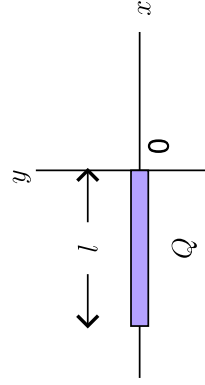


Tutorial 5 Question

- Text: Ch. 21: Pr. 48.
- A thin rod of length l carries a total charge Q distributed uniformly along its length. Determine the electric field along the axis of the rod starting at one end—that is, find $E(x)$ for $x \geq 0$.

• Hint: $\int \frac{dz}{(x+z)^2} = \frac{-1}{x+z} + C$.



<http://www.zoology.ubc.ca/~rkhlok/phys102/tutorial/>

UBC Physics 102: Tutorial 5, July 8, 2009 – p. 14

Solution, contd

- The charge in that chunk is $dQ = \frac{Q dz}{l}$. And it is at a distance $r = x + z$ from the point x so, from Coulomb's law the electric field is

$$\begin{aligned} d\mathbf{E} &= \frac{k dQ}{r^2} \hat{\mathbf{r}} \\ &= \frac{kQ dz}{l(x+z)^2} \hat{\mathbf{i}}. \end{aligned}$$

- That gives the contribution from the chunk at position z . To get the total field we add up the contributions for all z between 0 and l to get

$$\mathbf{E} = \int d\mathbf{E}$$

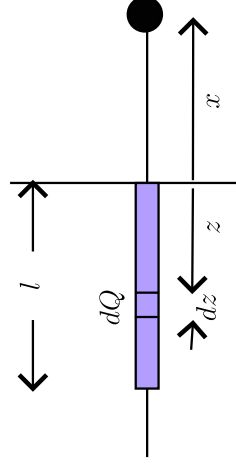


<http://www.zoology.ubc.ca/~rkhlok/phys102/tutorial/>

UBC Physics 102: Tutorial 5, July 8, 2009 – p. 34

Solution

- Since this is a continuous charge distribution we have to break it into small chunks and add all the electric fields together.
- To break the rod into chunks we introduce a new variable z which indicates our current position along the length of the rod. Then we look at a chunk of rod of length dz .



<http://www.zoology.ubc.ca/~rkhlok/phys102/tutorial/>

UBC Physics 102: Tutorial 5, July 8, 2009 – p. 24

Solution, contd

$$\begin{aligned} \mathbf{E} &= \int_0^l \frac{kQ dz}{l(x+z)^2} \hat{\mathbf{i}} \\ &= \frac{kQ \hat{\mathbf{i}}}{l} \int_0^l \frac{dz}{(x+z)^2} \\ &= \frac{kQ \hat{\mathbf{i}}}{l} \frac{l}{(x+l)x} \\ &= \frac{kQ}{(x+l)x} \hat{\mathbf{i}}. \quad \square \end{aligned}$$

- Nontrivial integrals will be given if needed on tests.
- The question only asks for the scalar field strength. I included the vector to demonstrate how it can be worked through the integral.



<http://www.zoology.ubc.ca/~rkhlok/phys102/tutorial/>

UBC Physics 102: Tutorial 5, July 8, 2009 – p. 44