

# Visualization Analysis & Design

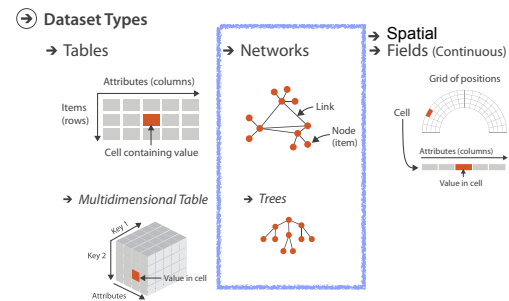
## Network Data (Ch 9)

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### Network data

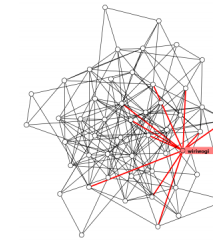
- networks
  - model relationships between things
    - aka graphs
    - two kinds of items, both can have attributes
      - nodes
      - links
- tree
  - special case
  - no cycles
    - one parent per node



2

### Network tasks: topology-based and attribute-based

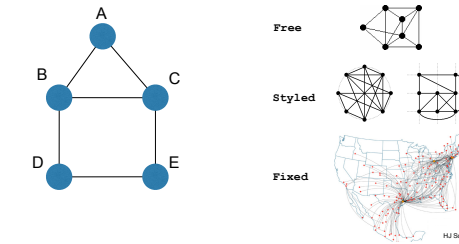
- topology based tasks
  - find paths
  - find (topological) neighbors
  - compare centrality/importance measures
  - identify clusters / communities
- attribute based tasks (similar to table data)
  - find distributions, ...
- combination tasks, incorporating both
  - example: find friends-of-friends who like cats
    - topology: find all adjacent nodes of given node
    - attributes: check if has-pet (node attribute) == cat



3

### Node-link diagrams

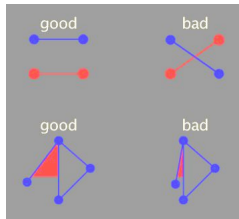
- nodes: point marks
  - links: line marks
    - straight lines or arcs
    - connections between nodes
- intuitive & familiar
  - most common
  - many, many variants



4

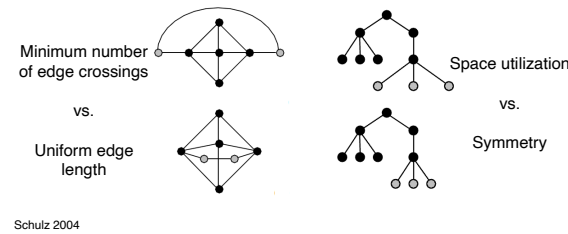
### Criteria for good node-link layouts

- minimize
  - edge crossings, node overlaps
  - distances between topological neighbor nodes
  - total drawing area
  - edge bends
- maximize
  - angular distance between different edges
  - aspect ratio disparities
- emphasize symmetry
  - similar graph structures should look similar in layout



### Criteria conflict

- most criteria NP-hard individually
- many criteria directly conflict with each other



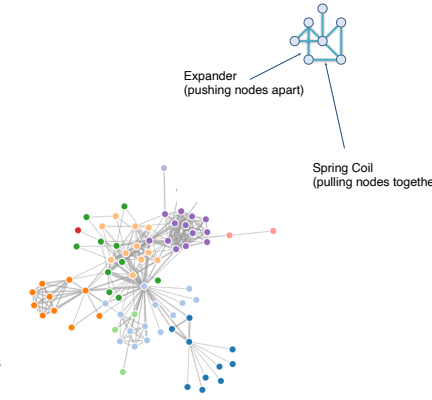
Schulz 2004

### Optimization-based layouts

- formulate layout problem as optimization problem
- convert criteria into weighted cost function
  - $F(\text{layout}) = a * [\text{crossing counts}] + b * [\text{drawing space used}] + \dots$
- use known optimization techniques to find layout at minimal cost
  - energy-based physics models
  - force-directed placement
  - spring embedders

### Force-directed placement

- physics model
  - links = springs pull together
  - nodes = magnets repulse apart
- algorithm
  - place vertices in random locations
  - while not equilibrium
    - calculate force on vertex
      - sum of
        - pairwise repulsion of all nodes
        - attraction between connected nodes
    - move vertex by  $c * \text{vertex\_force}$



<http://mbostock.github.com/d3/ex/force.html>

5

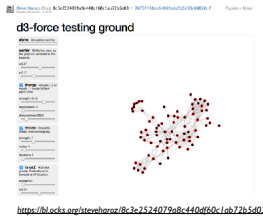
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7

8

### Force-directed placement properties

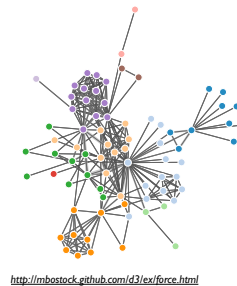
- strengths
  - reasonable layout for small, sparse graphs
  - clusters typically visible
  - edge length uniformity
- weaknesses
  - nondeterministic
    - computationally expensive:  $O(n^3)$  for n nodes
      - each step is  $n^2$ , takes ~n cycles to reach equilibrium
    - naive FD doesn't scale well beyond 1K nodes
    - iterative progress: engaging but distracting



<https://bl.ocks.org/mbostock/7524879#0-4404f50c-1ab7265d02>

### Idiom: force-directed placement

- visual encoding
  - link connection marks, node point marks
- considerations
  - spatial position: no meaning directly encoded
    - left free to minimize crossings
  - proximity semantics?
    - sometimes meaningful
    - sometimes arbitrary, artifact of layout algorithm
    - tension with length
      - long edges more visually salient than short
- tasks
  - explore topology; locate paths, clusters
- scalability
  - node/edge density  $E < 4N$



<http://mbostock.github.com/d3/ex/force.html>

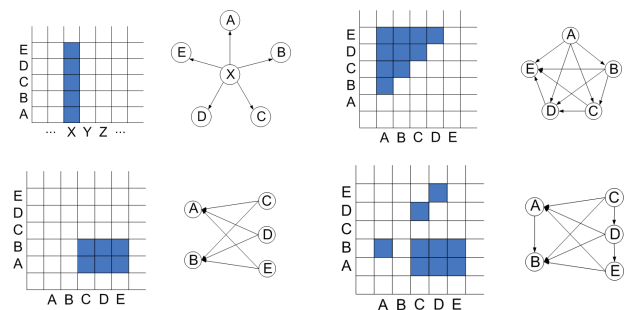
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11

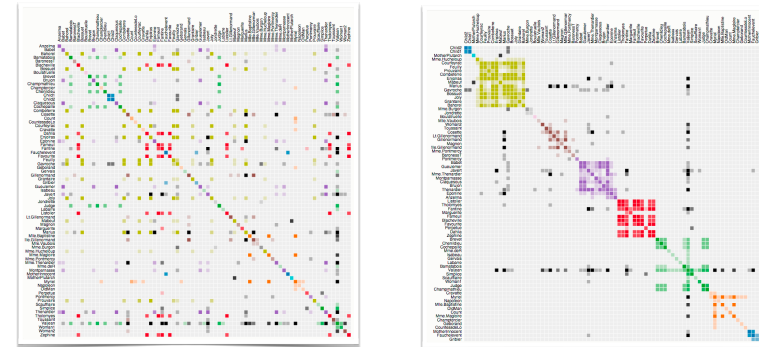
12

### Adjacency matrix examples



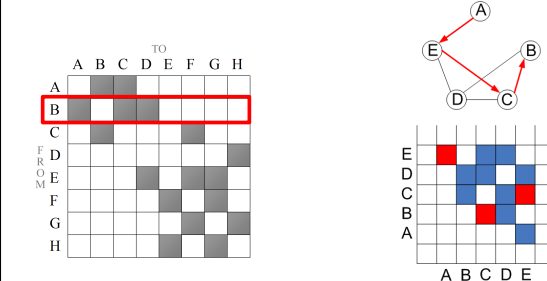
HJ Schulz 2007

### Node order is crucial: Reordering



<https://bost.ocks.org/mike/miserables/>

### Adjacency matrix



good for topology tasks related to neighborhoods (node 1-hop neighbors)

bad for topology tasks related to paths

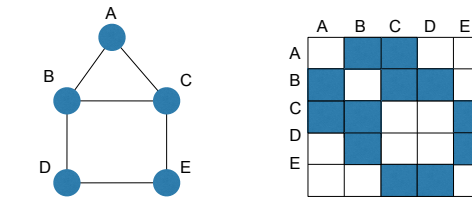
13

14

15

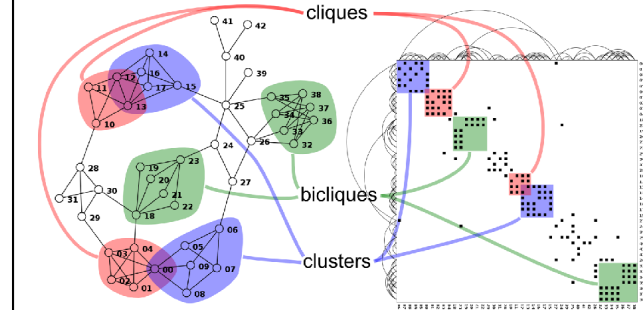
### Adjacency matrix representations

- derive adjacency matrix from network



16

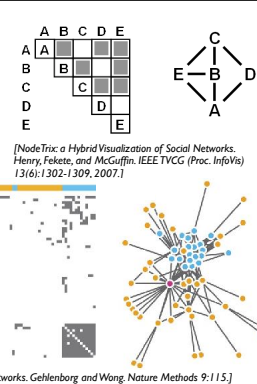
### Structures visible in both



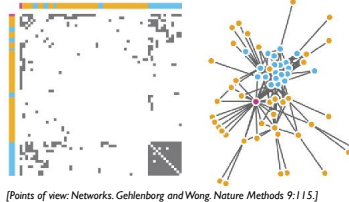
<http://www.michaelmcguffin.com/courses/vis/patternsInAdjacencyMatrix.png>

## Idiom: adjacency matrix view

- data: network
  - transform into same data/encoding as heatmap
- derived data: table from network
  - 1 quant attrib
    - weighted edge between nodes
  - 2 categ attribs: node list x 2
- visual encoding
  - cell shows presence/absence of edge
- scalability
  - 1K nodes, 1M edges



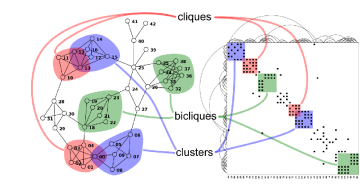
[NodeTrix: a Hybrid Visualization of Social Networks. Henry Fekete, and McGuffin. IEEE TVCG (Proc. InfoVis) 13(6):1302-1309, 2007.]



[Points of view: Networks. Gehlenborg and Wong. Nature Methods 9:115.]

## Node-link vs. matrix comparison

- node-link diagram strengths
  - topology understanding, path tracing
  - intuitive, flexible, no training needed
- adjacency matrix strengths
  - focus on edges rather than nodes
  - layout straightforward (reordering needed)
  - predictability, scalability
  - some topology tasks trainable
- empirical study
  - node-link best for small networks
  - matrix best for large networks
    - if tasks don't involve path tracing!

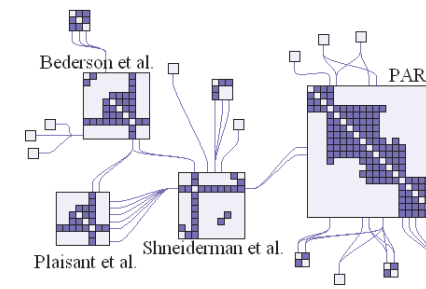


<http://www.michaelmcguffin.com/courses/vis/patterns/AdjacencyMatrix.png>

[On the readability of graphs using node-link and matrix-based representations: a controlled experiment and statistical analysis. Ghoniem, Fekete, and Castagliola. Information Visualization 4:2 (2005), 114–135.]

## Idiom: NodeTrix

- hybrid nodelink/matrix
- capture strengths of both

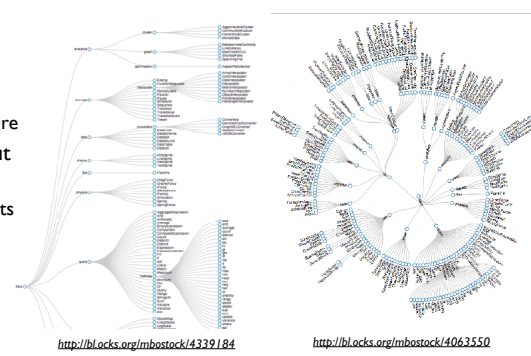


[NodeTrix: a Hybrid Visualization of Social Networks. Henry Fekete, and McGuffin. IEEE TVCG (Proc. InfoVis) 13(6):1302-1309, 2007.]

## Trees

## Node-link trees

- Reingold-Tilford
  - tidy drawings of trees
    - exploit parent/child structure
  - allocate space: compact but without overlap
    - rectilinear and radial variants
- nice algorithm writeup
  - <http://billmill.org/pymag-trees/>

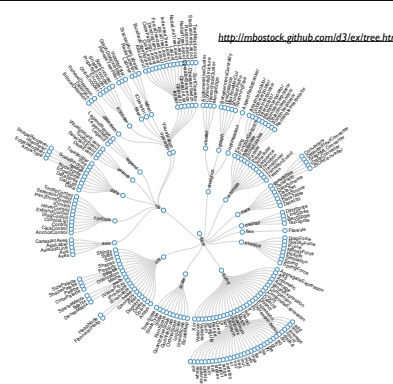


<http://bllocks.org/mbostock/4339184>

<http://bllocks.org/mbostock/4063550>

## Idiom: radial node-link tree

- data
  - tree
- encoding
  - link connection marks
  - point node marks
  - radial axis orientation
    - angular proximity: siblings
    - distance from center: depth in tree
- tasks
  - understanding topology, following paths
- scalability
  - 1K - 10K nodes (with/without labels)

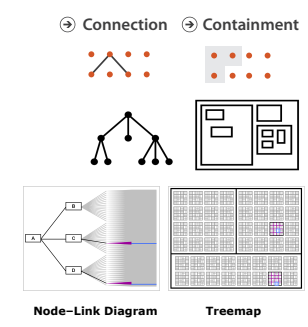


<http://mbostock.github.com/d3/ex/tree.html>

[Elastic Hierarchies: Combining Treemaps and Node-Link Diagrams. Dong, McGuffin, and Chignell. Proc. InfoVis 2005, p. 57-64.]

## Link marks: Connection and containment

- marks as links (vs. nodes)
  - common case in network drawing
  - 1D case: connection
    - ex: all node-link diagrams
    - emphasizes topology, path tracing
    - networks and trees
  - 2D case: containment
    - ex: all treemap variants
    - emphasizes attribute values at leaves (size coding)
    - only trees

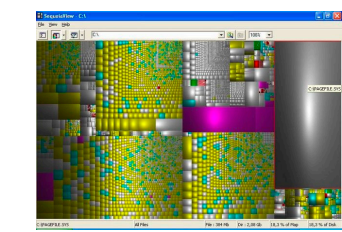


Node-Link Diagram Treemap

[Elastic Hierarchies: Combining Treemaps and Node-Link Diagrams. Dong, McGuffin, and Chignell. Proc. InfoVis 2005, p. 57-64.]

## Idiom: treemap

- data
  - tree
  - 1 quant attrib at leaf nodes
- encoding
  - area containment marks for hierarchical structure
  - rectilinear orientation
  - size encodes quant attrib
- tasks
  - query attribute at leaf nodes
  - ex: disk space usage within filesystem
- scalability
  - 1M leaf nodes



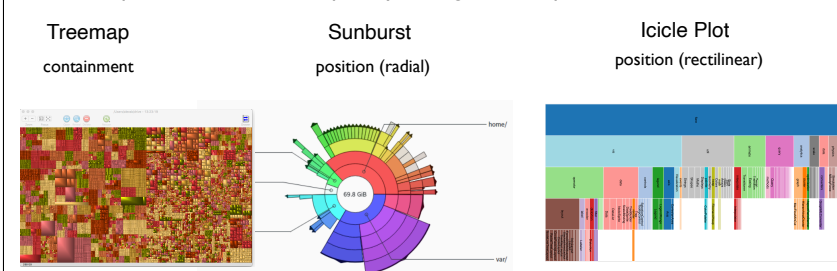
<https://www.win.tue.nl/sequoia/view/>  
[Cushion Treemaps, van Wijk and van de Wetering. Proc. Symp. InfoVis 1999, 73-78.]



24

## Idiom: implicit tree layouts (sunburst, icicle plot)

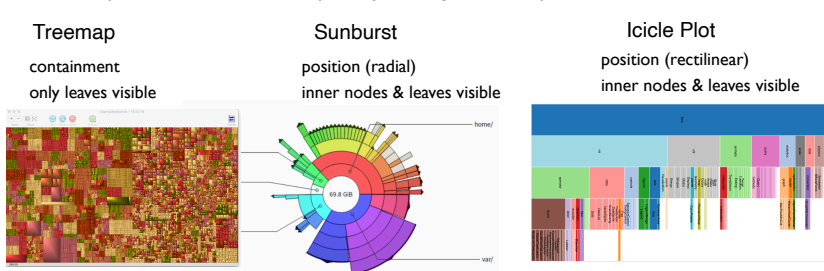
- alternative to connection and containment: position
  - show parent-child relationships only through relative positions



25

## Idiom: implicit tree layouts (sunburst, icicle plot)

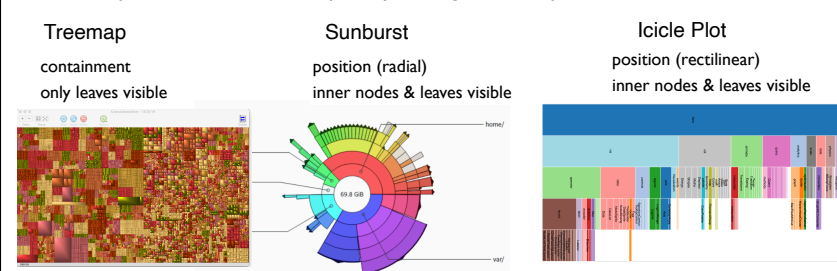
- alternative to connection and containment: position
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26

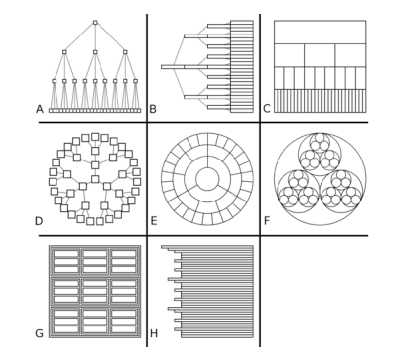
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- alternative to connection and containment: position
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27

## Tree drawing idioms comparison

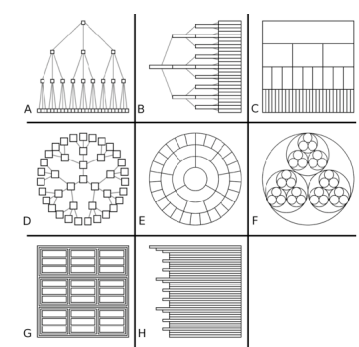


[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees. McGuffin and Robert. Information Visualization 9:2 (2010), 115–140.]

28

## Comparison: tree drawing idioms

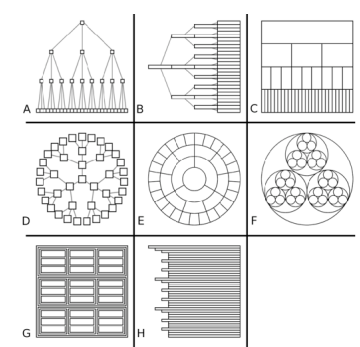
- data shown
  - link relationships
  - tree depth
  - sibling order



[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees. McGuffin and Robert. Information Visualization 9:2 (2010), 115–140.]

## Comparison: tree drawing idioms

- data shown
  - link relationships
  - tree depth
  - sibling order
- design choices
  - connection vs containment link marks
  - rectilinear vs radial layout
  - spatial position channels

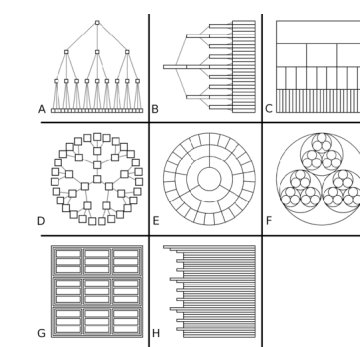


[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees. McGuffin and Robert. Information Visualization 9:2 (2010), 115–140.]

29

## Comparison: tree drawing idioms

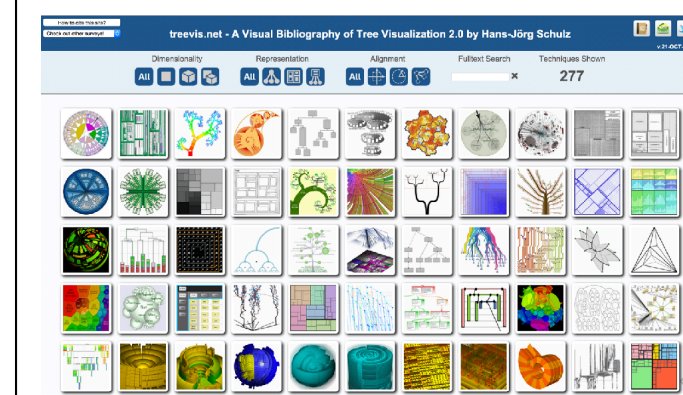
- data shown
  - link relationships
  - tree depth
  - sibling order
- design choices
  - connection vs containment link marks
  - rectilinear vs radial layout
  - spatial position channels
- considerations
  - redundant? arbitrary?
  - information density?
    - avoid wasting space
    - consider where to fit labels!



[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees. McGuffin and Robert. Information Visualization 9:2 (2010), 115–140.]

30

## treevis.net: Many, many options!



<https://treevis.net/>

31

## Arrange networks and trees

Node-Link Diagrams  
 Connection Marks  
 NETWORKS  TREES

Adjacency Matrix  
 Derived Table  
 NETWORKS  TREES

Enclosure  
 Containment Marks  
 NETWORKS  TREES

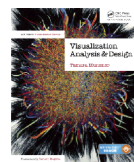
Implicit  
 Spatial Position  
 NETWORKS  TREES

33

## Visualization Analysis & Design

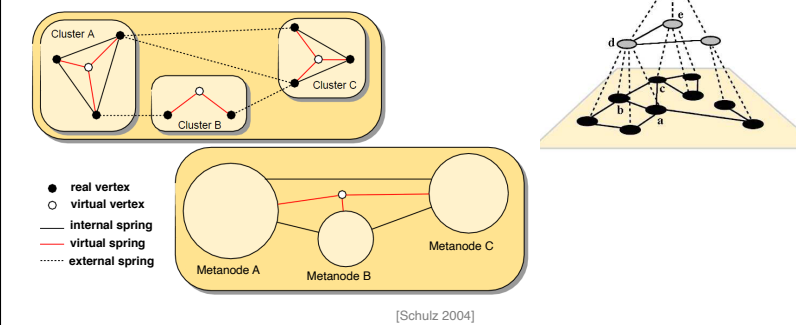
### Network Data (Ch 9) II

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## Multilevel networks

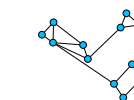
- derive cluster hierarchy of metanodes on top of original graph nodes



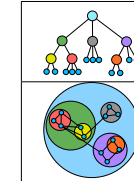
35

## Idiom: GrouseFlocks

- data: compound network
  - network
  - cluster hierarchy atop it
    - derived or interactively chosen
- visual encoding
  - connection marks for network links
  - containment marks for hierarchy
  - point marks for nodes
- dynamic interaction
  - select individual metanodes in hierarchy to expand/contract



Graph Hierarchy 1

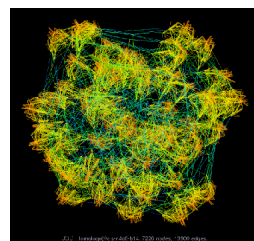


[GrouseFlocks: Steerable Exploration of Graph Hierarchy Space. Archambault, Munzner, and Auber. IEEE TVCG 14(4):900-913, 2008.]

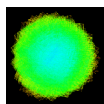
36

## Idiom: sdfp (multi-level force-directed placement)

- data: compound graph
  - original: network
  - derived: cluster hierarchy atop it
- considerations
  - better algorithm for same encoding technique
    - same: fundamental use of space
    - hierarchy used for algorithm speed/quality but not shown explicitly
- scalability
  - nodes, edges: 1K-10K
  - hairball problem eventually hits



[Efficient and high quality force-directed graph drawing. Hu. The Mathematica Journal 10:37-71, 2005.]

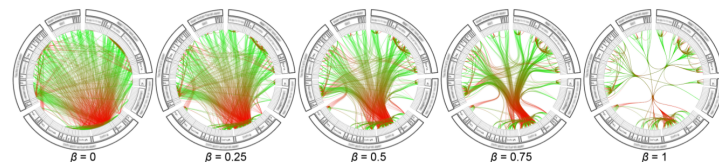


<http://www.research.att.com/~erhu/GALLERY/GRAPHS/index.html>

37

## Idiom: hierarchical edge bundling

- data
  - any layout of compound network
    - network: software classes (nodes), import/export between classes (links)
    - cluster hierarchy: class package structure
  - derived: bundles of edges with same source/destination (multi-level)
- idiom: curve edge routes according to bundles
- task: edge clutter reduction

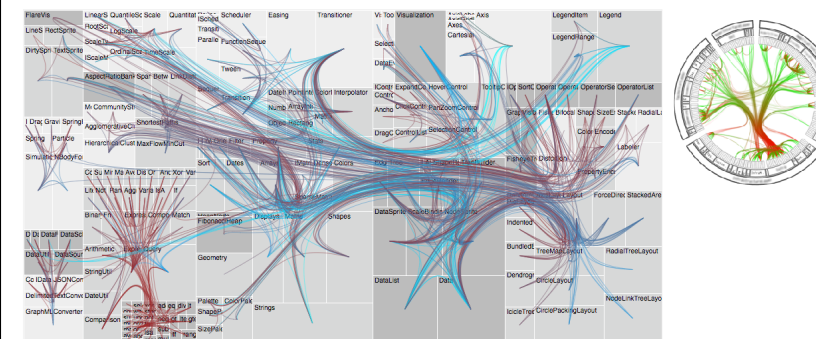


[Hierarchical Edge Bundles: Visualization of Adjacency Relations in Hierarchical Data. Danny Holten. TVCG 12(5):741-748 2006]

38

## Hierarchical edge bundling

- works for any layout: treemap vs radial



[Hierarchical Edge Bundles: Visualization of Adjacency Relations in Hierarchical Data. Danny Holten. TVCG 12(5):741-748 2006]

39