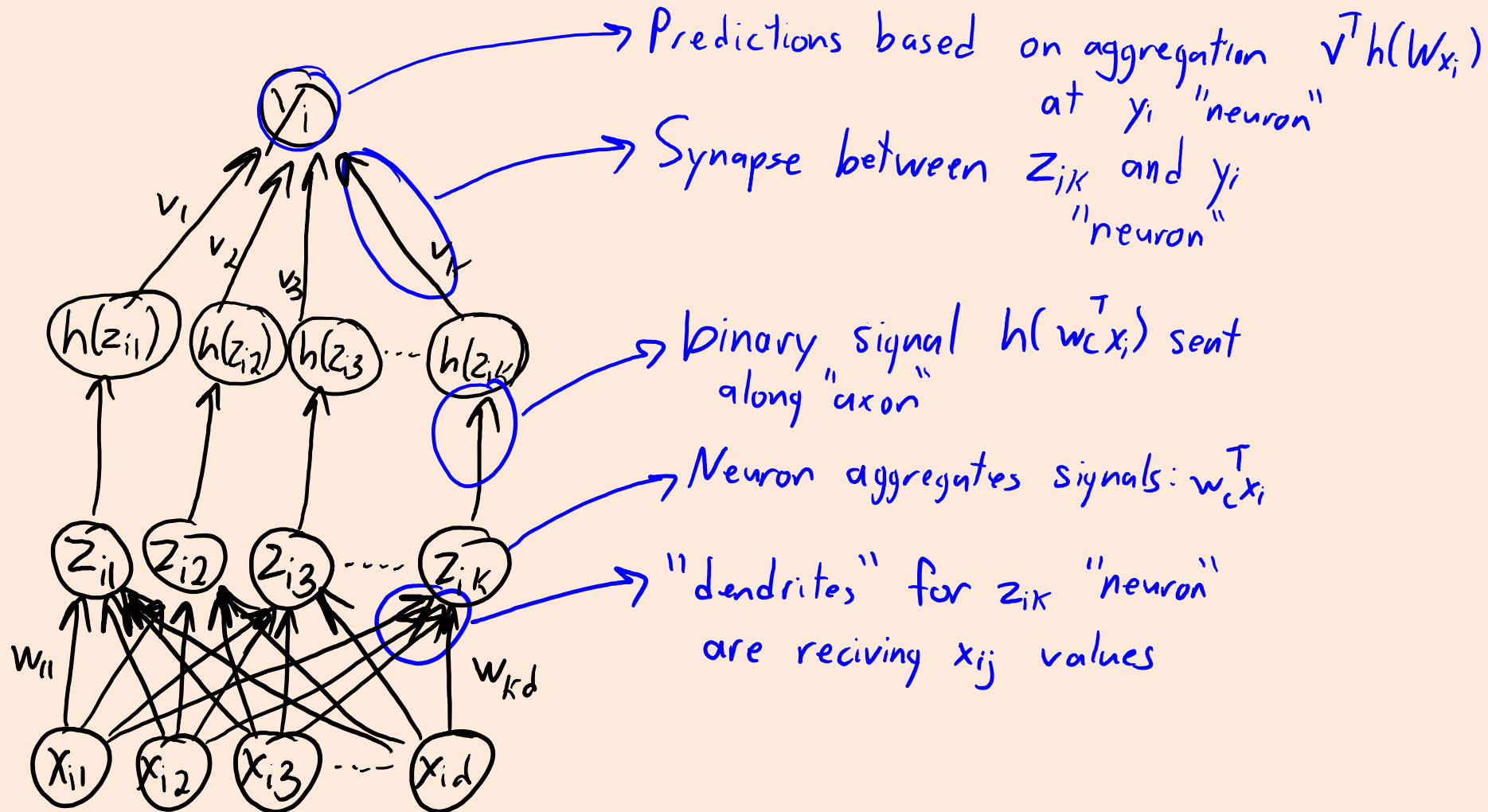
If $z_{ic} \geq 0.5$ neuron } We approximate binary
Sends signal along axon. } signal with $\frac{1}{1 + \exp(-2z_{ic})}$

Why "Neural Network"?



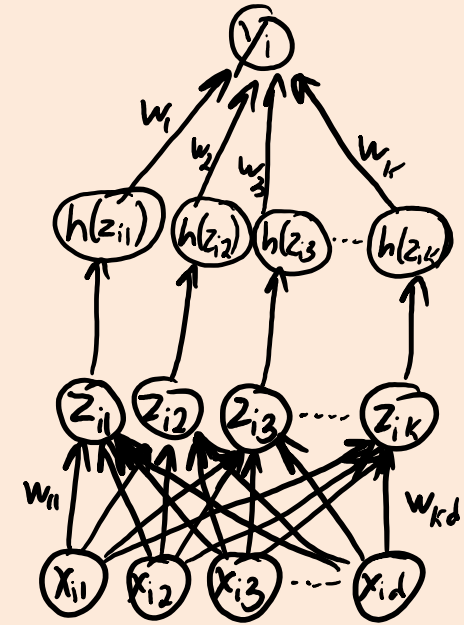
If $z_{ic} \geq 0.5$ neuron } We approximate binary
 Sends signal along axon. } signal with $\frac{1}{1 + \exp(-2z_{ic})}$

Why "Neural Network"?



“Artificial” Neural Nets vs. “Real” Networks Nets


- Artificial neural network:
 - x_i is measurement of the world.
 - z_i is internal representation of world.
 - y_i is output of neuron for classification/regression.
- Real neural networks are more complicated:
 - **Timing** of action potentials seems to be important.
 - “Rate coding”: frequency of action potentials simulates continuous output.
 - **Sparsity** of action potentials.
 - How much computation is done **inside neuron**?
 - Brain is highly **organized** (e.g., substructures and cortical columns).
 - Connection **structure changes**.
 - **Different types** of neurotransmitters.





Coming Up Next

WHAT IS DEEP LEARNING?



 **Nam Hee Gordon Kim** @NamHeeGordonKim · May 19, 2020 ...
Replying to @NamHeeGordonKim
The word "deep" is ambiguous. In DL, it's meant to describe the multilayered neural network architectures (I don't like the term neural network either, but that's for another time).

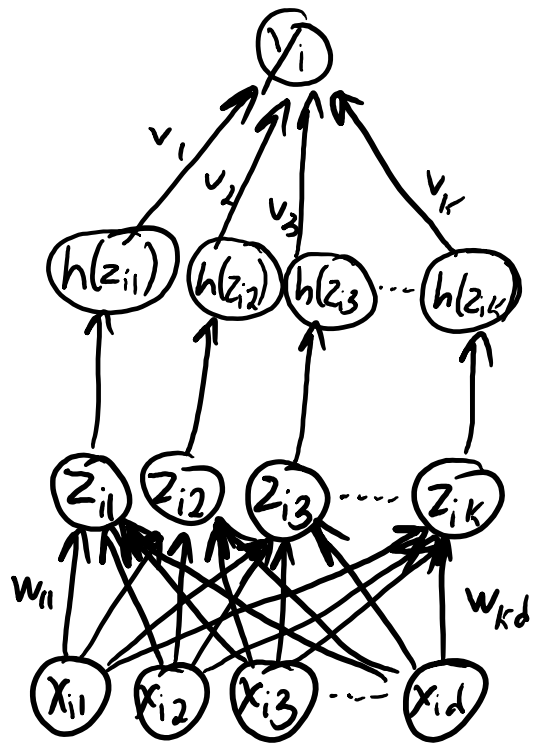
 **Nam Hee Gordon Kim** @NamHeeGordonKim · May 19, 2020 ...
However, in so many cases e.g. graphics, "deep" conveys full-throttled execution of programs. Moreover, neural networks don't even have to be deep or even multilayered at all do retain their universal approximator property.

 **Nam Hee Gordon Kim** @NamHeeGordonKim · May 19, 2020 ...
If you asked me what we should call it instead, I'd call it differentiable matrix learning. For its applications, instead of throwing the word "deep" about everywhere, I'd use the terms "learned mappings" and "function approximations".



Deep Learning

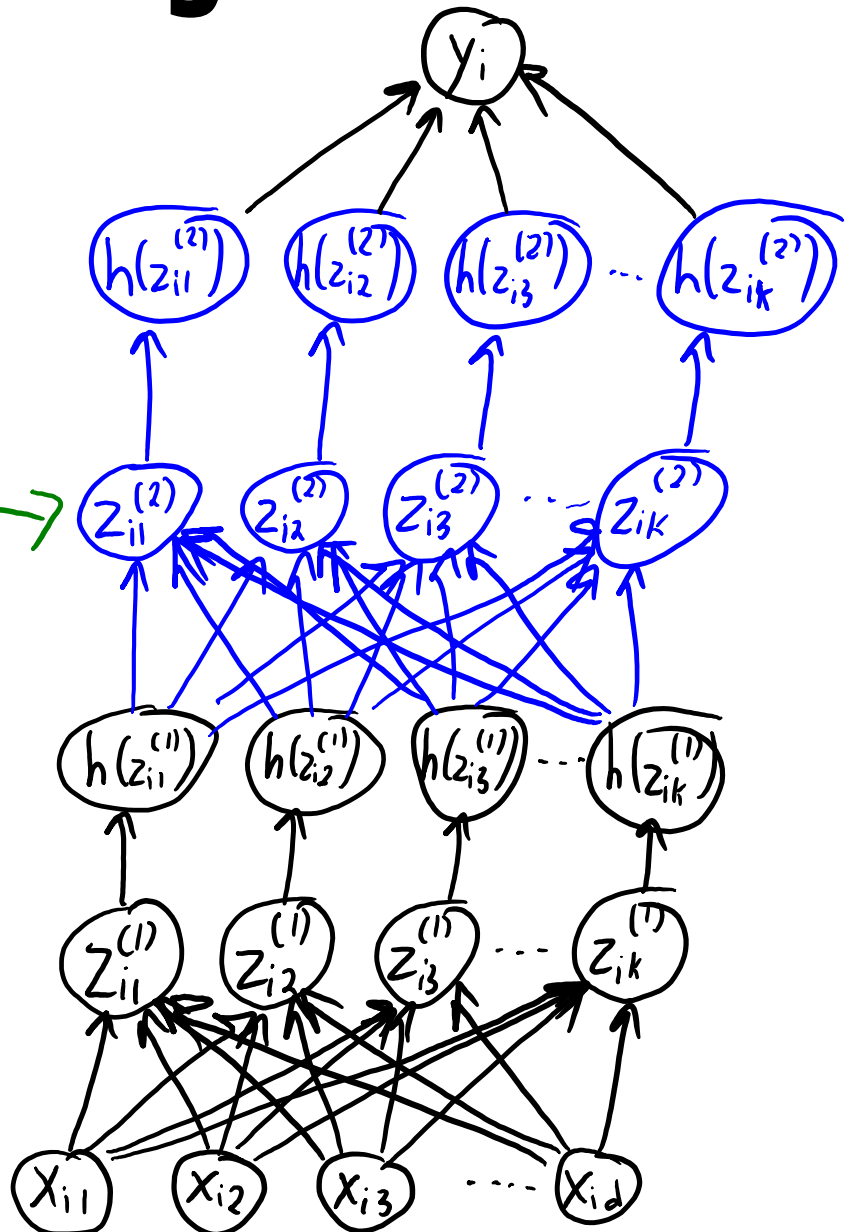
Neural network:



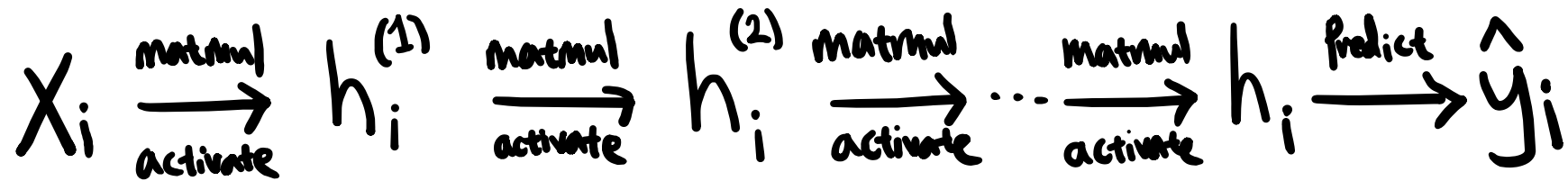
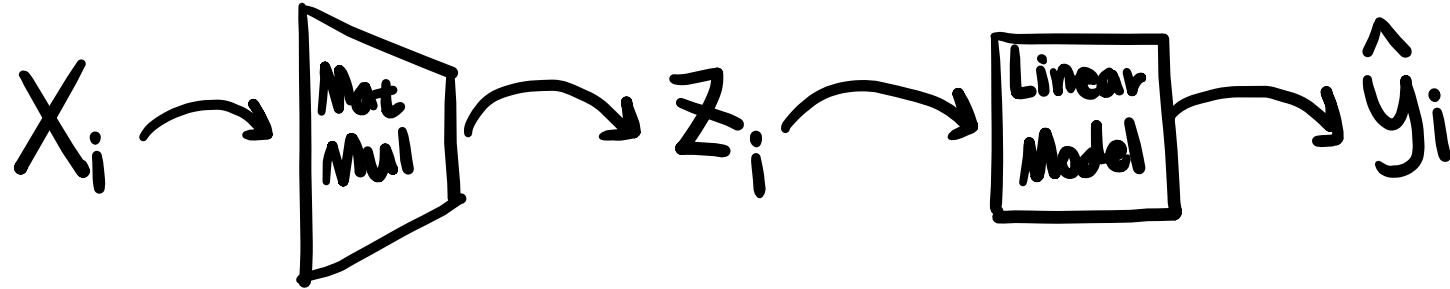
Deep learning:

Second "layer" of latent features

You can add more "layers" to go "deeper"



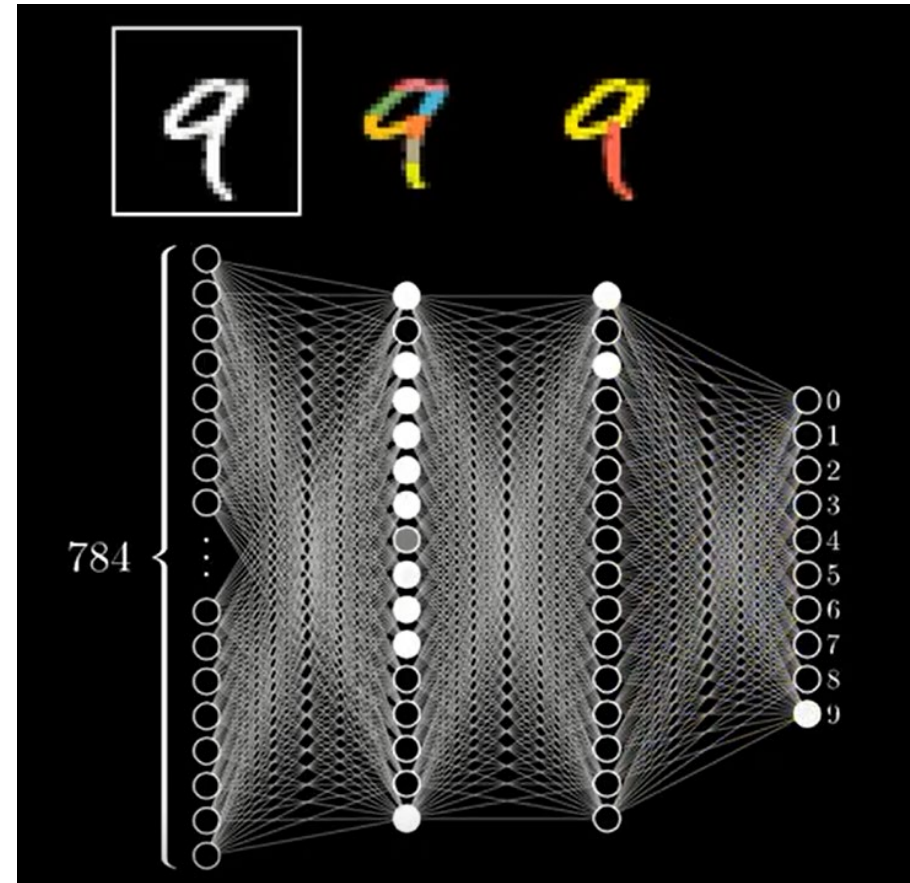
Encoder-Predictor View of Deep Learning



- Compose multiple non-linear encoders
- Overall idea is still the same:
 - Train encoder and predictor at the same time
 - (we have a “bigger” encoder now)

“Hierarchies of Parts” Motivation for Deep Learning

- Each “neuron” might recognize a “part” of digit.
 - “Deeper” neurons might recognize combinations of parts.
 - Represent complex objects as hierarchical combinations of re-useable parts (a simple “grammar”).
- Watch the full video here:
 - <https://www.youtube.com/watch?v=aircAruvnKk>
- Theory:
 - 1 big-enough hidden layer already gives universal approximation.
 - But some functions require exponentially-fewer parameters to approximate with more layers (can fight curse of dimensionality).



Deep Learning

Linear model:

$$\hat{y}_i = w^T x_i$$

Neural network with 1 hidden layer:

$$\hat{y}_i = v^T h(Wx_i)$$

$\underbrace{\hspace{2em}}_{z_i}$

Neural network with 2 hidden layers:

$$\hat{y}_i = v^T h(W^{(2)} h(W^{(1)} x_i))$$

$\underbrace{\hspace{2em}}_{z_i^{(1)}} \underbrace{\hspace{2em}}_{z_i^{(2)}}$

Neural network with 3 hidden layers:

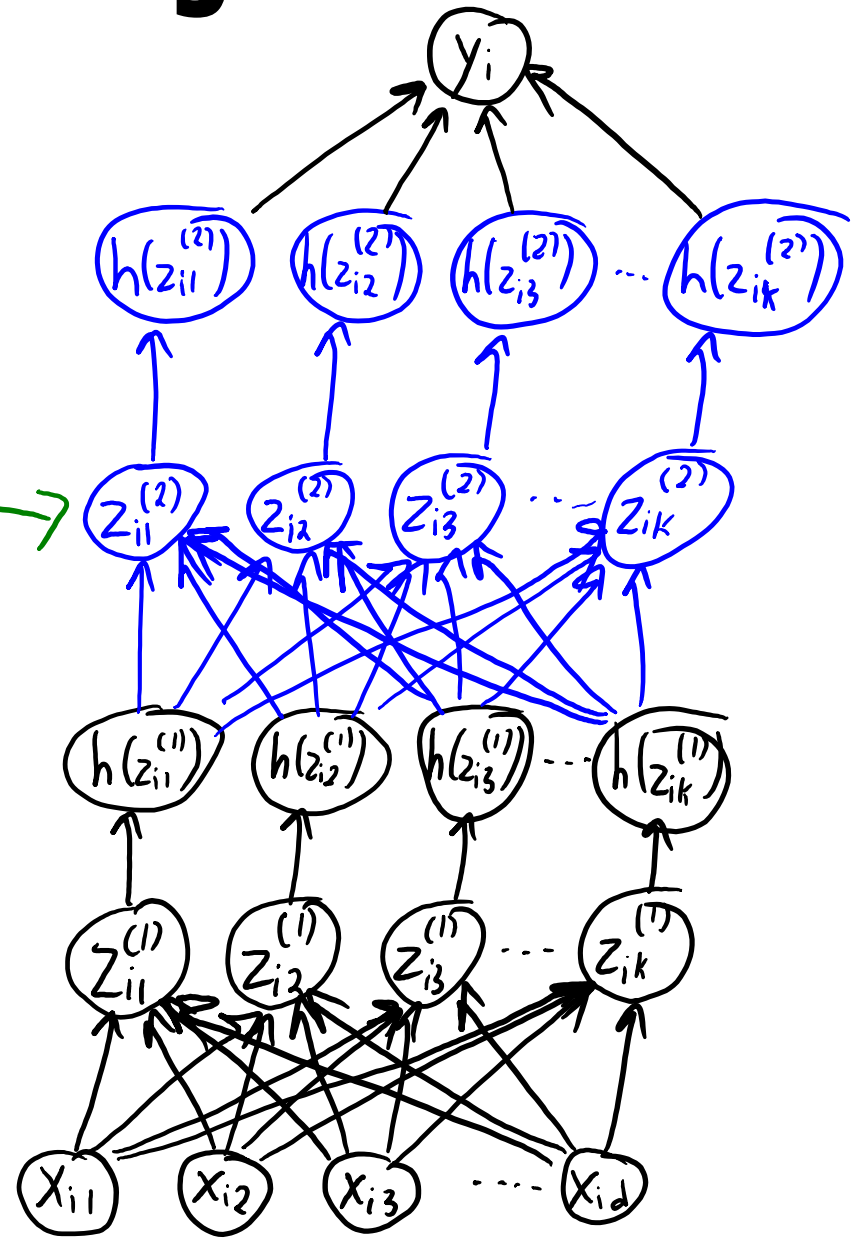
$$\hat{y}_i = v^T h(W^{(3)} h(W^{(2)} h(W^{(1)} x_i)))$$

$\underbrace{\hspace{2em}}_{z_i^{(1)}} \underbrace{\hspace{2em}}_{z_i^{(2)}} \underbrace{\hspace{2em}}_{z_i^{(3)}}$

Deep learning:

Second "layer" of latent features

You can add more "layers" to go "deeper"



Deep Learning

- For 4 layers, we could write the prediction as:

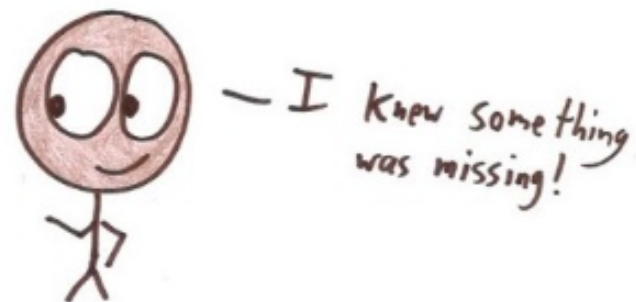
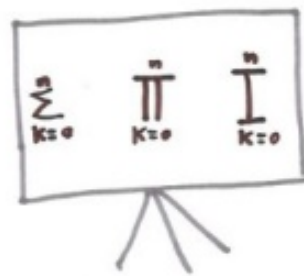
$$\hat{y}_i = v^T h(W^{(4)} h(W^{(3)} h(W^{(2)} h(W^{(1)} x_i))))$$

Symbol: $\prod_{k=0}^n f_k(+)$

Meaning: $f_n \circ f_{n-1} \circ f_{n-2} \circ \dots \circ f_2 \circ f_1 \circ f_0(+)$

- For 'm' layers, we could use

$$\hat{y}_i = v^T \left(\prod_{l=1}^m h(W^{(l)} x_i) \right)$$



Coming Up Next

HISTORY OF DEEP LEARNING

'Godfathers of AI' honored with Turing Award, the Nobel Prize of computing

Yoshua Bengio, Geoffrey Hinton, and Yann LeCun laid the foundations for modern AI

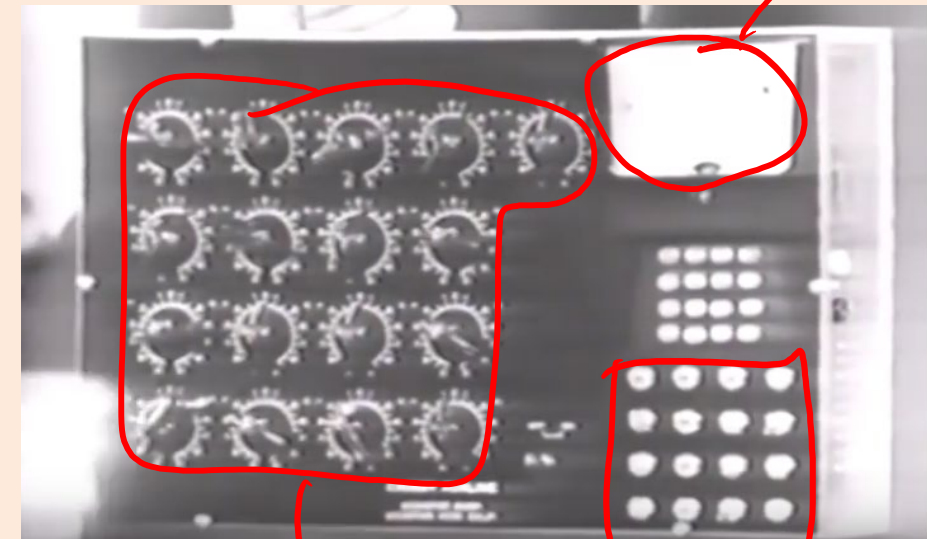
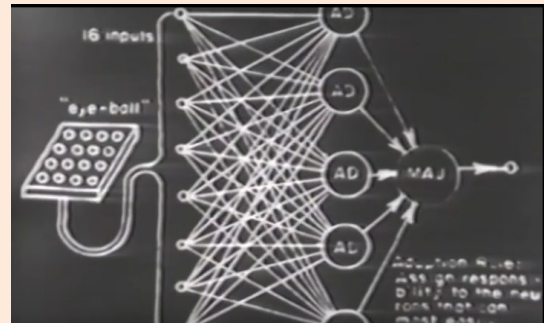
By [James Vincent](#) | Mar 27, 2019, 6:02am EDT



From left to right: Yann LeCun | Photo: Facebook; Geoffrey Hinton | Photo: Google; Yoshua Bengio | Photo: Botler AI

ML and Deep Learning History

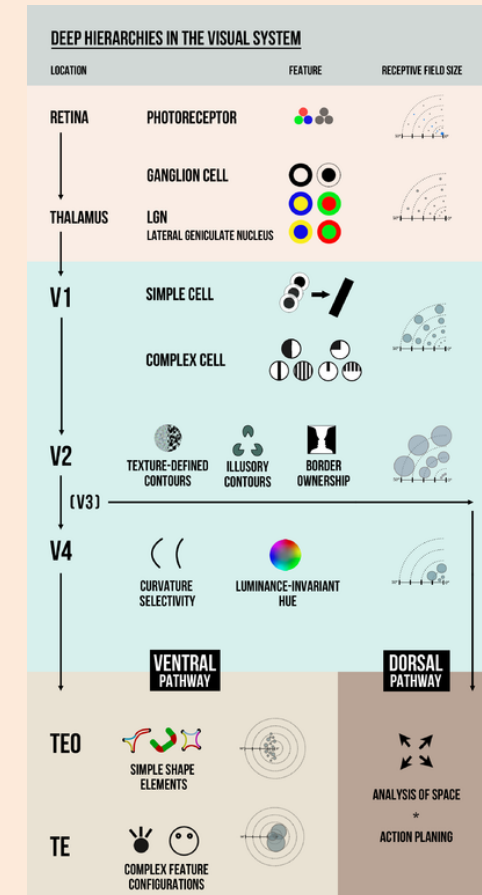
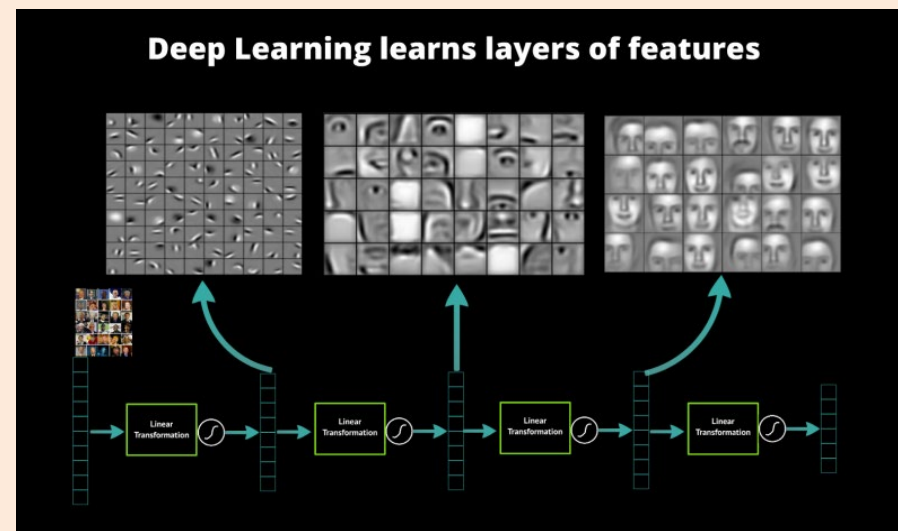
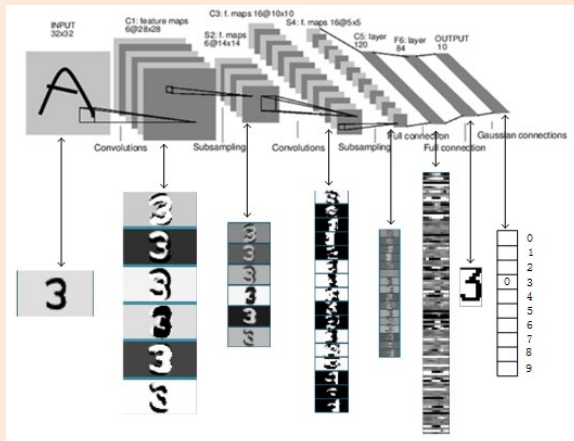
- 1950 and 1960s: Initial excitement.
 - **Perceptron**: linear classifier and stochastic gradient (roughly).
 - “the embryo of an electronic computer that [the Navy] expects will be able to walk, talk, see, write, reproduce itself and be conscious of its existence.” New York Times (1958).
 - <https://www.youtube.com/watch?v=IEFRtz68m-8>
 - Object recognition assigned to students as a summer project



- Then drop in popularity:
 - Quickly realized **limitations of linear models.**

ML and Deep Learning History

- 1970 and 1980s: **Connectionism** (brain-inspired ML)
 - Want “connected **networks of simple units**”.
 - Use **parallel computation** and **distributed representations**.
 - **Adding hidden layers z_i** increases expressive power.
 - With 1 layer and enough sigmoid units, a **universal approximator**.
 - Success in optical character recognition.

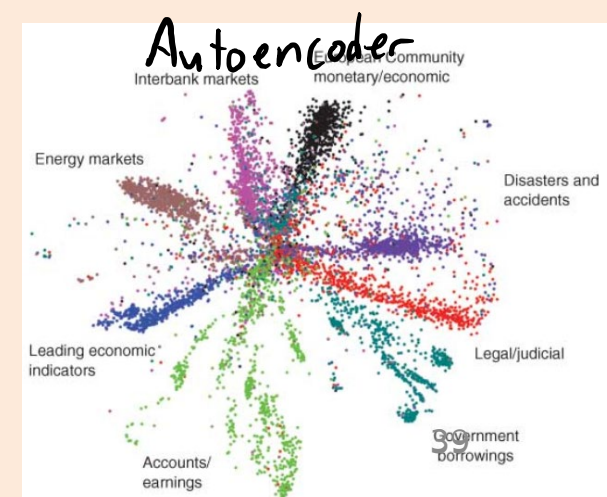
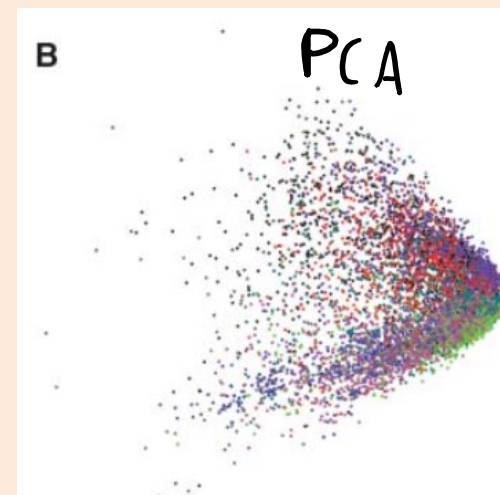


ML and Deep Learning History

- 1990s and early-2000s: drop in popularity.
 - It **proved really difficult to get multi-layer models working** robustly.
 - We obtained similar performance with simpler models:
 - Rise in popularity of **logistic regression and SVMs with regularization and kernels**.
 - Lots of internet successes (spam filtering, web search, recommendation).
 - ML moved closer to other fields like numerical optimization and statistics.

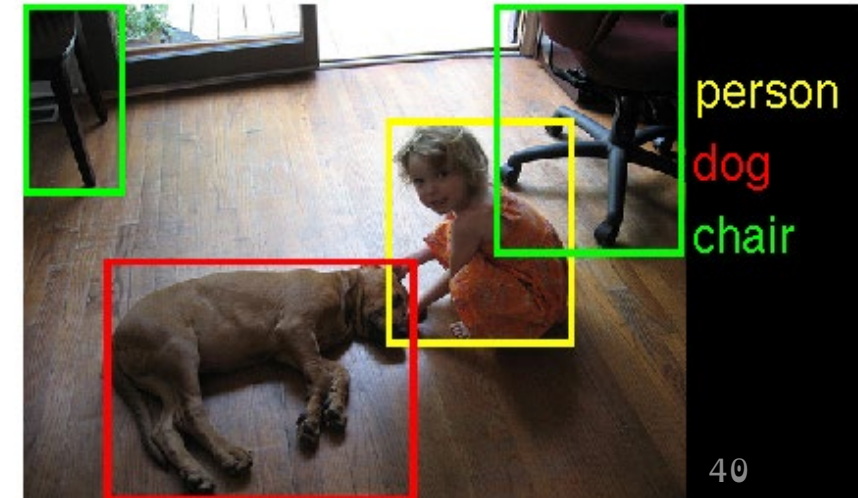
ML and Deep Learning History

- Late 2000s: push to revive connectionism as “**deep learning**”.
 - Canadian Institute For Advanced Research (CIFAR) NCAP program:
 - “Neural Computation and Adaptive Perception”.
 - Led by Geoff Hinton, Yann LeCun, and Yoshua Bengio (“Canadian mafia”).
 - Unsupervised successes: “deep belief networks” and “autoencoders”.
 - Could be used to initialize deep neural networks.
 - <https://www.youtube.com/watch?v=KuPai0ogiHk>



2010s: DEEP LEARNING!!!

- Bigger datasets, bigger models, parallel computing (GPUs/clusters).
 - And some tweaks to the models from the 1980s.
- Huge improvements in automatic speech recognition (2009).
 - All phones now have deep learning.
- Huge improvements in computer vision (2012).
 - Changed computer vision field almost instantly.
 - This is now finding its way into products.



2010s: DEEP LEARNING!!!

- Media hype:
 - “How many computers to identify a cat? 16,000”
New York Times (2012).
 - “Why Facebook is teaching its machines to think like humans”
Wired (2013).
 - “What is ‘deep learning’ and why should businesses care?”
Forbes (2013).
 - “Computer eyesight gets a lot more accurate”
New York Times (2014).
- 2015: huge improvement in language understanding.

Cut-off for Final Exam

(Final exam will have materials from everything before this slide)

Summary

- **Neural networks** learn features z_i for supervised learning.
- **Sigmoid function** avoids degeneracy by introducing non-linearity.
 - Universal approximator with large-enough 'k'.
- **Biological motivation** for (deep) neural networks.
- **Deep learning** considers neural networks with many hidden layers.
 - Can more-efficiently represent some functions.
- **Unprecedented performance** on difficult pattern recognition tasks.

- **Next time:**
 - Training deep networks.

Please Do Course Evaluation!

Review Questions

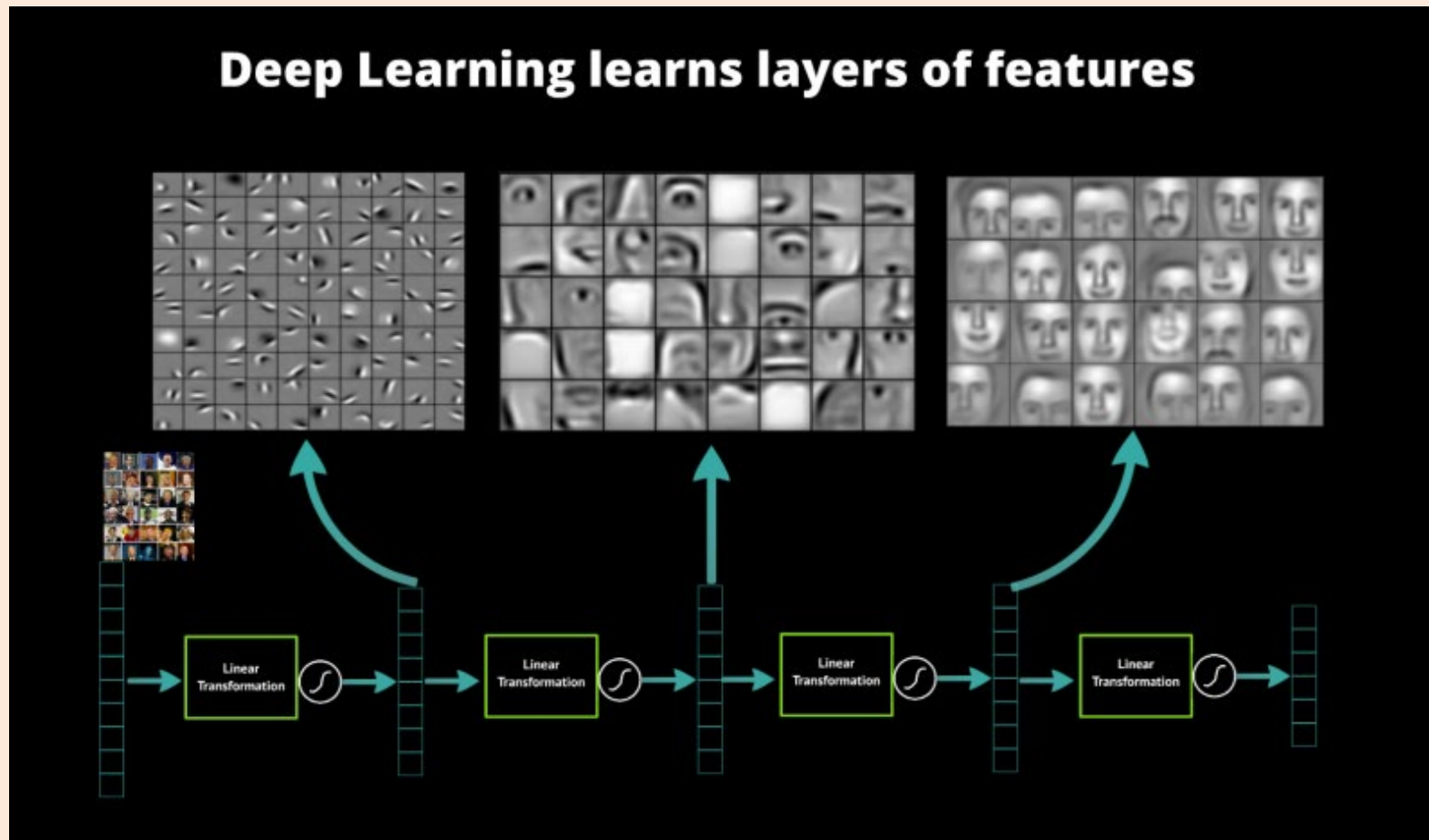
- Q1: What is the problem with using a linear encoder and a linear predictor for a neural network?
- Q2: What is the motivation for using multiple layers of encoders?
- Q3:

Why $z_i = Wx_i$?

- In PCA we had that the optimal $Z = XW^T(WW^T)^{-1}$.
- If W had normalized+orthogonal rows, $Z = XW^T$ (since $WW^T = I$).
 - So $z_i = Wx_i$ in this normalized+orthogonal case.
- Why we would use $z_i = Wx_i$ in neural networks?
 - We didn't enforce normalization or orthogonality.
- Well, the value $W^T(WW^T)^{-1}$ is just “some matrix”.
 - You can think of neural networks as just **directly learning this matrix**.

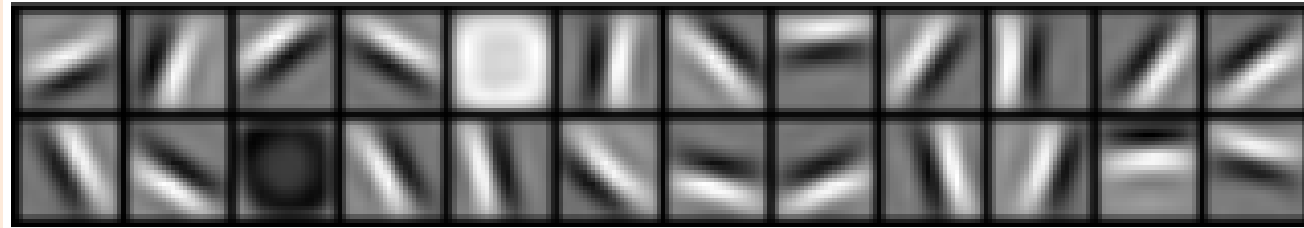
Cool Picture Motivation for Deep Learning

- Faces might be composed of different “parts”:



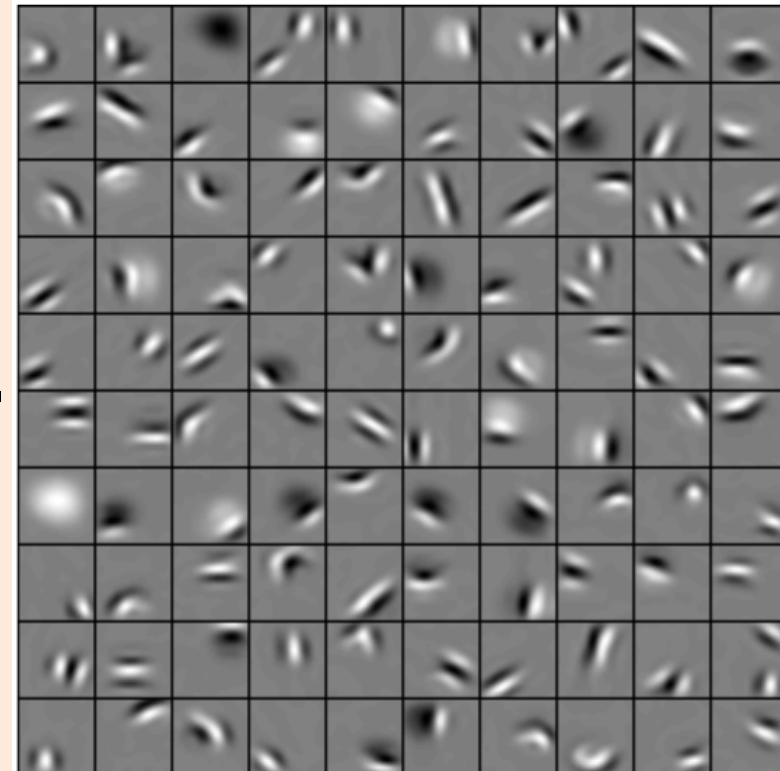
Cool Picture Motivation for Deep Learning

- First layer of z_i trained on 10 by 10 image patches:



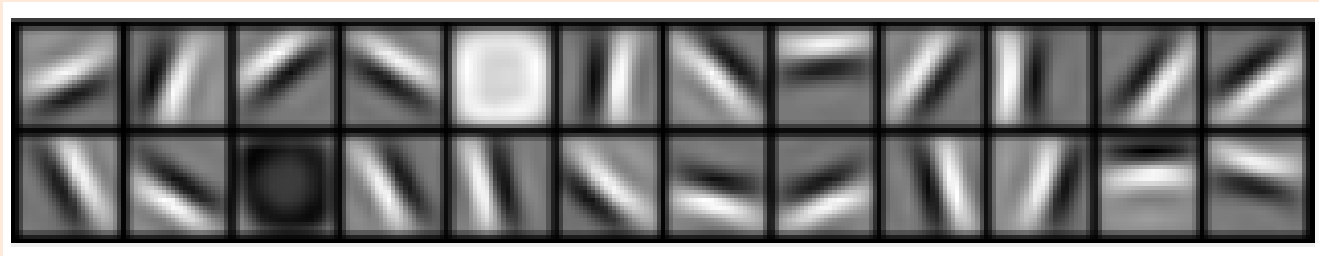
} "Gabor filters"

- Attempt to visualize second layer:
 - Corners, angles, surface boundaries?
- Models require many tricks to work.
 - We'll discuss these next time.



Cool Picture Motivation for Deep Learning

- First layer of z_i trained on 10 by 10 image patches:



} "Gabor filters"

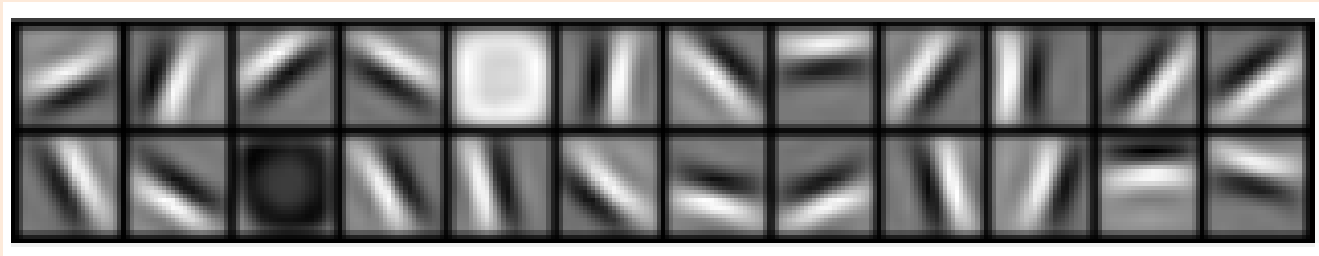
- Visualization of second and third layers trained on specific objects:

faces



Cool Picture Motivation for Deep Learning

- First layer of z_i trained on 10 by 10 image patches:

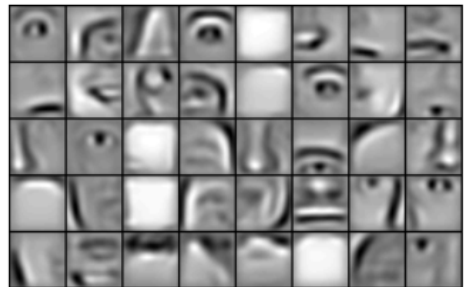


} "Gabor filters"

- Visualization of second and third layers trained on specific objects:

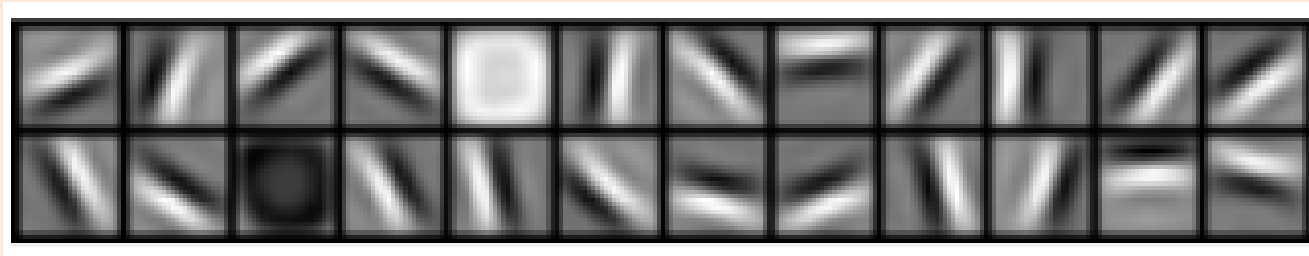
faces

cars



Cool Picture Motivation for Deep Learning

- First layer of z_i trained on 10 by 10 image patches:



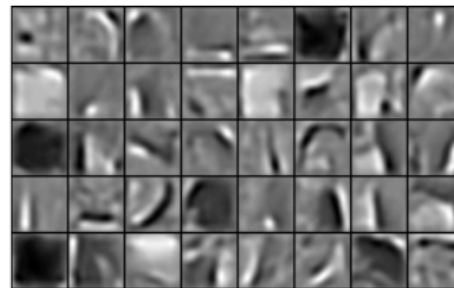
} "Gabor filters"

- Visualization of second and third layers trained on specific objects:

faces

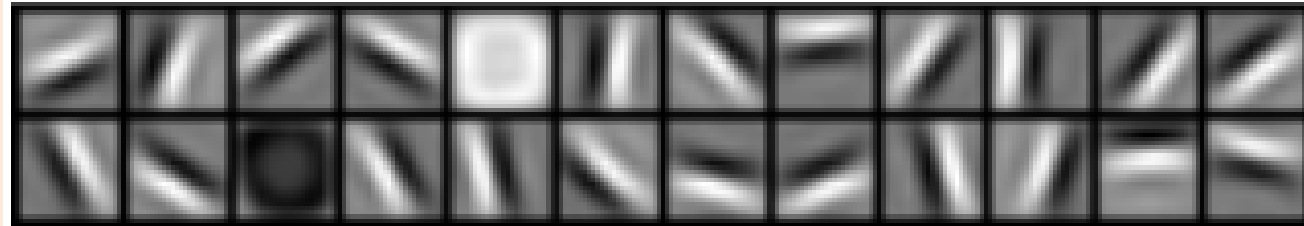
cars

elephants



Cool Picture Motivation for Deep Learning

- First layer of z_i trained on 10 by 10 image patches:



} "Gabor filters"

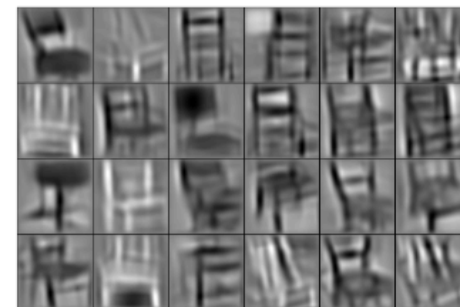
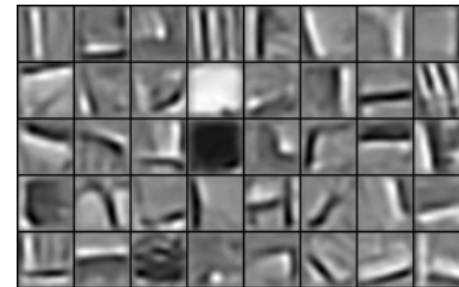
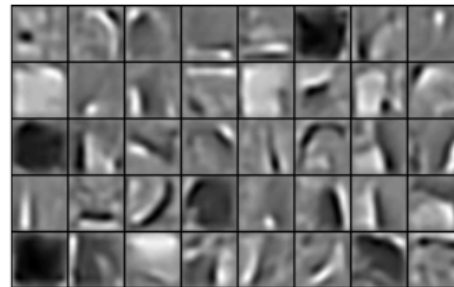
- Visualization of second and third layers trained on specific objects:

faces

cars

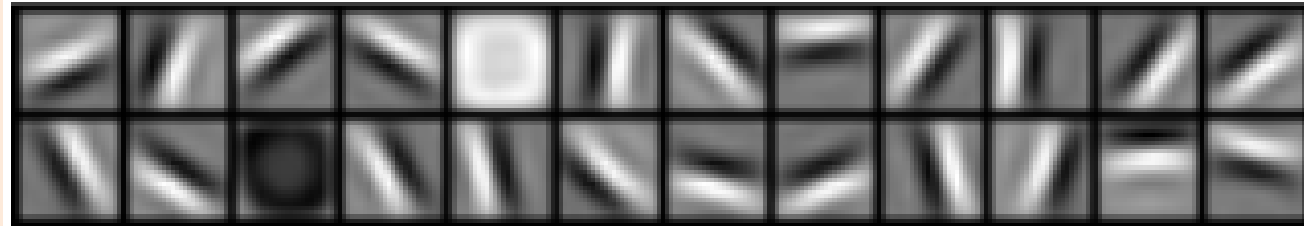
elephants

chairs



Cool Picture Motivation for Deep Learning

- First layer of z_i trained on 10 by 10 image patches:



} "Gabor filters"

- Visualization of second and third layers trained on specific objects:

faces

cars

elephants

chairs

faces, cars, airplanes, motorbikes

