

# Visualization Analysis & Design

## *Network Data (Ch 9)*

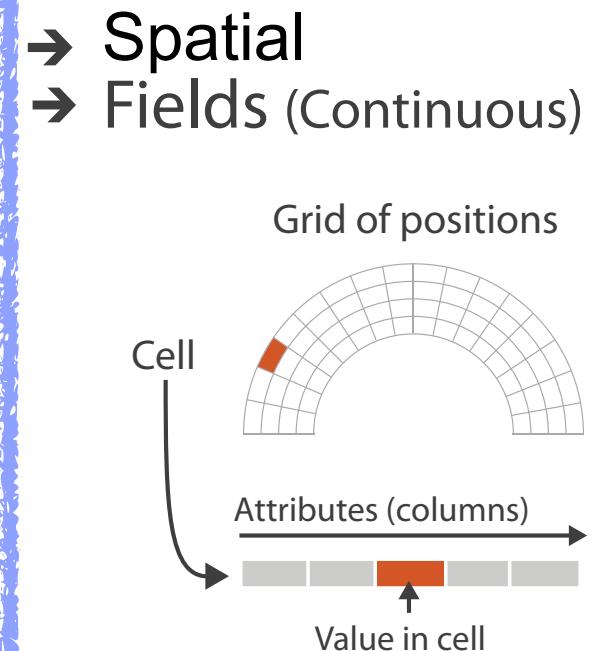
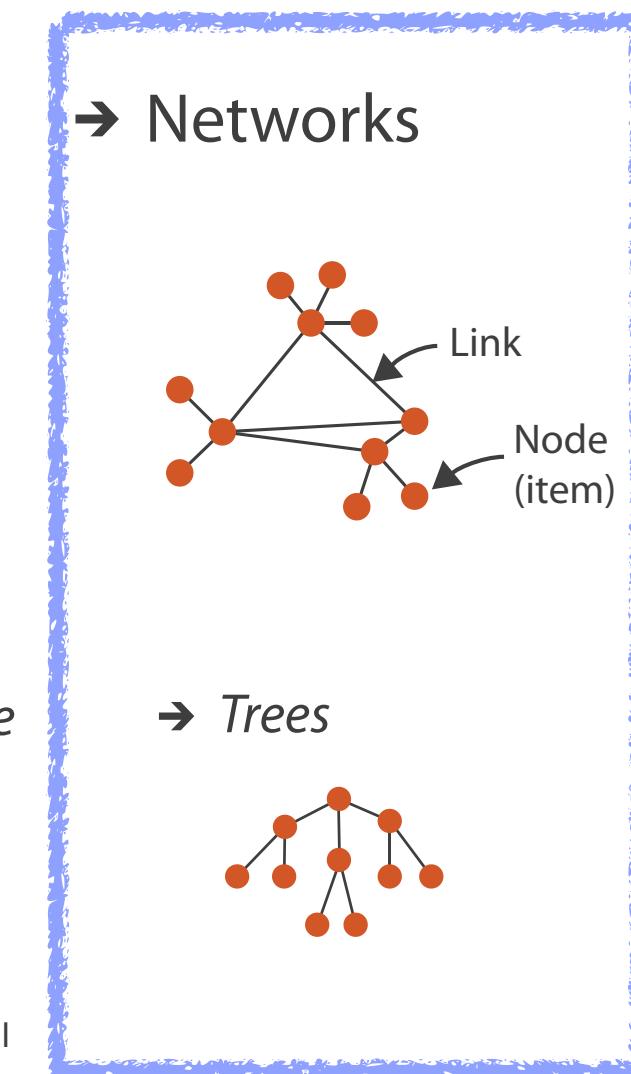
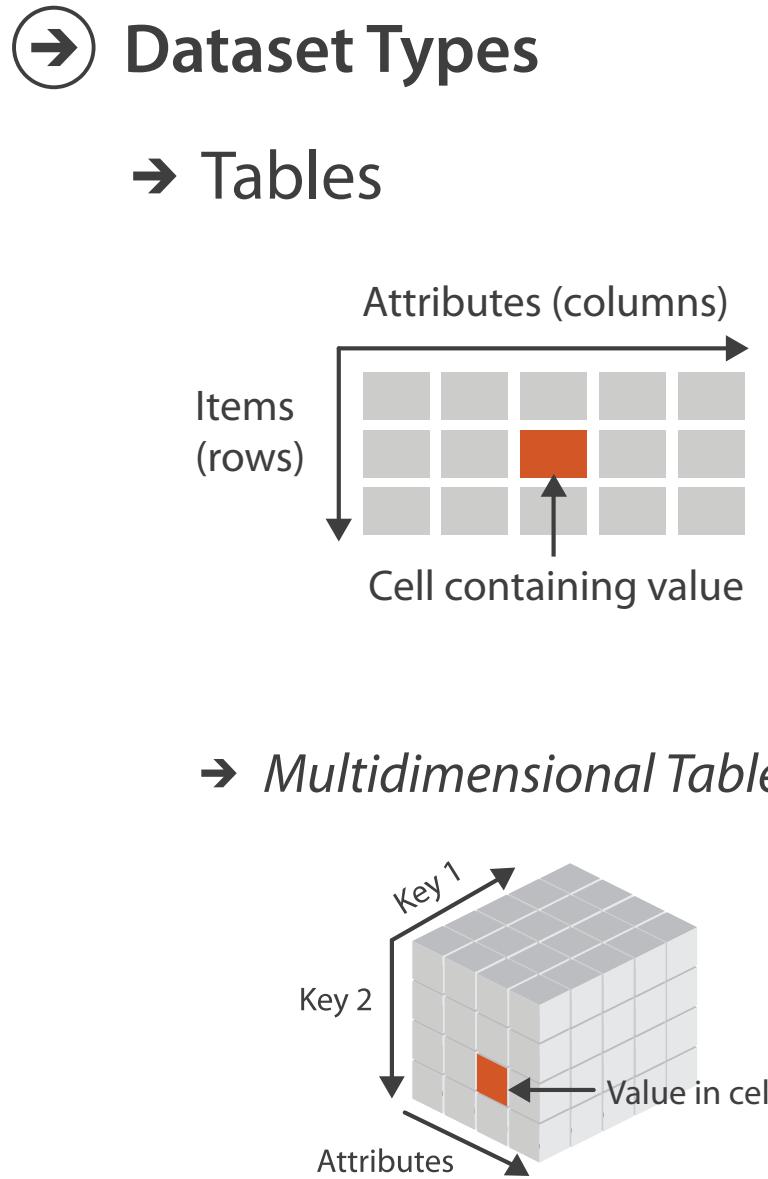
**Tamara Munzner**

Department of Computer Science  
University of British Columbia

[@tamaramunzner](#)

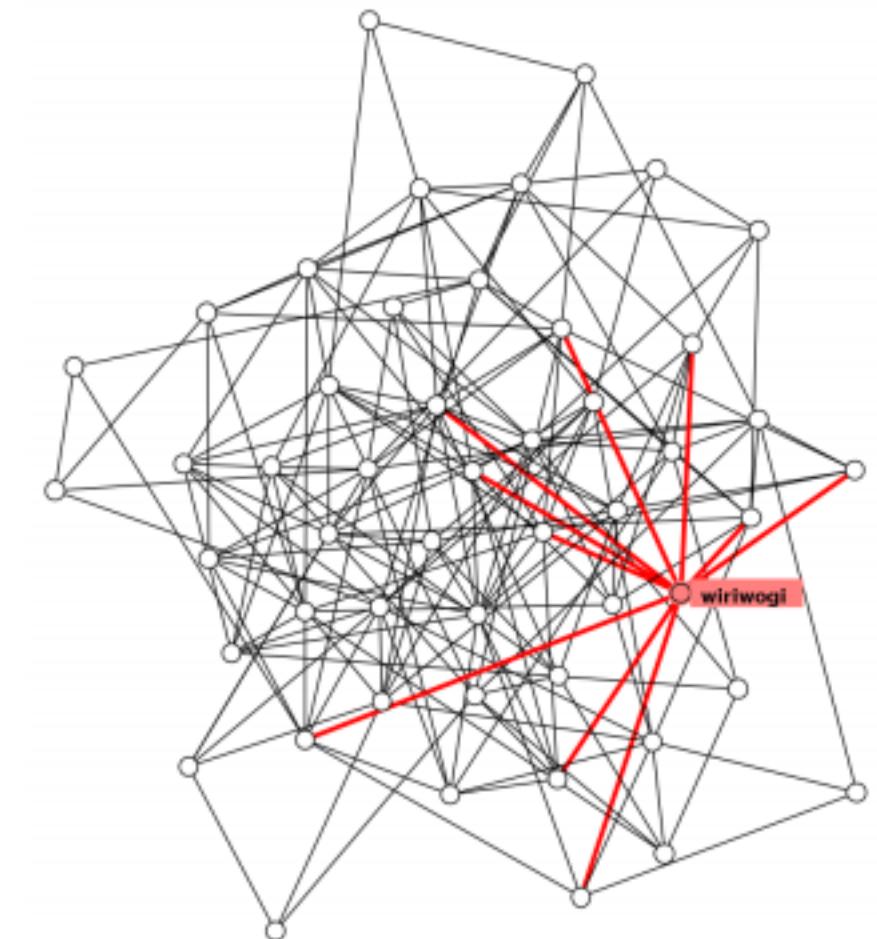
# Network data

- networks
  - model relationships between things
    - aka graphs
  - two kinds of items, both can have attributes
    - nodes
    - links
- tree
  - special case
  - no cycles
    - one parent per node



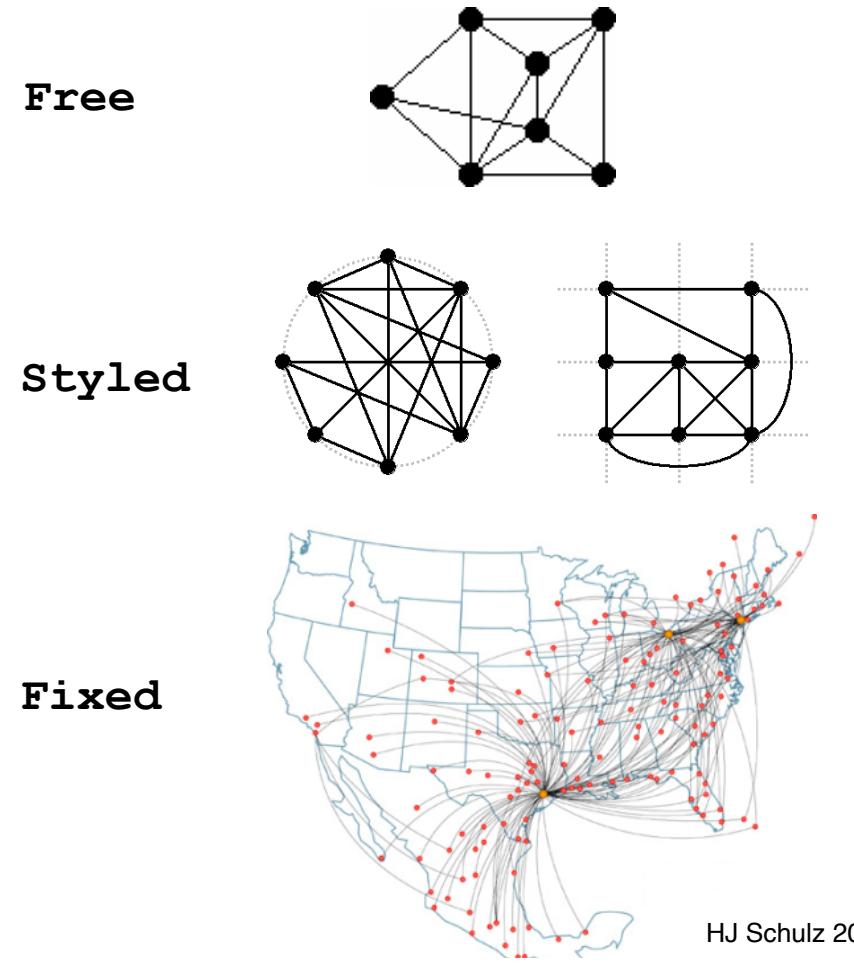
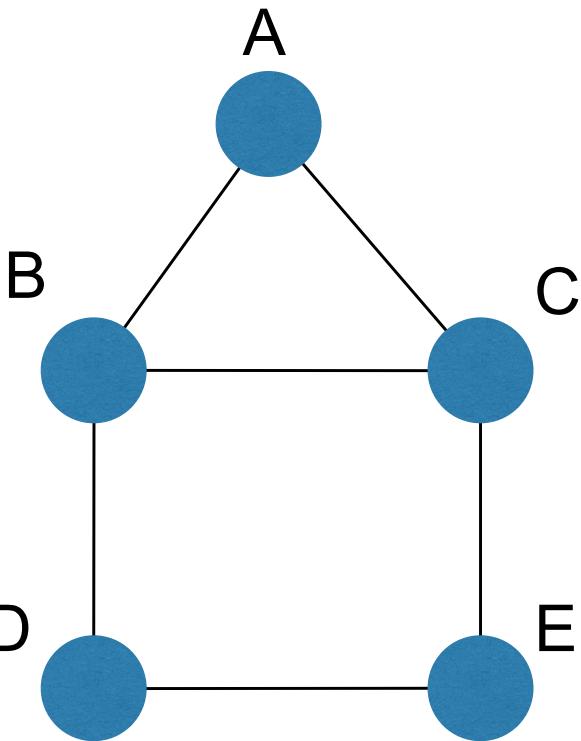
# Network tasks: topology-based and attribute-based

- topology based tasks
  - find paths
  - find (topological) neighbors
  - compare centrality/importance measures
  - identify clusters / communities
- attribute based tasks (similar to table data)
  - find distributions, ...
- combination tasks, incorporating both
  - example: find friends-of-friends who like cats
    - topology: find all adjacent nodes of given node
    - attributes: check if has-pet (node attribute) == cat



# Node-link diagrams

- nodes: point marks
- links: line marks
  - straight lines or arcs
  - connections between nodes
- intuitive & familiar
  - most common
  - many, many variants



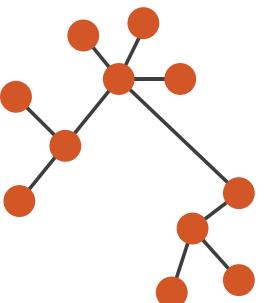
HJ Schulz 2006

## → Node-Link Diagrams

Connection Marks

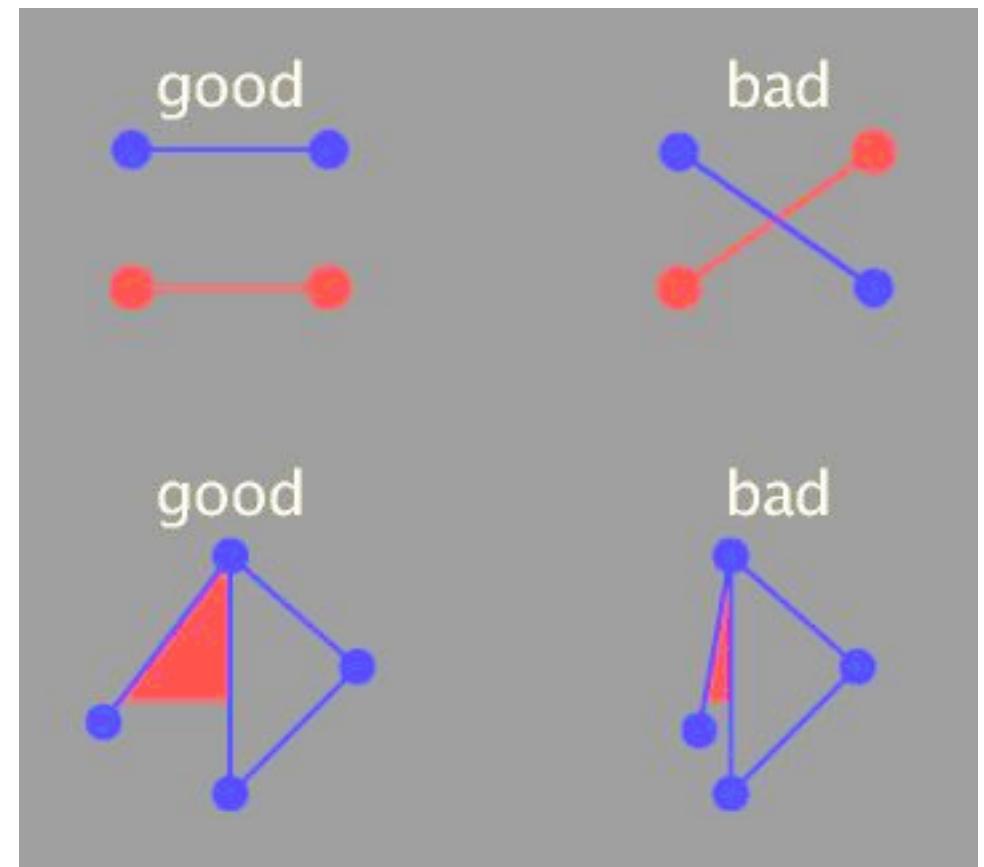
NETWORKS

TREES



# Criteria for good node-link layouts

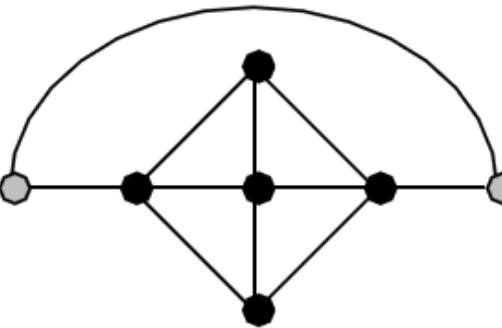
- minimize
  - edge crossings, node overlaps
  - distances between topological neighbor nodes
  - total drawing area
  - edge bends
- maximize
  - angular distance between different edges
  - aspect ratio disparities
- emphasize symmetry
  - similar graph structures should look similar in layout



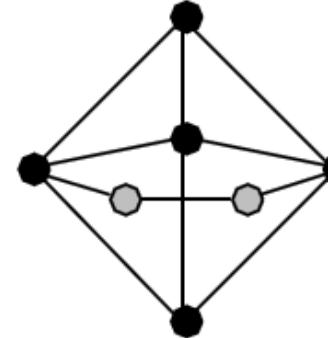
# Criteria conflict

- most criteria NP-hard individually
- many criteria directly conflict with each other

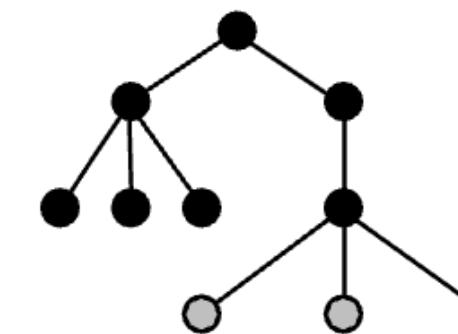
Minimum number  
of edge crossings



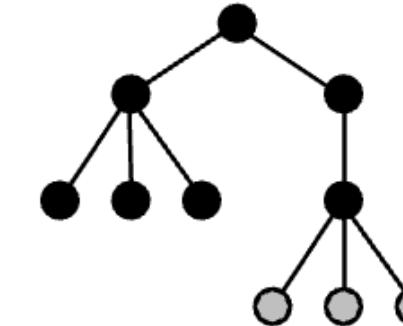
Uniform edge  
length



vs.



Space utilization



Symmetry

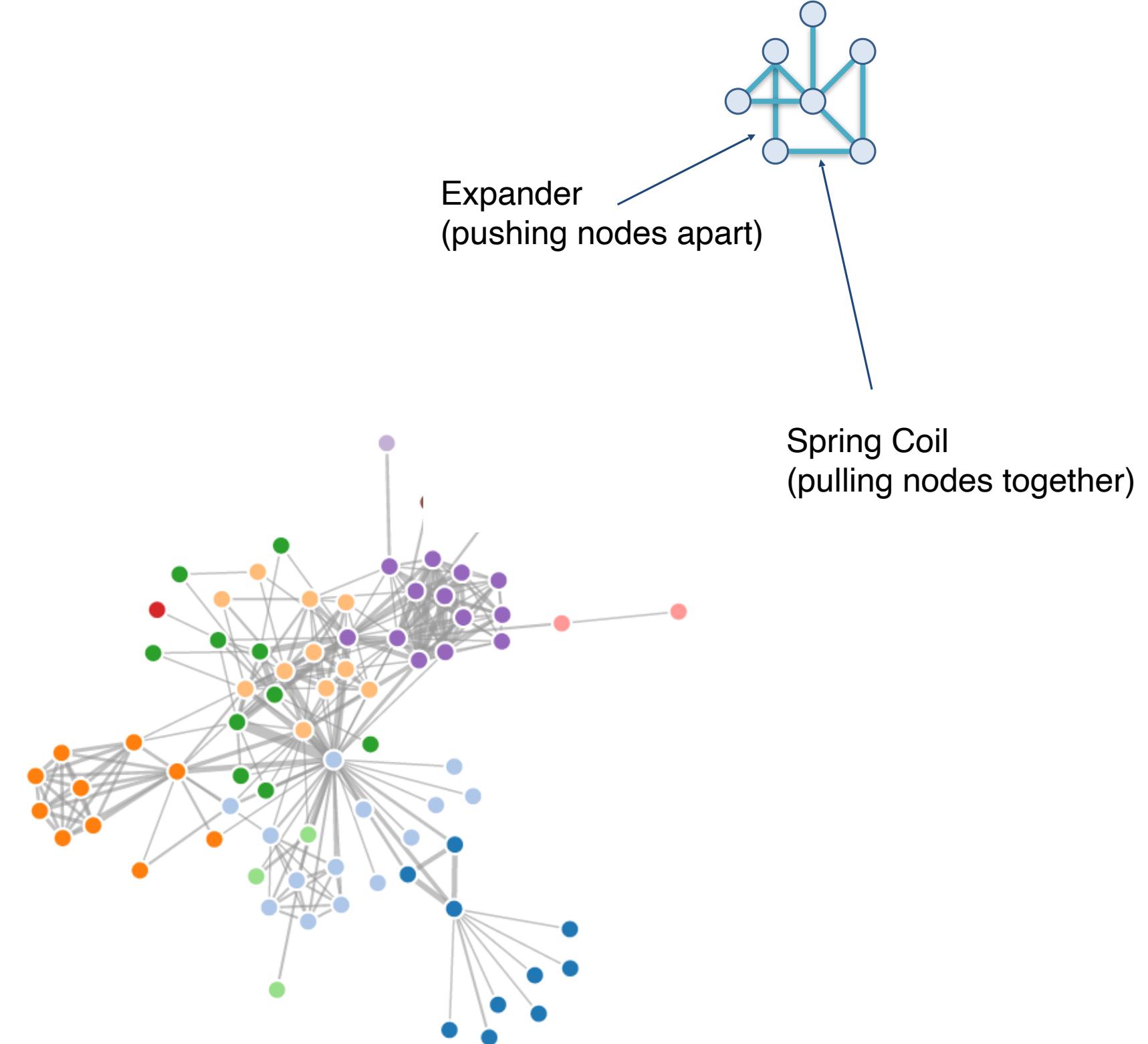
Schulz 2004

# Optimization-based layouts

- formulate layout problem as optimization problem
- convert criteria into weighted cost function
  - $F(\text{layout}) = a * [\text{crossing counts}] + b * [\text{drawing space used}] + \dots$
- use known optimization techniques to find layout at minimal cost
  - energy-based physics models
  - force-directed placement
  - spring embedders

# Force-directed placement

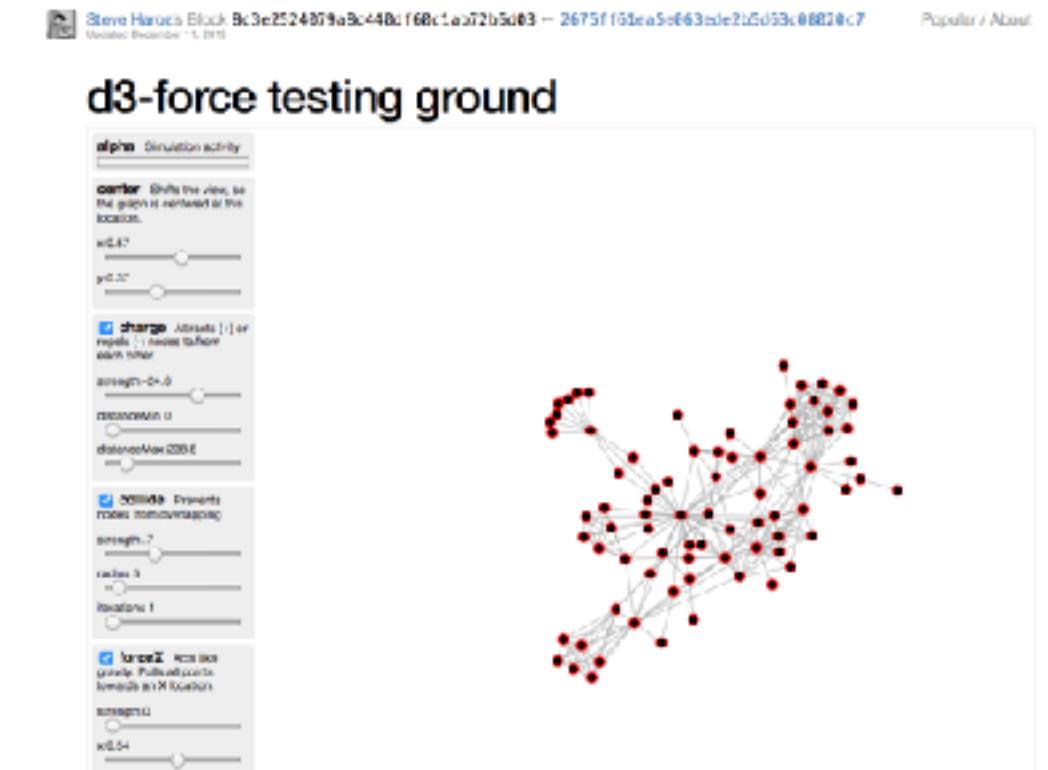
- physics model
  - links = springs pull together
  - nodes = magnets repulse apart
- algorithm
  - place vertices in random locations
  - while not equilibrium
    - calculate force on vertex
      - sum of
        - » pairwise repulsion of all nodes
        - » attraction between connected nodes
    - move vertex by  $c * \text{vertex\_force}$



<http://mbostock.github.com/d3/ex/force.html>

# Force-directed placement properties

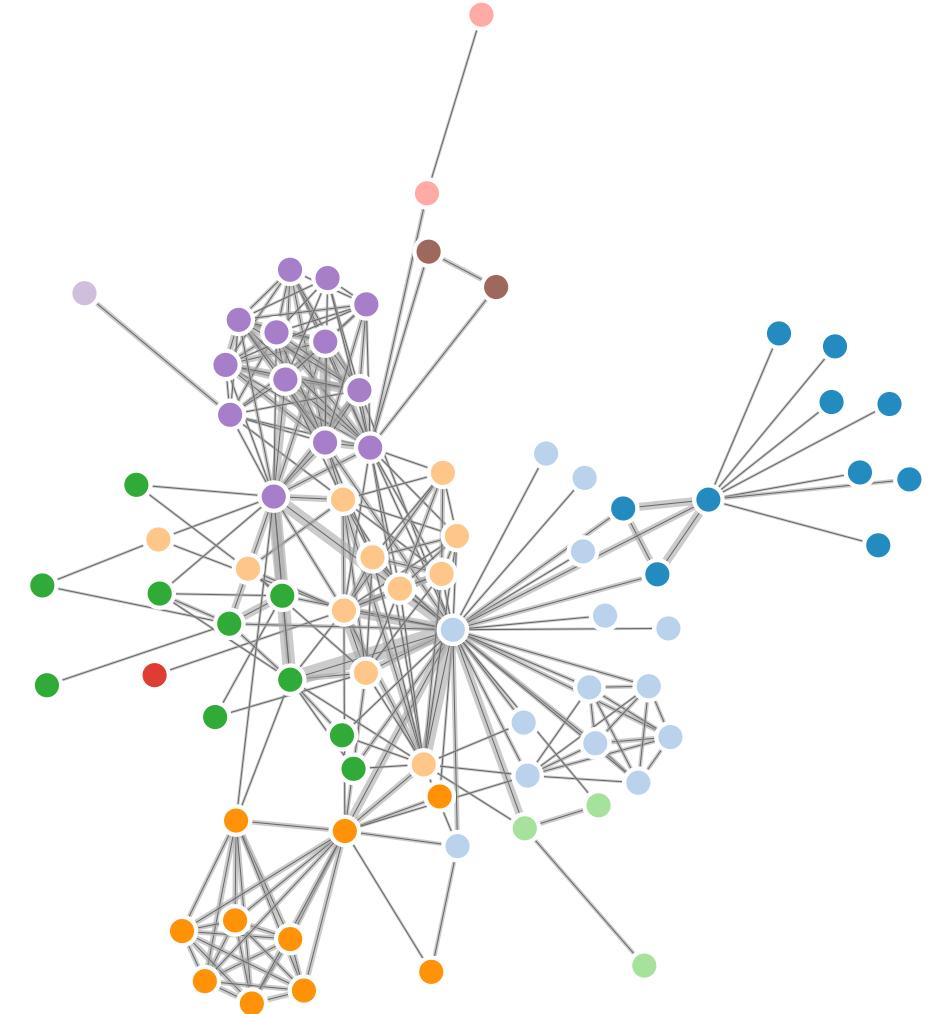
- strengths
  - reasonable layout for small, sparse graphs
  - clusters typically visible
  - edge length uniformity
- weaknesses
  - nondeterministic
  - computationally expensive:  $O(n^3)$  for  $n$  nodes
    - each step is  $n^2$ , takes  $\sim n$  cycles to reach equilibrium
  - naive FD doesn't scale well beyond 1K nodes
  - iterative progress: engaging but distracting



<https://blocks.org/steveharoz/8c3e2524079a8c440df60c1ab72b5d03>

# Idiom: force-directed placement

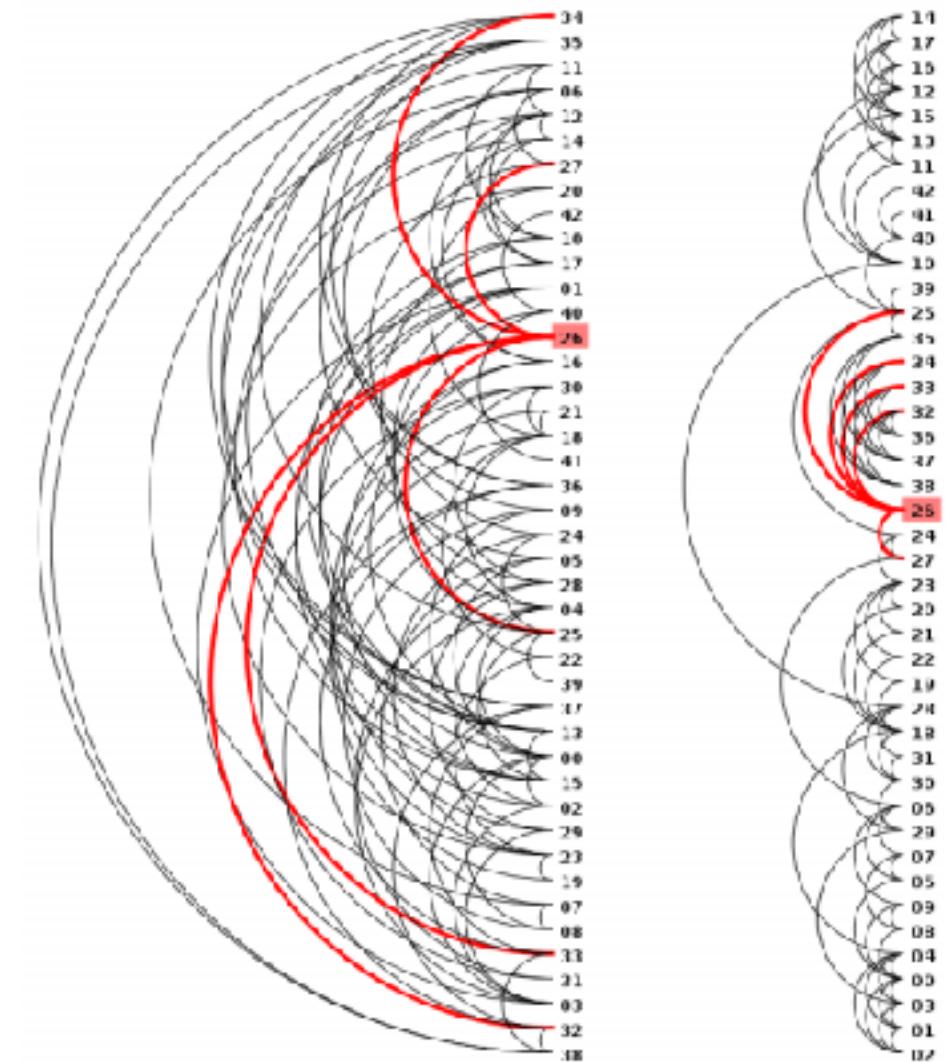
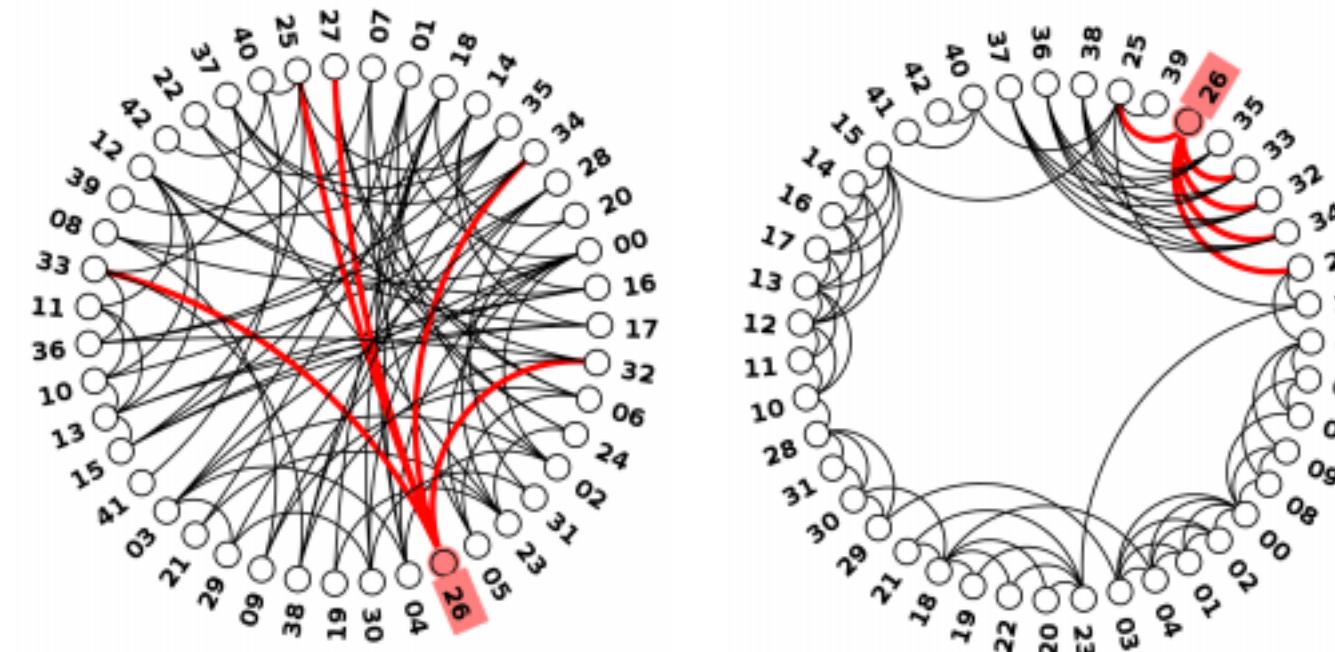
- visual encoding
  - link connection marks, node point marks
- considerations
  - spatial position: no meaning directly encoded
    - left free to minimize crossings
  - proximity semantics?
    - sometimes meaningful
    - sometimes arbitrary, artifact of layout algorithm
    - tension with length
      - long edges more visually salient than short
- tasks
  - explore topology; locate paths, clusters
- scalability
  - node/edge density  $E < 4N$



<http://mbostock.github.com/d3/ex/force.html>

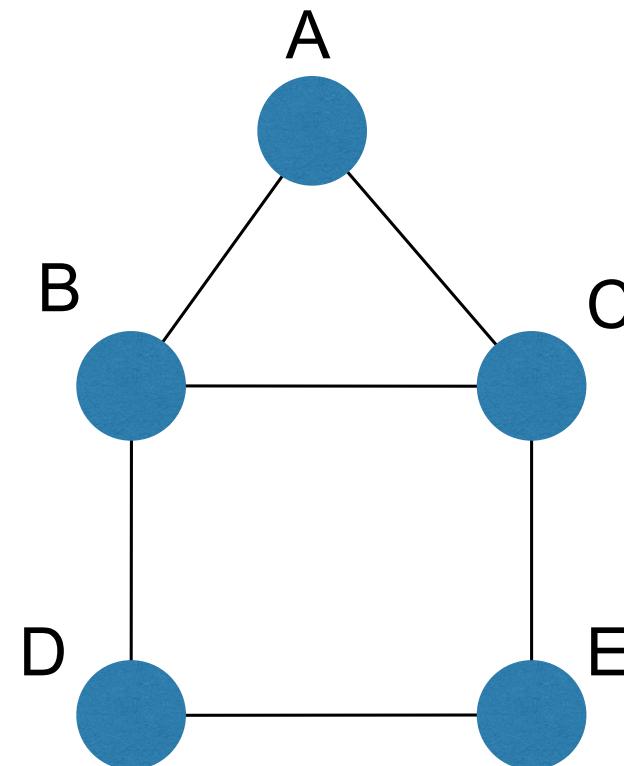
# Idiom: circular layouts / arc diagrams (node-link)

- restricted node-link layouts: lay out nodes around circle or along line
- data
  - original: network
  - derived: node ordering attribute (global computation)
- considerations: node ordering crucial to avoid excessive clutter from edge crossings
  - examples: before & after barycentric ordering



# Adjacency matrix representations

- derive adjacency matrix from network



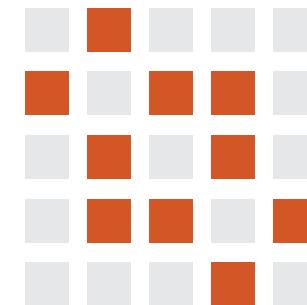
	A	B	C	D	E
A					
B					
C					
D					
E					

## → Adjacency Matrix

Derived Table

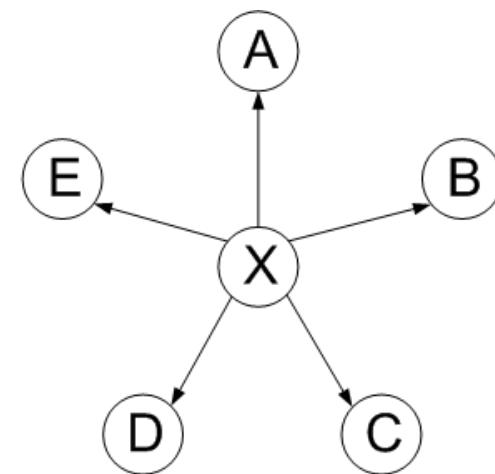
✓ NETWORKS

✓ TREES

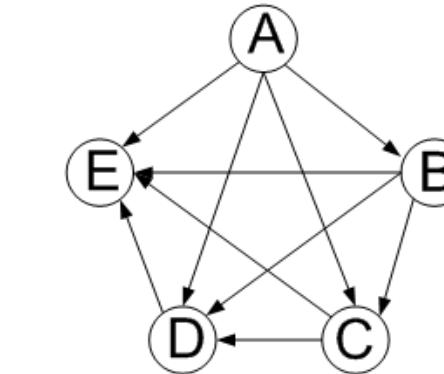


# Adjacency matrix examples

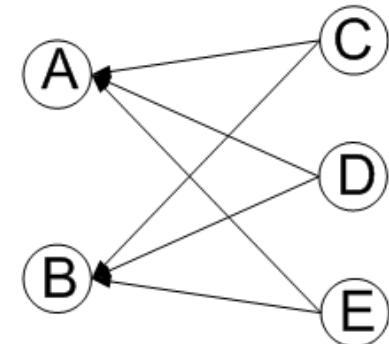
A					
D					
C					
B					
E					
...	X	Y	Z	...	



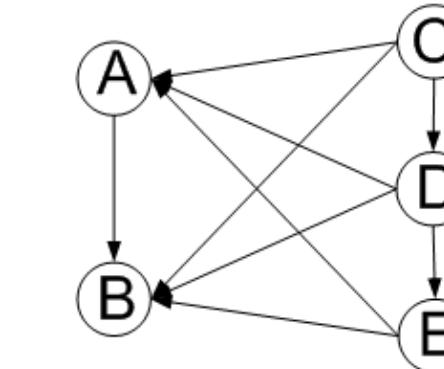
A					
B					
C					
D					
E					
...	A	B	C	D	E



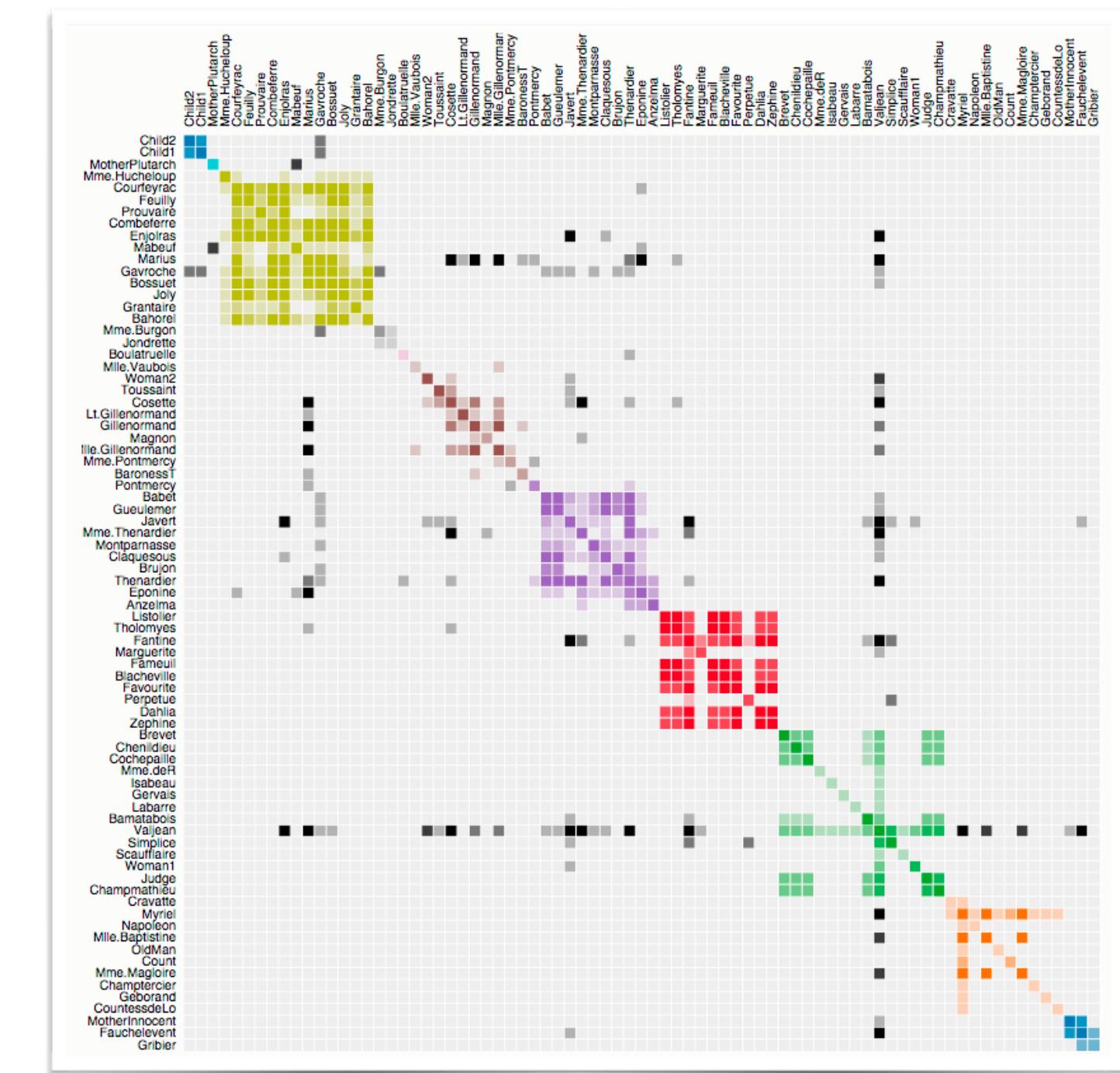
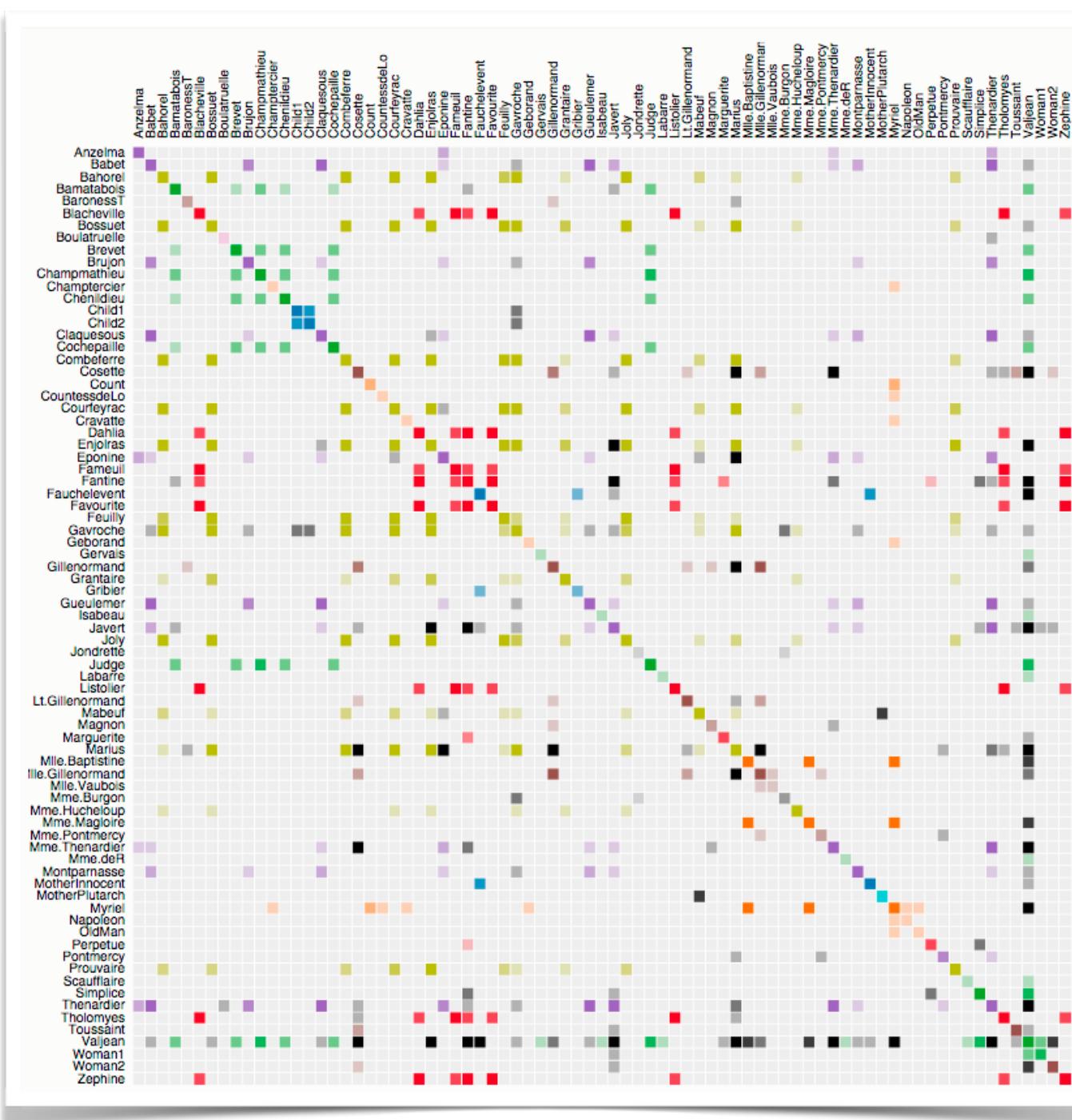
A					
B					
C					
D					
E					
...	A	B	C	D	E



A					
B					
C					
D					
E					
...	A	B	C	D	E



# Node order is crucial: Reordering

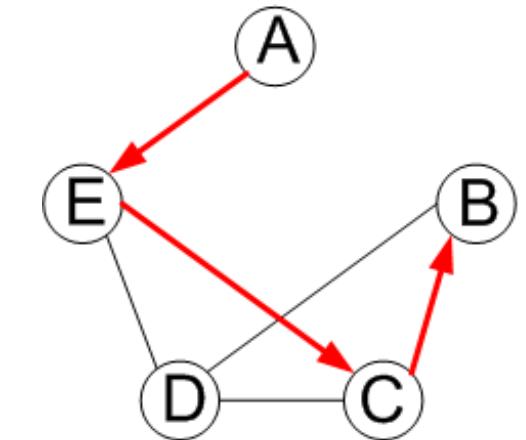


<https://bost.ocks.org/mike/miserables/>

# Adjacency matrix

	A	B	C	D	E	F	G	H
A								
B								
C								
D								
E								
F								
R								
O								
M								
E								
D								
C								
B								
A								

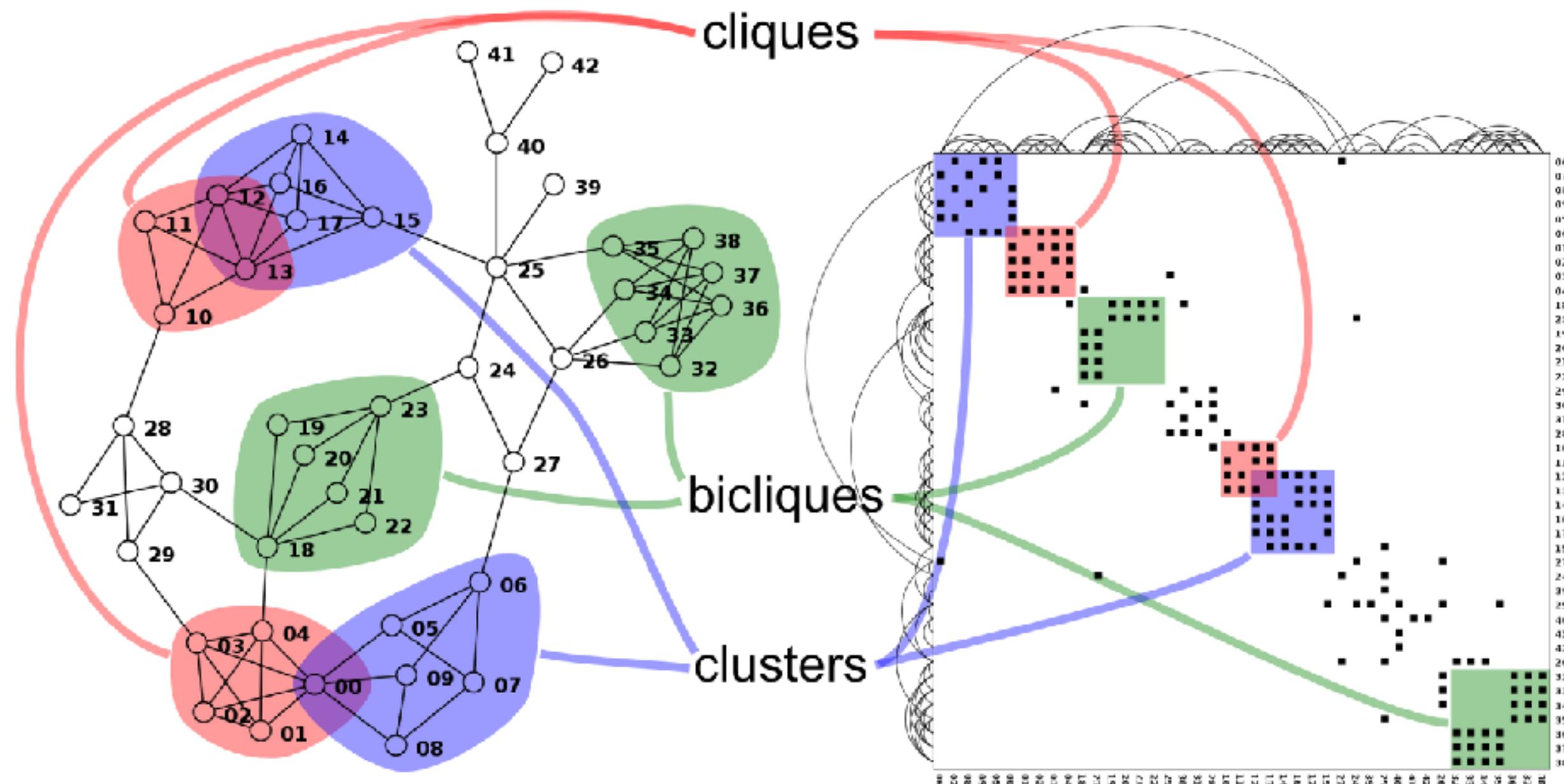
good for topology tasks  
related to neighborhoods  
(node 1-hop neighbors)



	A	B	C	D	E
E				■	■
D				■	■
C					■
B				■	
A					■

bad for topology tasks  
related to paths

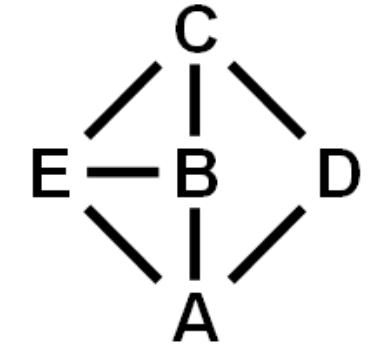
# Structures visible in both



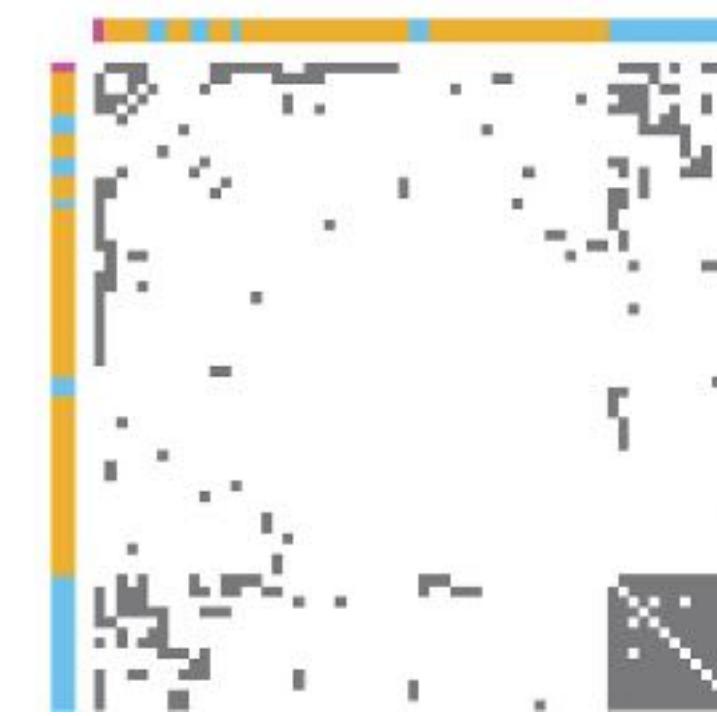
# Idiom: adjacency matrix view

- data: network
  - transform into same data/encoding as heatmap
- derived data: table from network
  - 1 quant attrib
    - weighted edge between nodes
  - 2 categ attribs: node list x 2
- visual encoding
  - cell shows presence/absence of edge
- scalability
  - 1K nodes, 1M edges

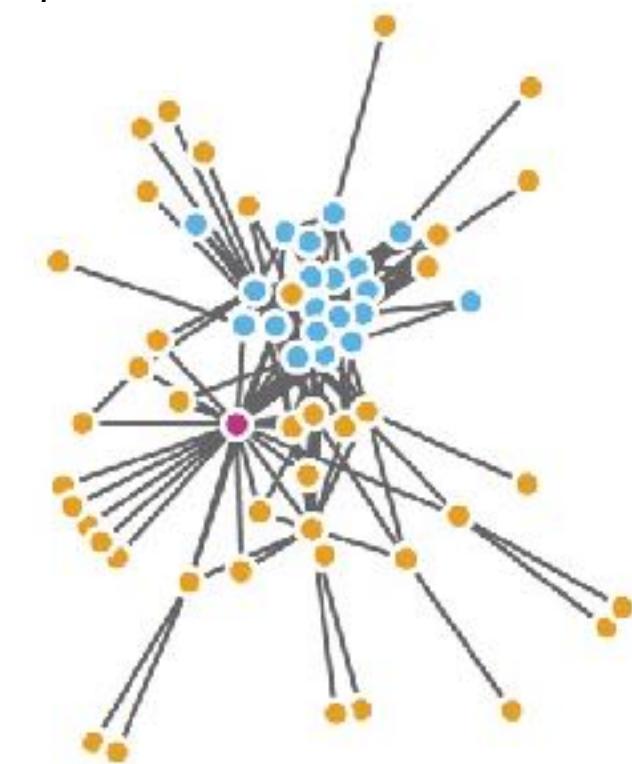
	A	B	C	D	E
A	A				
B		B			
C			C		
D				D	
E					E



[NodeTrix: a Hybrid Visualization of Social Networks.  
Henry, Fekete, and McGuffin. IEEE TVCG (Proc. InfoVis)  
13(6):1302-1309, 2007.]

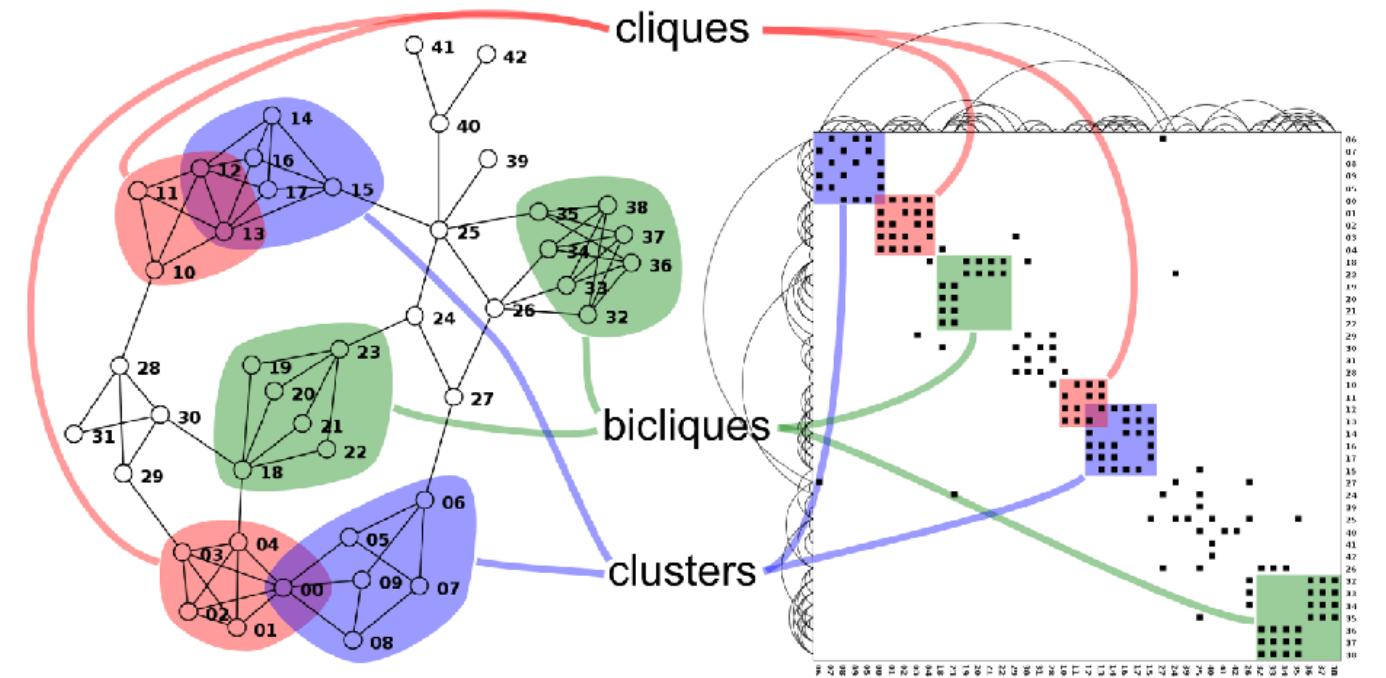


[Points of view: Networks. Gehlenborg and Wong. Nature Methods 9:115.]



# Node-link vs. matrix comparison

- node-link diagram strengths
  - topology understanding, path tracing
  - intuitive, flexible, no training needed
- adjacency matrix strengths
  - focus on edges rather than nodes
  - layout straightforward (reordering needed)
  - predictability, scalability
  - some topology tasks trainable
- empirical study
  - node-link best for small networks
  - matrix best for large networks
    - if tasks don't involve path tracing!

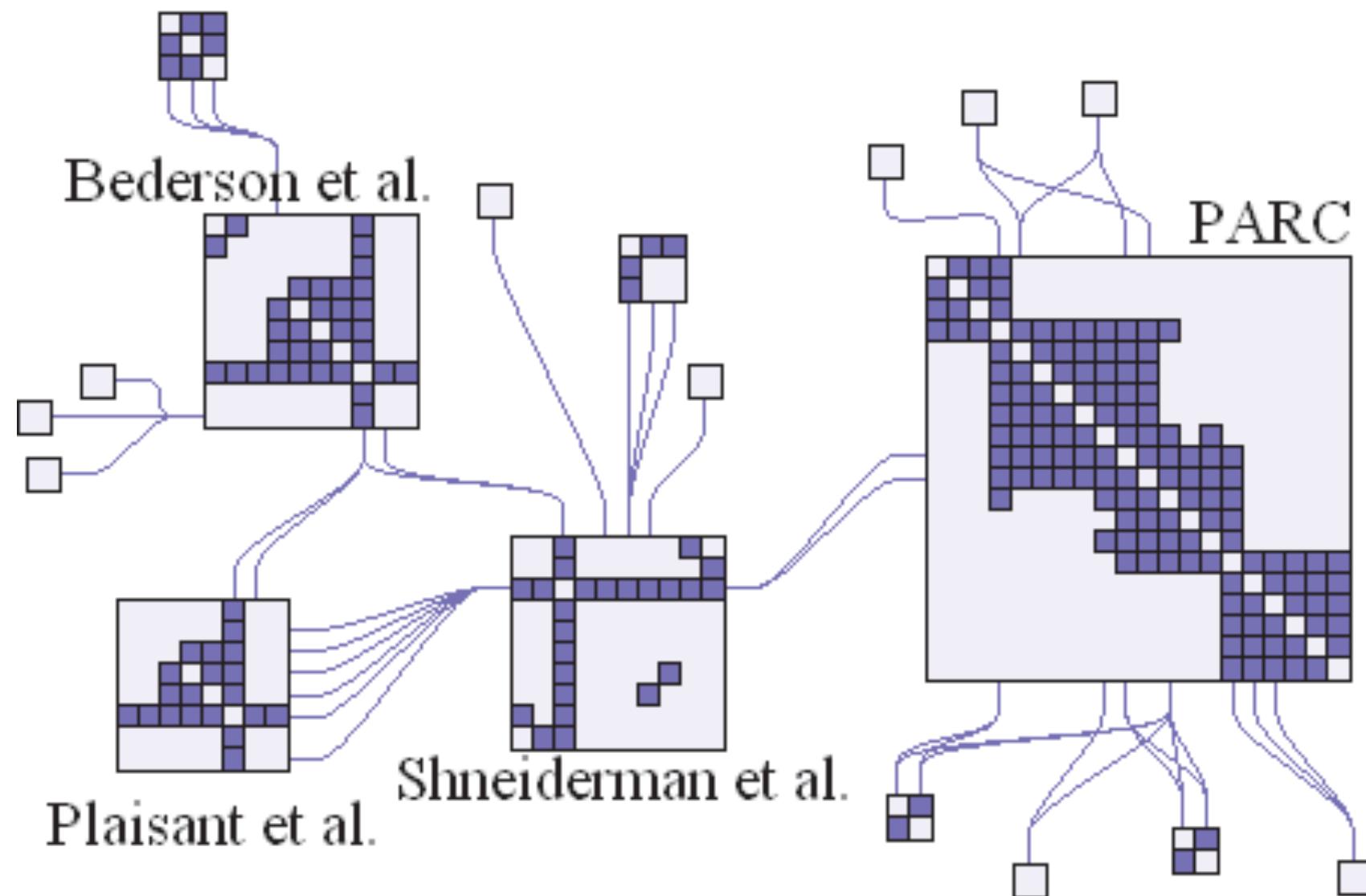


<http://www.michaelmcguffin.com/courses/vis/patternsInAdjacencyMatrix.png>

[On the readability of graphs using node-link and matrix-based representations: a controlled experiment and statistical analysis. Ghoniem, Fekete, and Castagliola. Information Visualization 4:2 (2005), 114–135.]

# Idiom: NodeTrix

- hybrid nodelink/matrix
- capture strengths of both



[*NodeTrix: a Hybrid Visualization of Social Networks.*  
Henry, Fekete, and McGuffin. IEEE TVCG (Proc. InfoVis)  
13(6):1302-1309, 2007.]

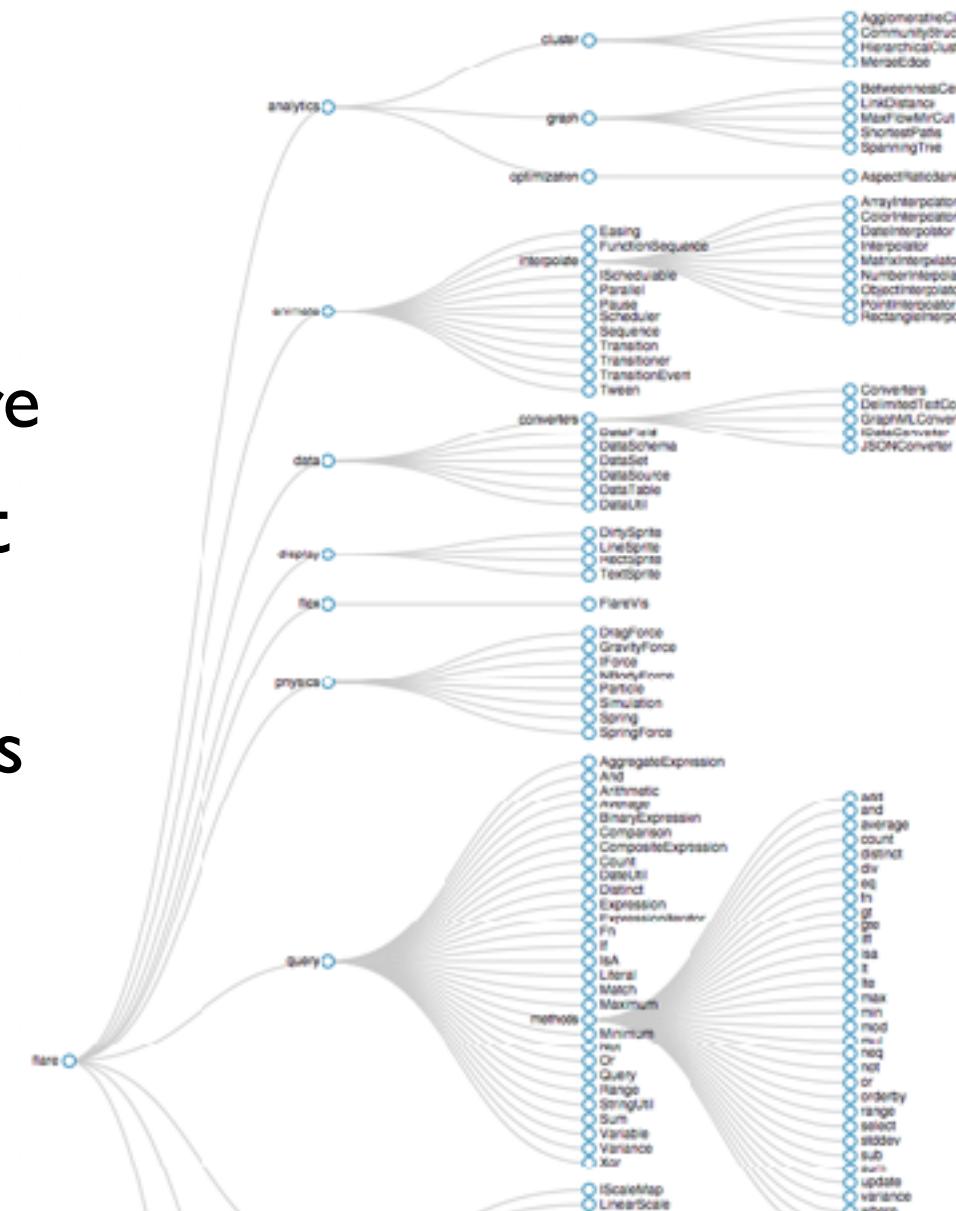
# Trees

# Node-link trees

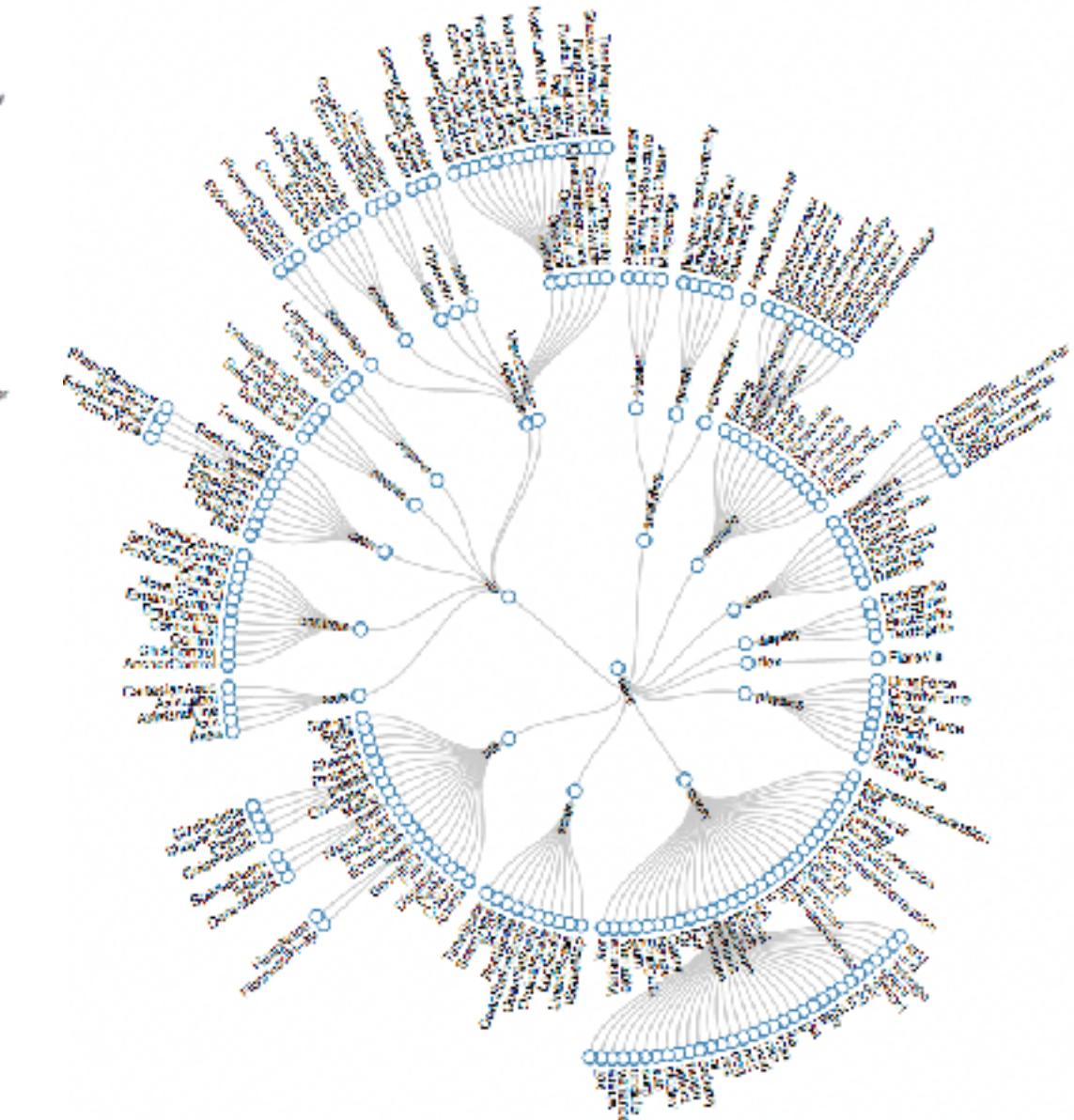
- Reingold-Tilford
  - tidy drawings of trees
    - exploit parent/child structure
  - allocate space: compact but without overlap
    - rectilinear and radial variants

[Tidier drawing of trees. Reingold and Tilford. IEEE Trans. Software Eng., SE-7(2):223–228, 1981.]

- nice algorithm writeup
  - <http://billmill.org/pymag-trees/>



<http://bl.ocks.org/mbostock/4339184>

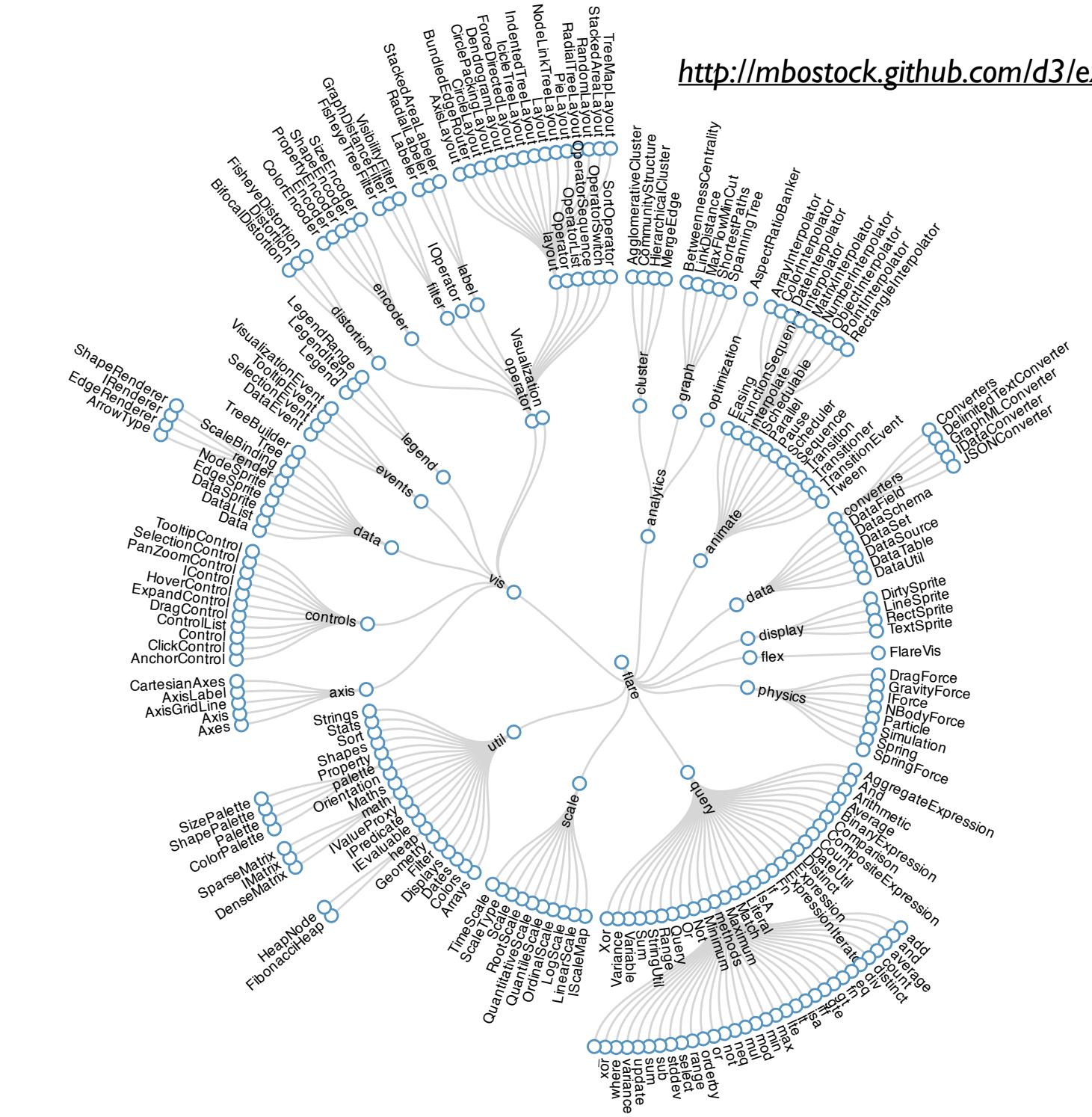


<http://bl.ocks.org/mbostock/4063550>

# Idiom: radial node-link tree

<http://mbostock.github.com/d3/ex/tree.html>

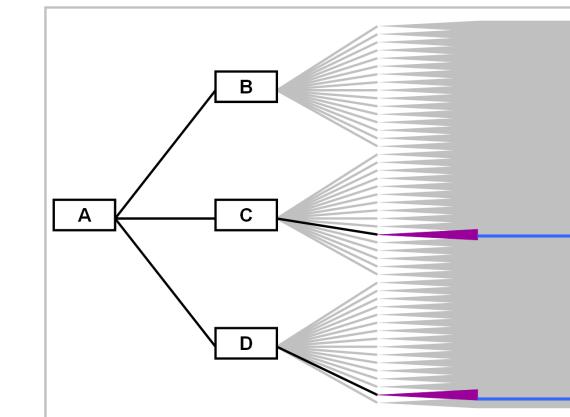
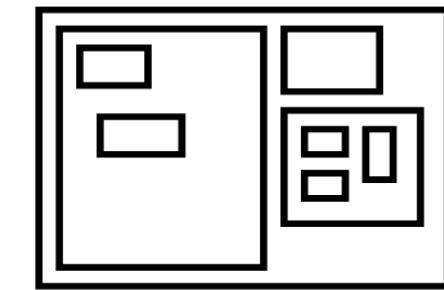
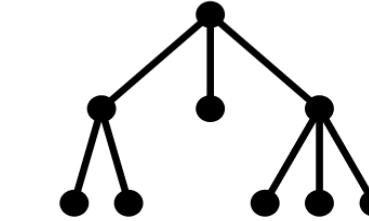
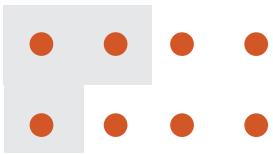
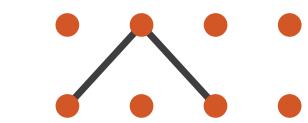
- data
    - tree
  - encoding
    - link connection marks
    - point node marks
    - radial axis orientation
      - angular proximity: siblings
      - distance from center: depth in tree
  - tasks
    - understanding topology, following paths
  - scalability
    - 1K - 10K nodes (with/without labels)



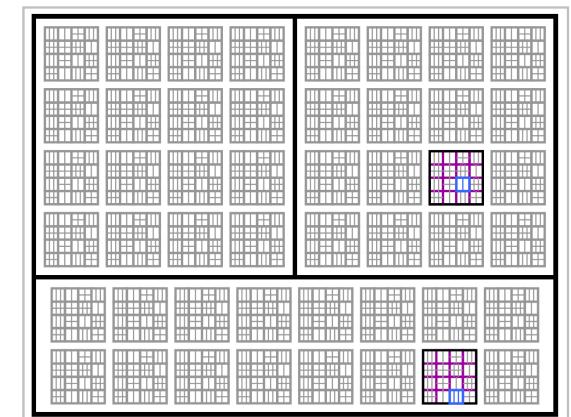
# Link marks: Connection and containment

- marks as links (vs. nodes)
  - common case in network drawing
  - 1D case: connection
    - ex: all node-link diagrams
    - emphasizes topology, path tracing
    - networks and trees
  - 2D case: containment
    - ex: all treemap variants
    - emphasizes attribute values at leaves (size coding)
    - only trees

→ Connection → Containment



Node-Link Diagram



Treemap

[*Elastic Hierarchies: Combining Treemaps and Node-Link Diagrams.*  
Dong, McGuffin, and Chignell. Proc. InfoVis 2005, p. 57-64.]

# Idiom: treemap

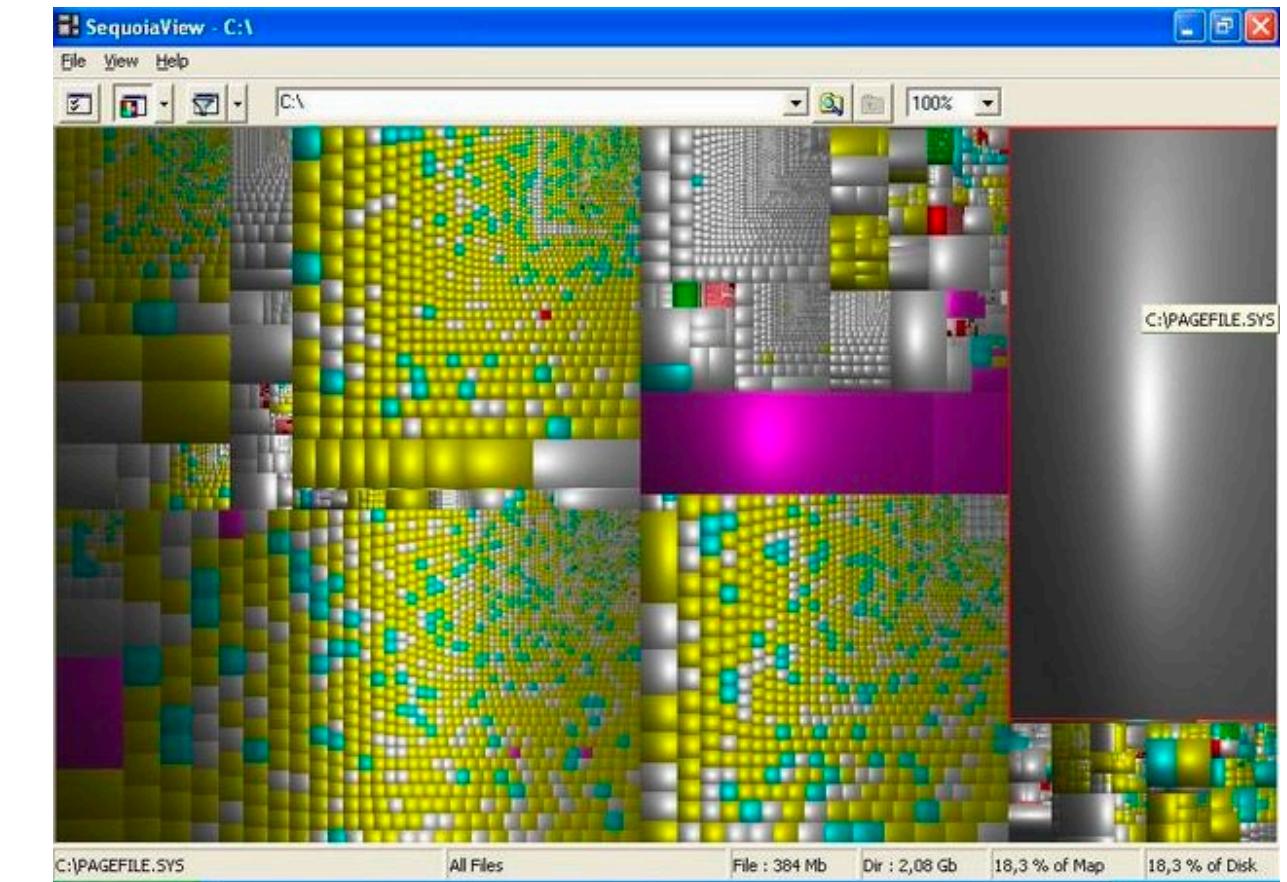
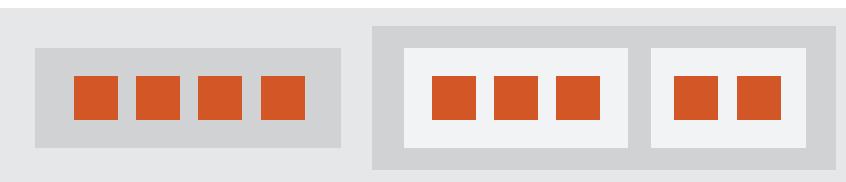
- data
  - tree
  - 1 quant attrib at leaf nodes
- encoding
  - area containment marks for hierarchical structure
  - rectilinear orientation
  - size encodes quant attrib
- tasks
  - query attribute at leaf nodes
  - ex: disk space usage within filesystem
- scalability
  - 1M leaf nodes

## → Enclosure

Containment Marks

NETWORKS

TREES



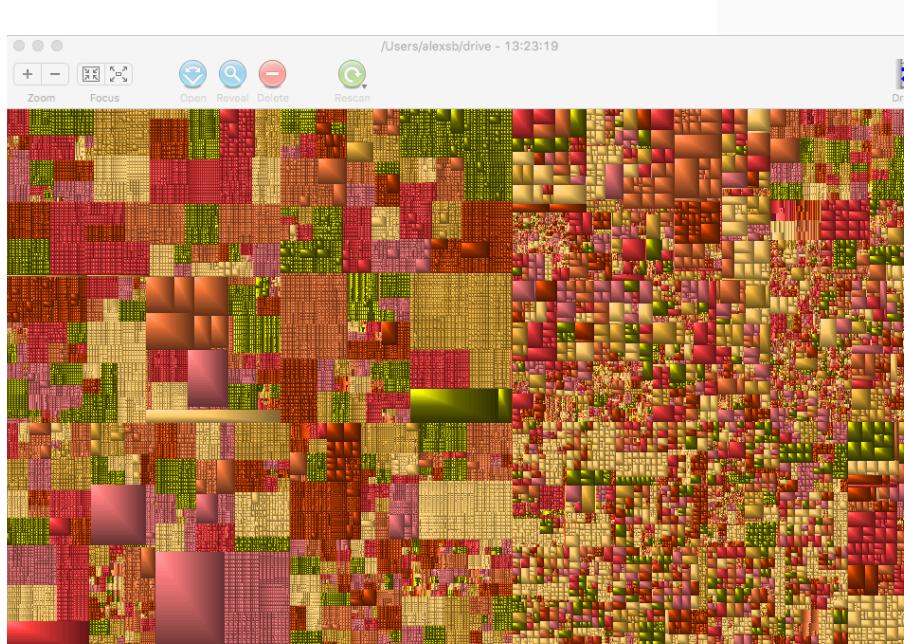
<https://www.win.tue.nl/sequoiaview/>

[Cushion Treemaps. van Wijk and van de Wetering.  
Proc. Symp. InfoVis 1999, 73-78.]

# Idiom: implicit tree layouts (sunburst, icicle plot)

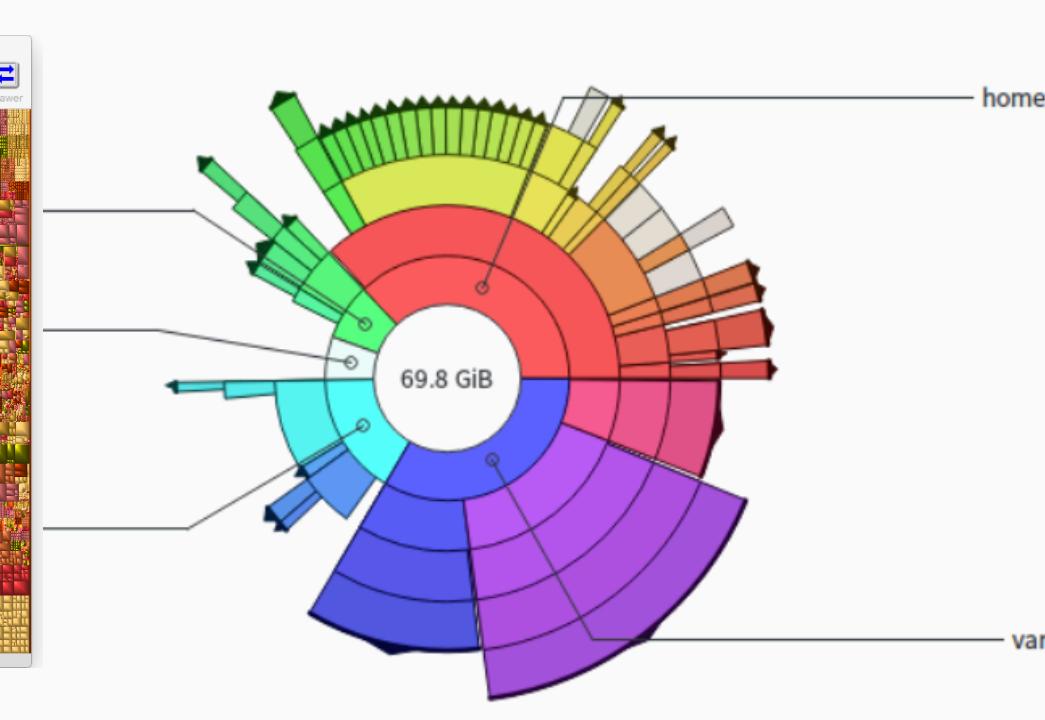
- alternative to connection and containment: position
    - show parent-child relationships only through relative positions

# Treemap containment



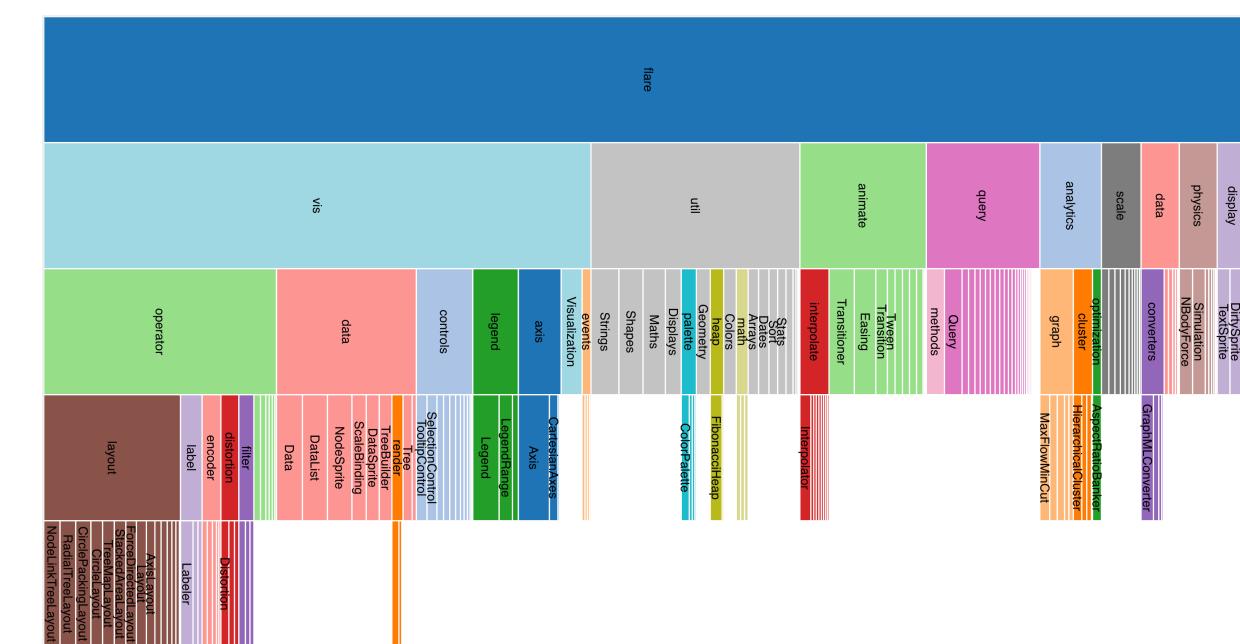
# Sunburst

## position (radial)



# Icicle Plot

## position (rectilinear)



# Idiom: implicit tree layouts (sunburst, icicle plot)

- alternative to connection and containment: position
  - show parent-child relationships only through relative positions

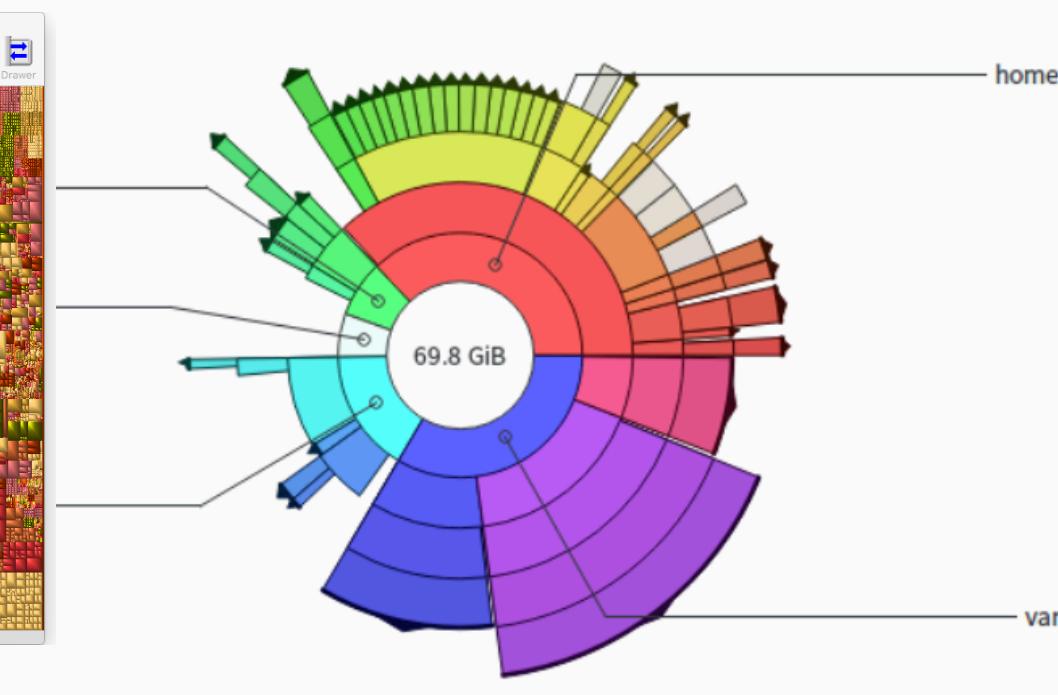
Treemap

containment  
only leaves visible



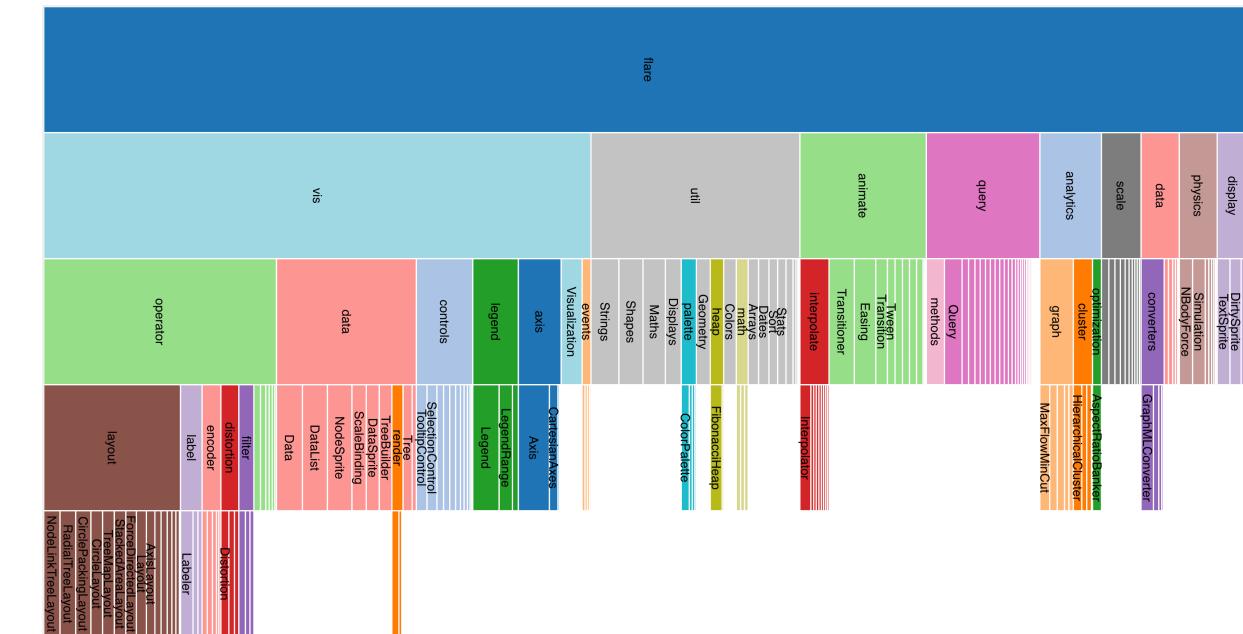
Sunburst

position (radial)  
inner nodes & leaves visible



Icicle Plot

position (rectilinear)  
inner nodes & leaves visible



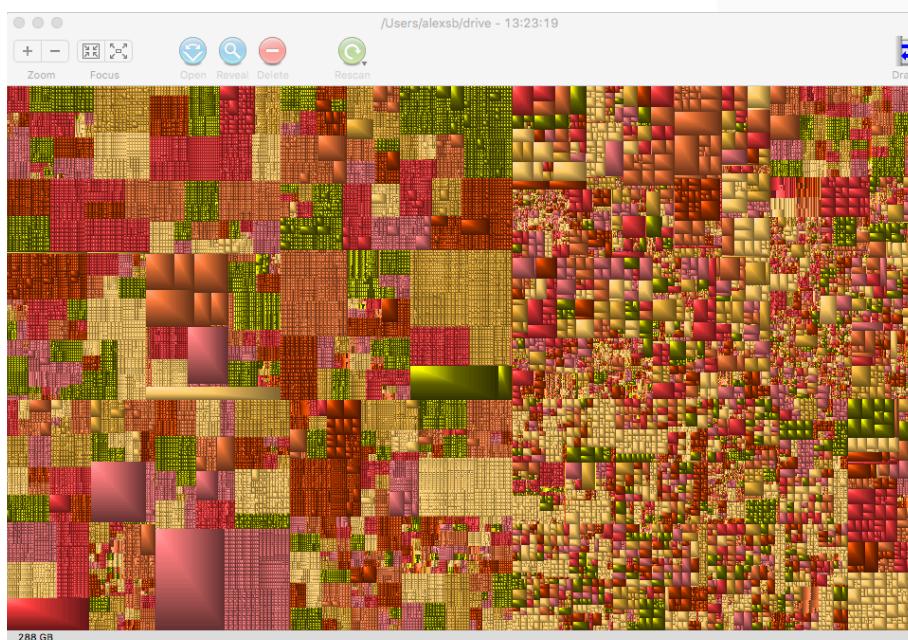
# Idiom: implicit tree layouts (sunburst, icicle plot)

- alternative to connection and containment: position
  - show parent-child relationships only through relative positions

Treemap

containment

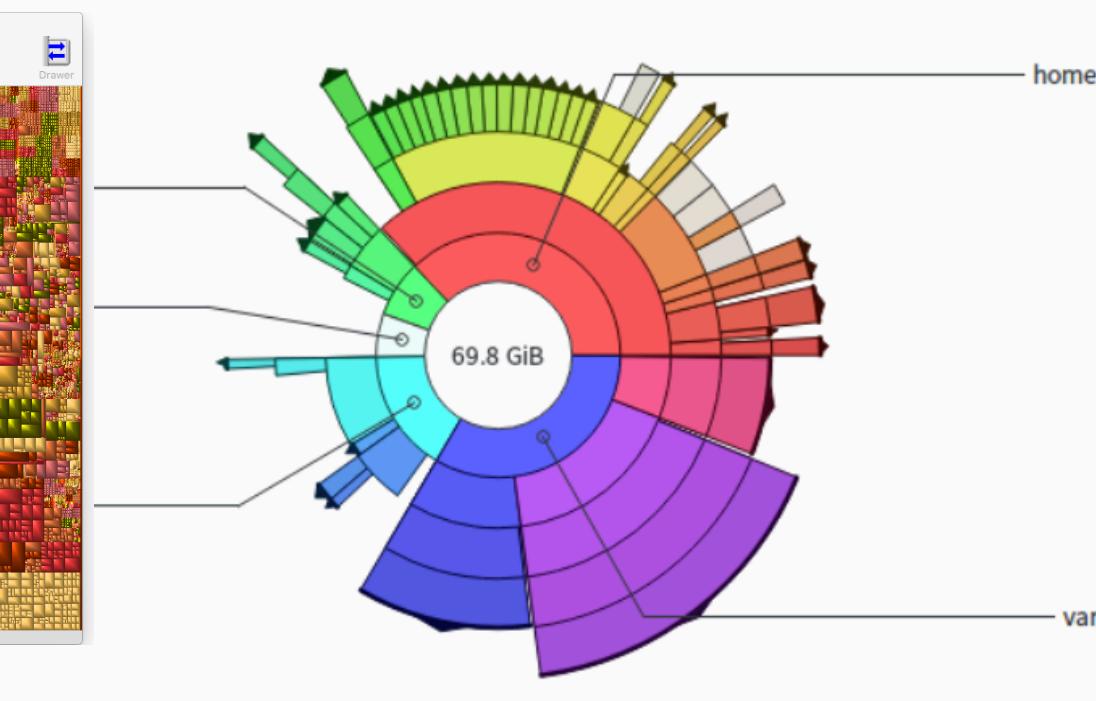
only leaves visible



Sunburst

position (radial)

inner nodes & leaves visible



Implicit  
Spatial Position

✗ NETWORKS

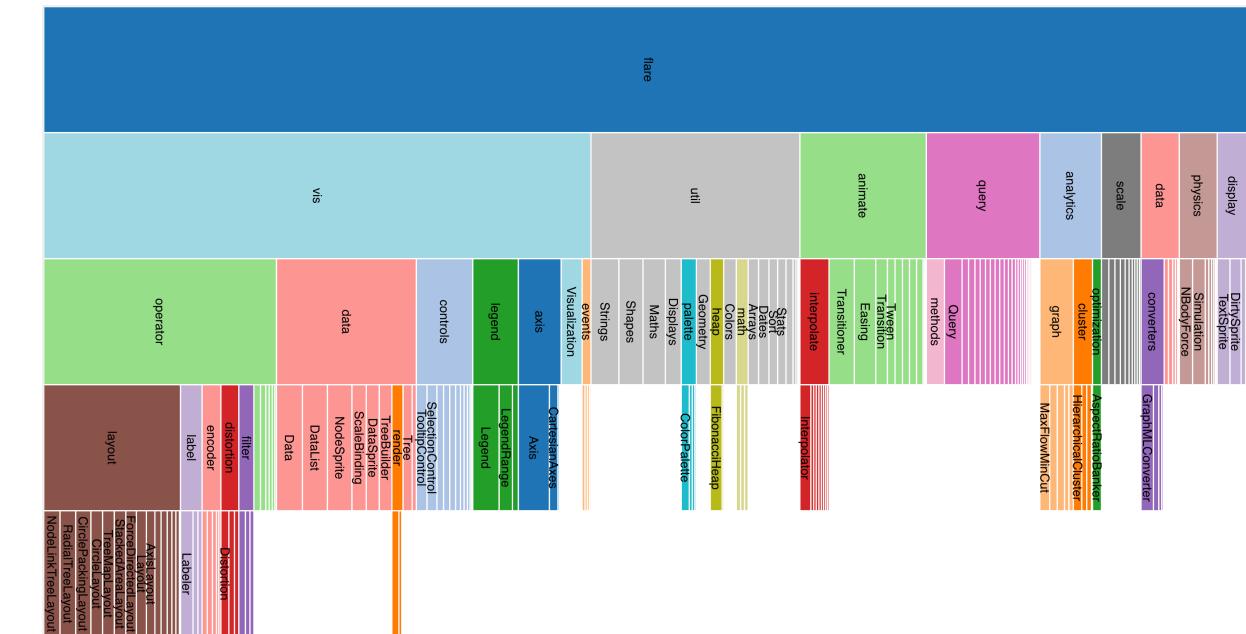
✓ TREES



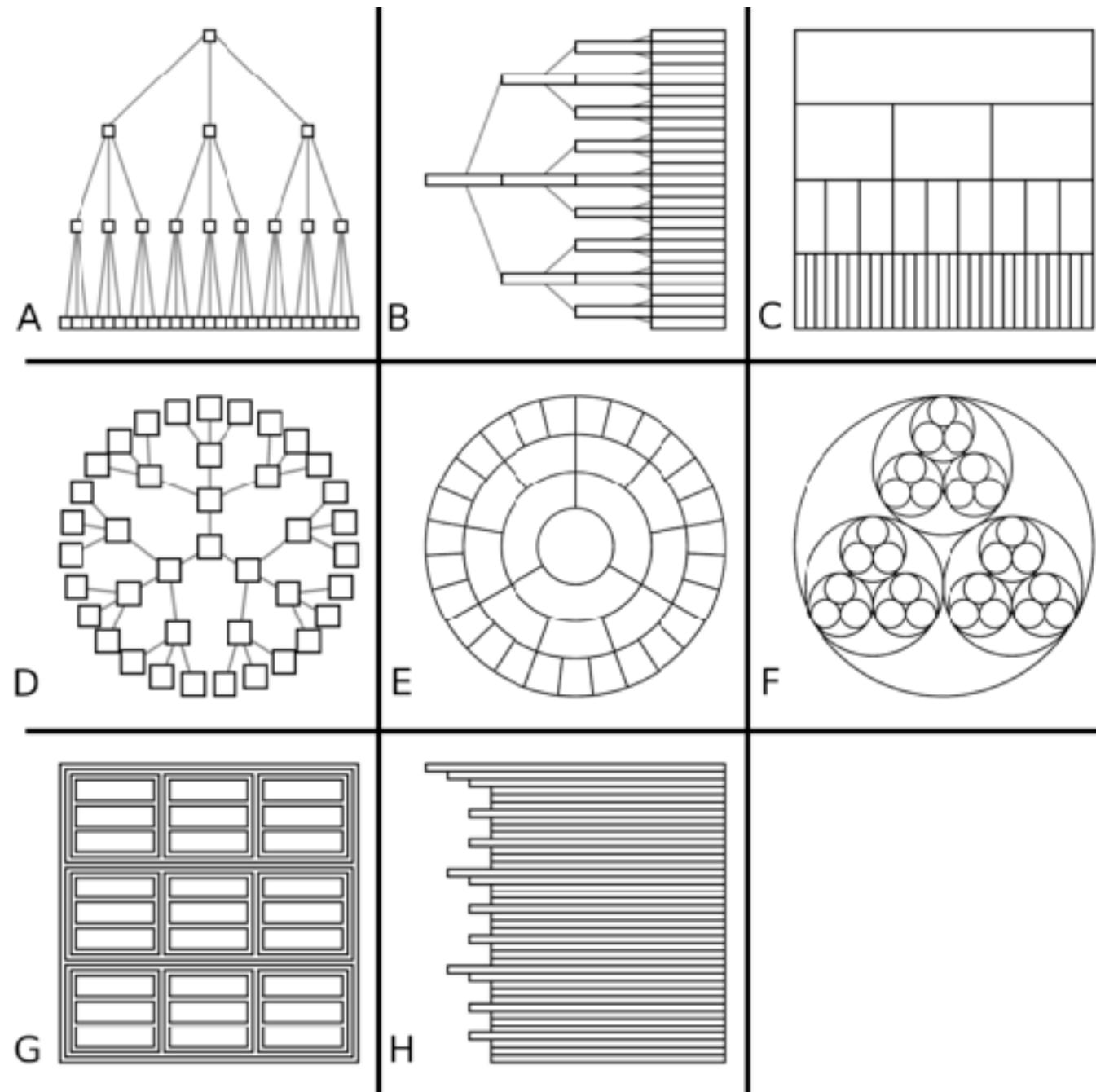
Icicle Plot

position (rectilinear)

inner nodes & leaves visible

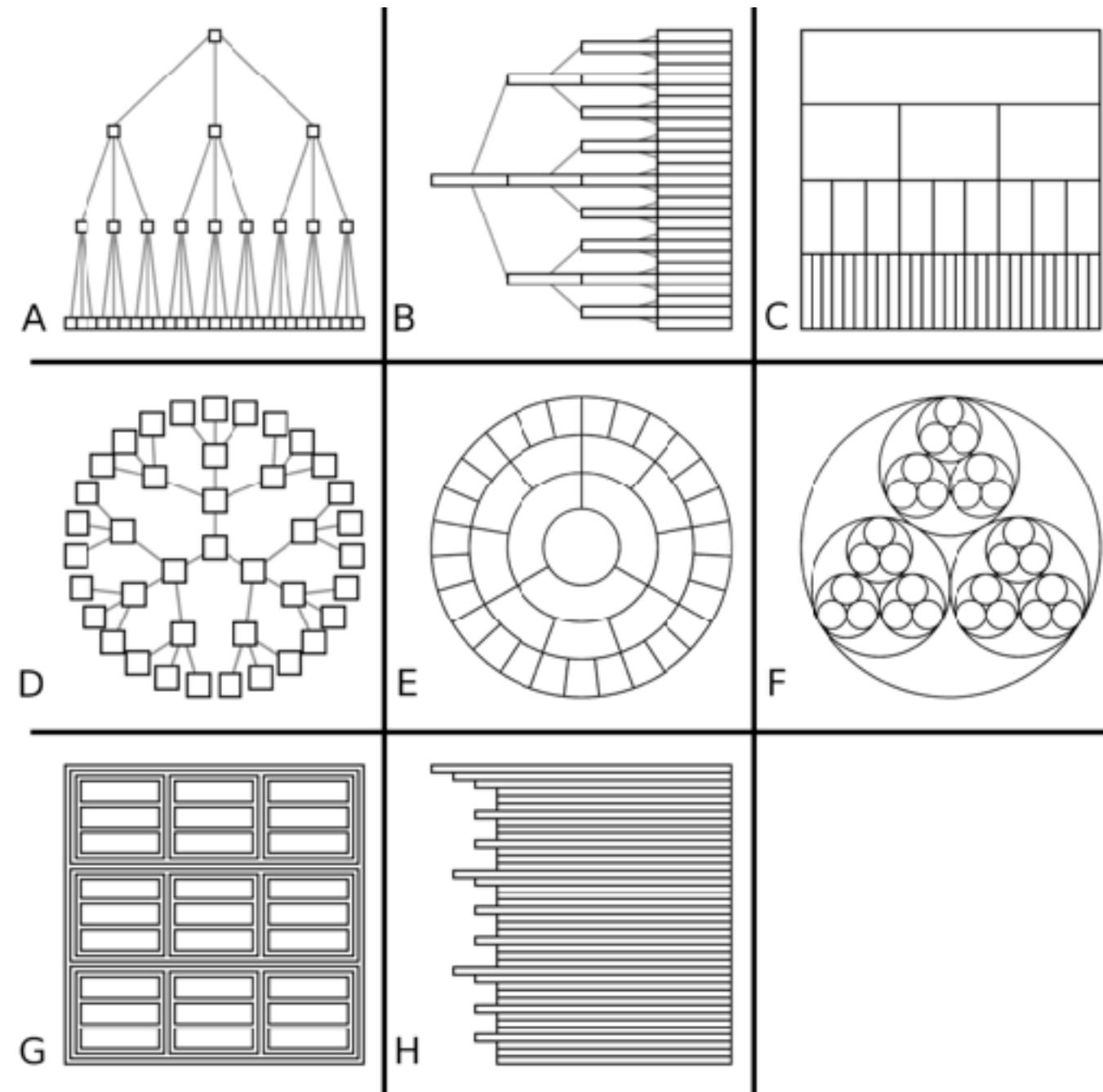


# Tree drawing idioms comparison



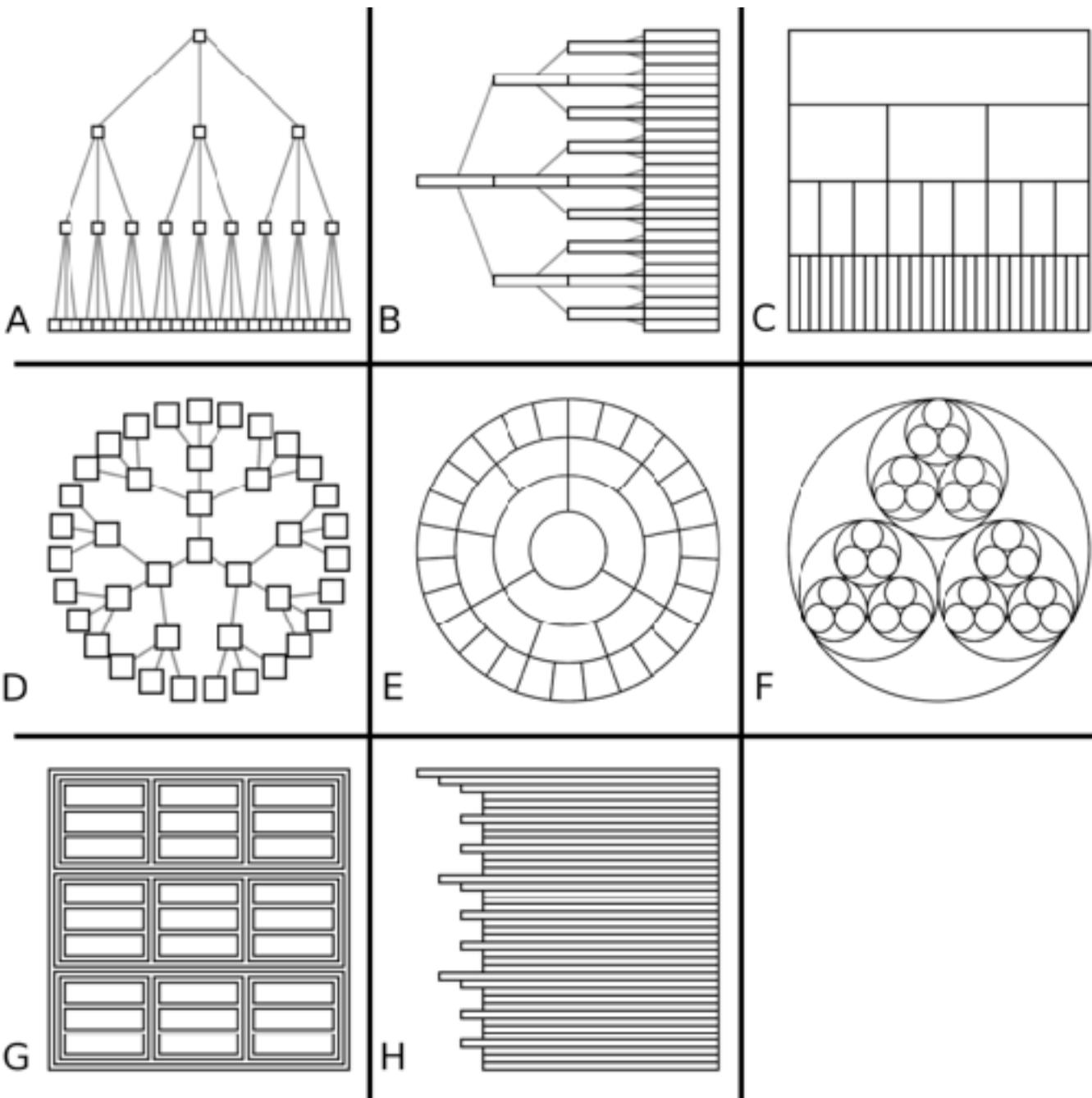
# Comparison: tree drawing idioms

- data shown
  - link relationships
  - tree depth
  - sibling order



# Comparison: tree drawing idioms

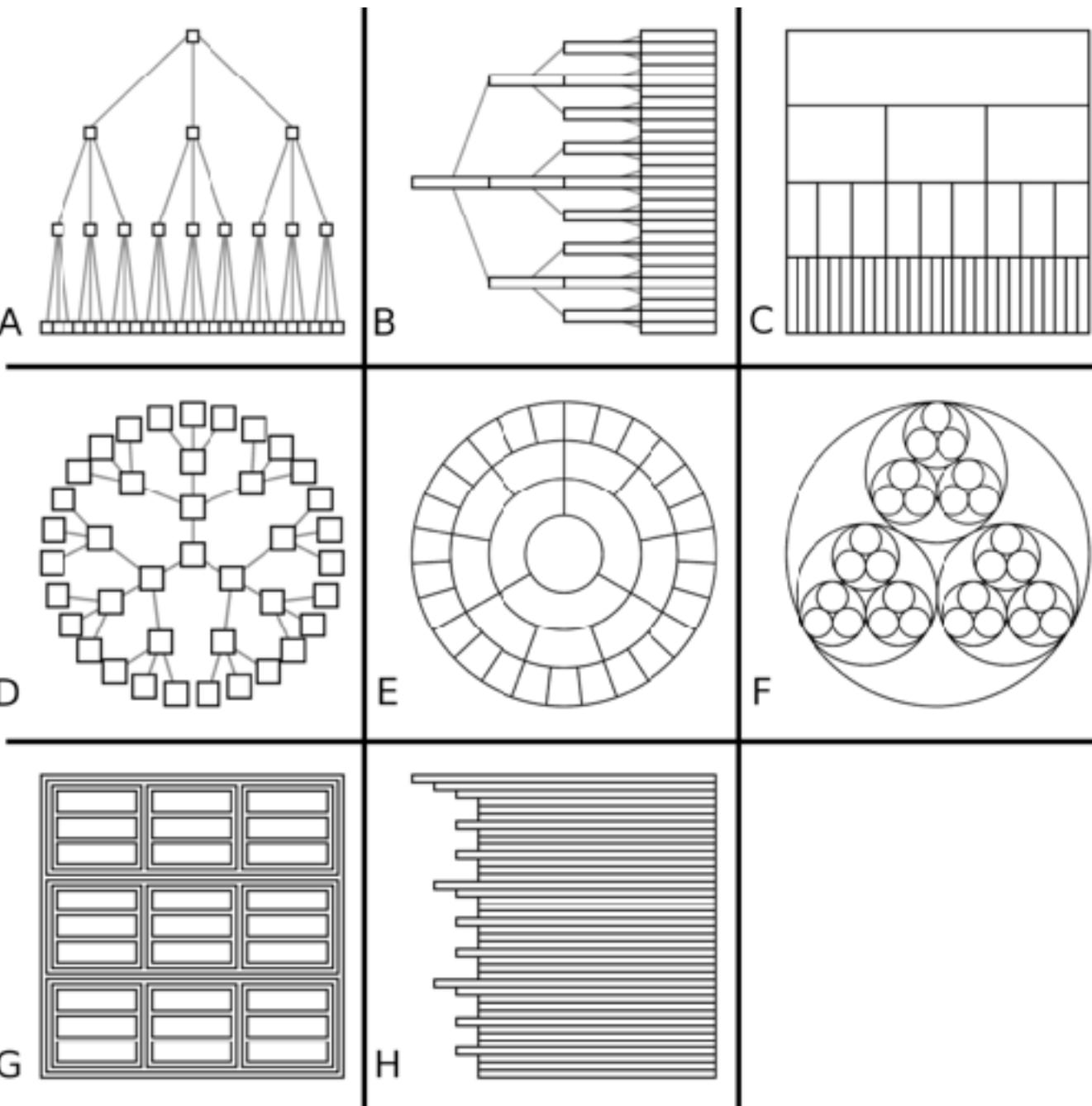
- data shown
  - link relationships
  - tree depth
  - sibling order
- design choices
  - connection vs containment link marks
  - rectilinear vs radial layout
  - spatial position channels



[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees.  
McGuffin and Robert. *Information Visualization* 9:2 (2010), 115–140.]

# Comparison: tree drawing idioms

- data shown
  - link relationships
  - tree depth
  - sibling order
- design choices
  - connection vs containment link marks
  - rectilinear vs radial layout
  - spatial position channels
- considerations
  - redundant? arbitrary?
  - information density?
    - avoid wasting space
    - consider where to fit labels!



# treevis.net: Many, many options!

How to cite this site?  
Check out other surveys

treevis.net - A Visual Bibliography of Tree Visualization 2.0 by Hans-Jörg Schulz v.21-OCT-2014

Dimensionality      Representation      Alignment      Fulltext Search      Techniques Shown

All      All      All      277

The website displays a collection of 277 different tree visualization techniques, each represented by a small thumbnail image. The thumbnails are arranged in a grid of 10 rows and 12 columns. The techniques vary widely in their visual style and complexity, including circular dendograms, hierarchical tree structures, radial trees, treemaps, and various 3D and 2D representations of hierarchical data. The thumbnails are arranged in a grid of 10 rows and 12 columns.

<https://treevis.net/>

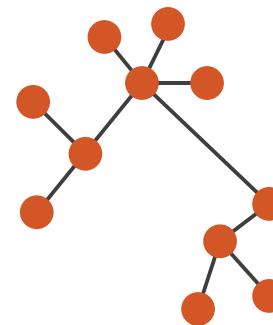
# Arrange networks and trees

## → Node–Link Diagrams

Connection Marks

NETWORKS

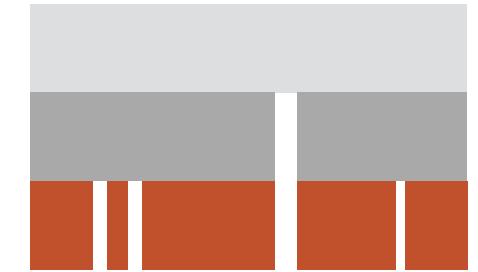
TREES



## → Implicit Spatial Position

NETWORKS

TREES

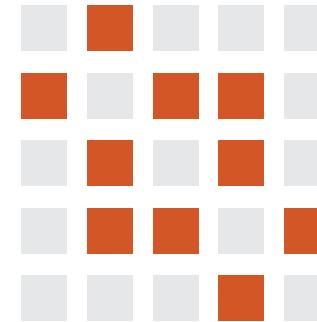


## → Adjacency Matrix

Derived Table

NETWORKS

TREES

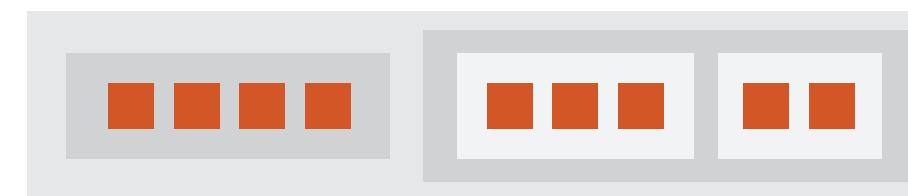


## → Enclosure

Containment Marks

NETWORKS

TREES



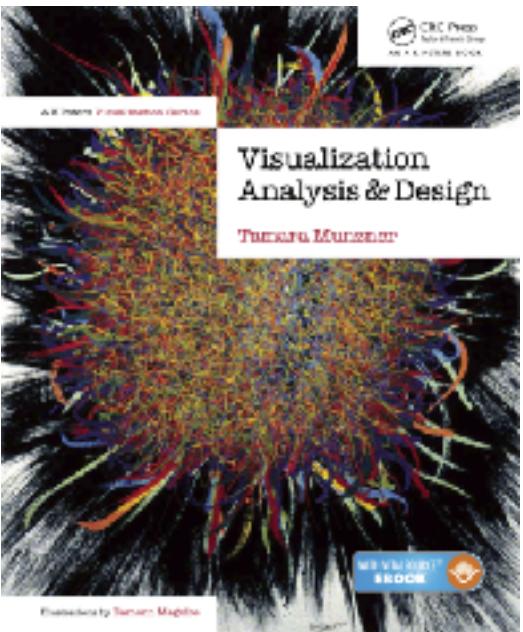
# Visualization Analysis & Design

## *Network Data (Ch 9) II*

**Tamara Munzner**

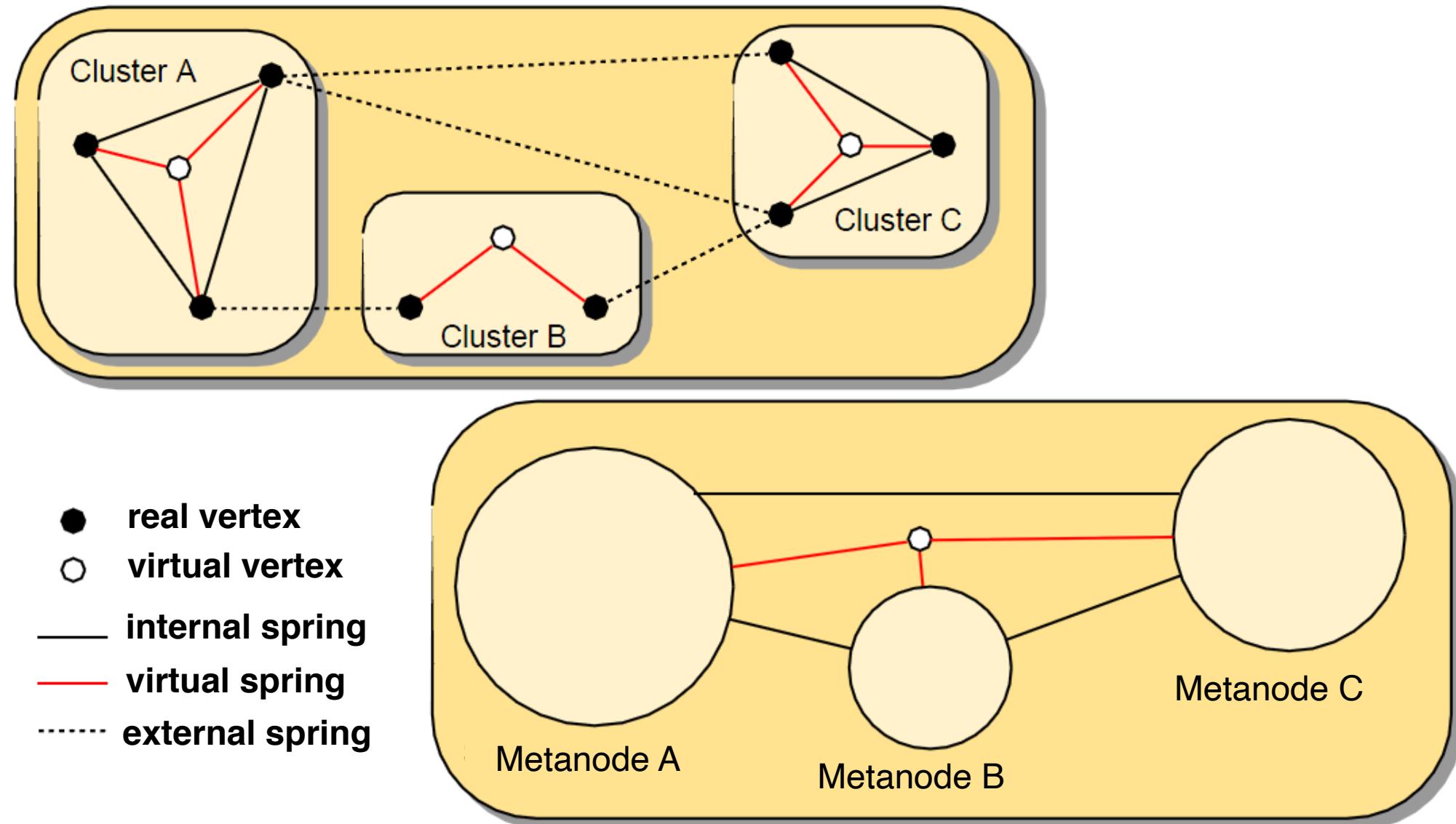
Department of Computer Science  
University of British Columbia

[@tamaramunzner](#)

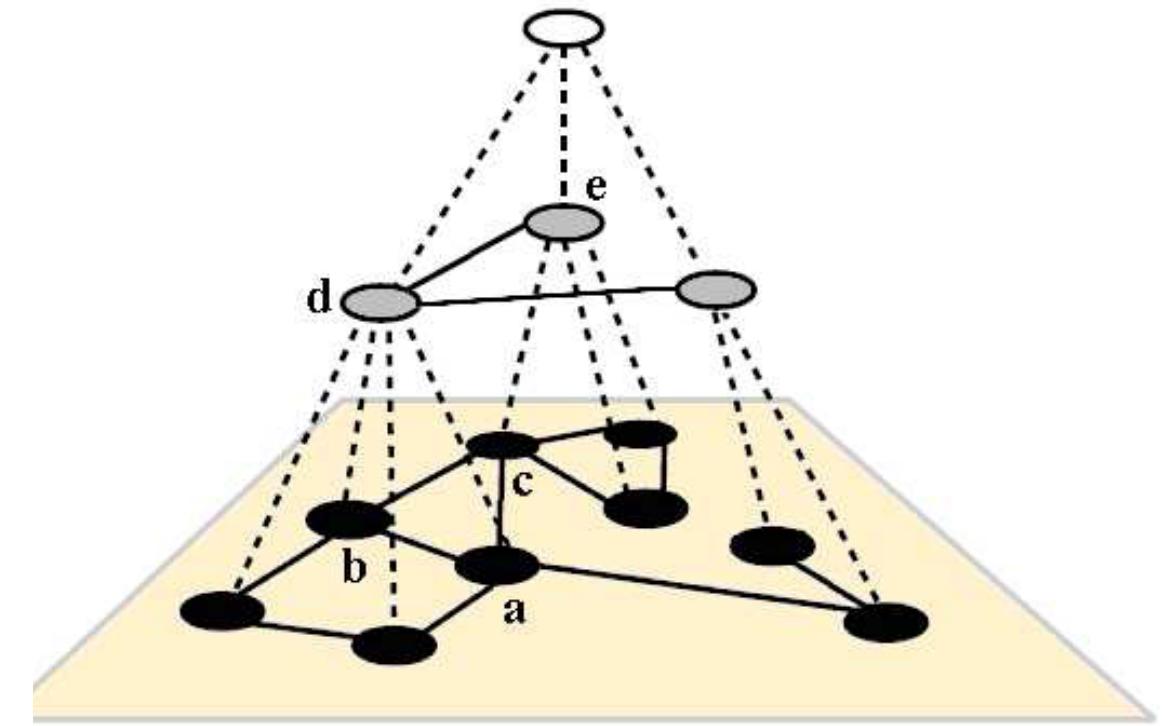


# Multilevel networks

- derive cluster hierarchy of metanodes on top of original graph nodes

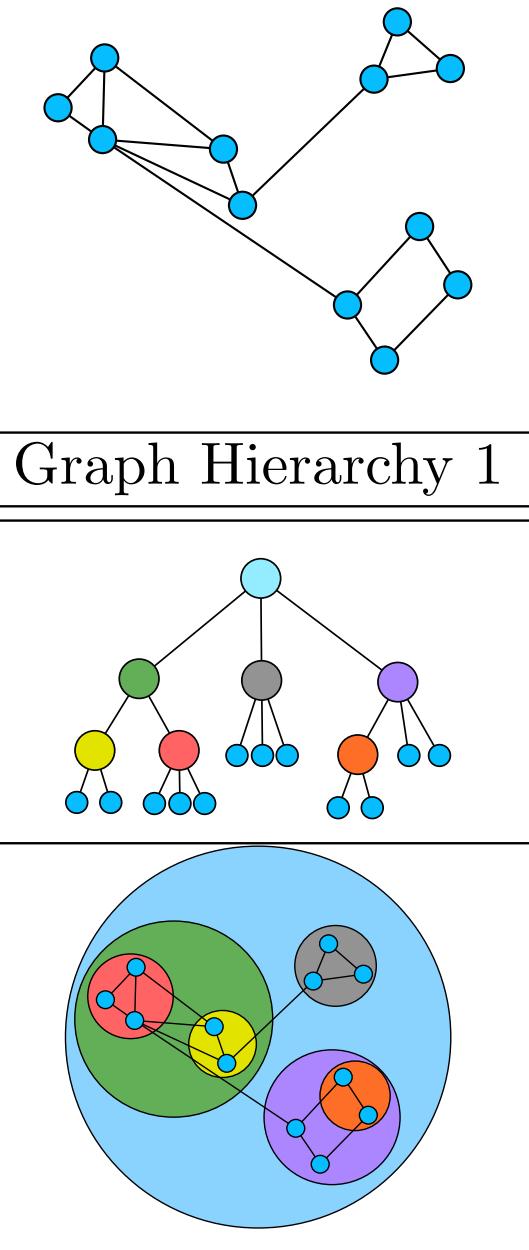


[Schulz 2004]



# Idiom: GrouseFlocks

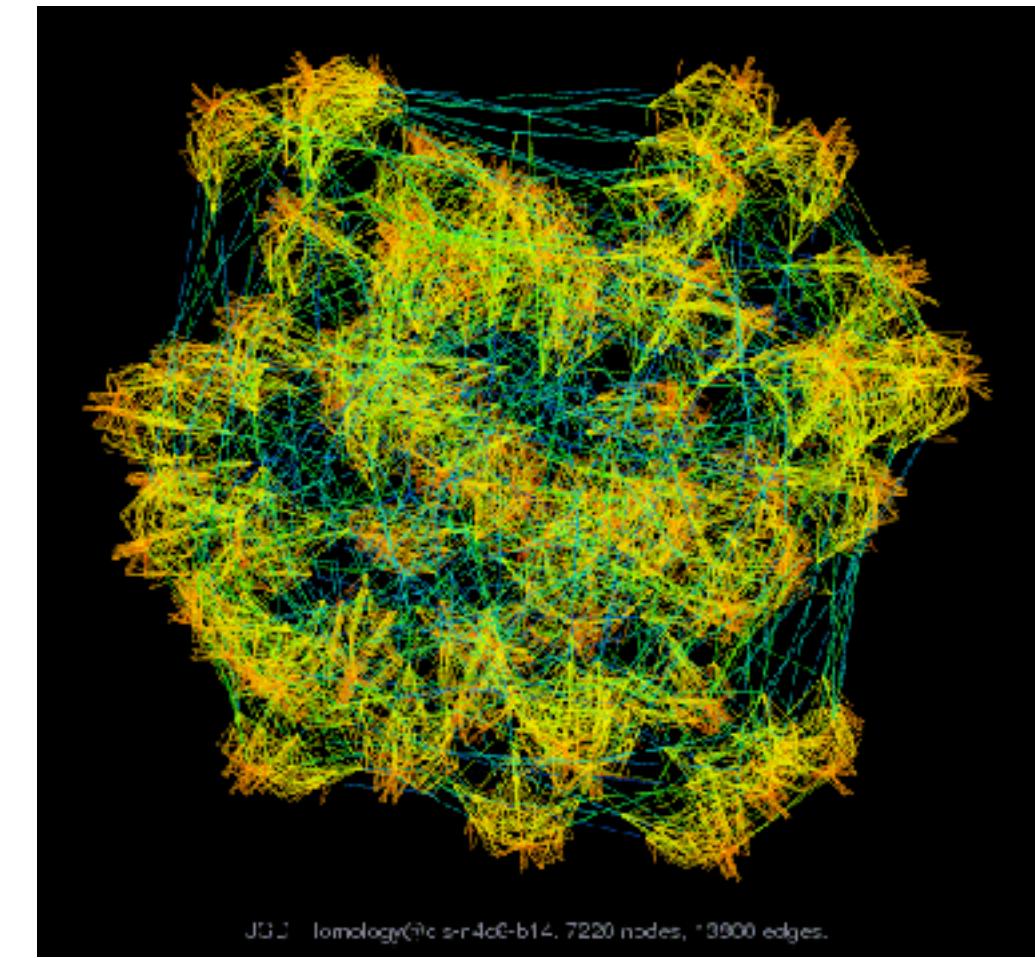
- data: compound network
  - network
  - cluster hierarchy atop it
    - derived or interactively chosen
- visual encoding
  - connection marks for network links
  - containment marks for hierarchy
  - point marks for nodes
- dynamic interaction
  - select individual metanodes in hierarchy to expand/contract



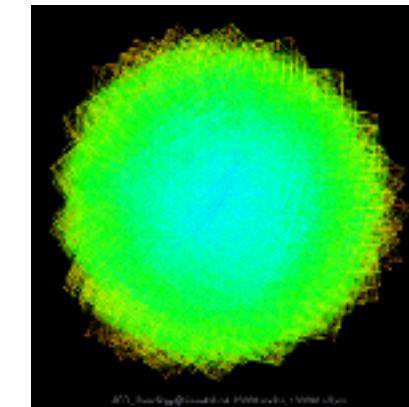
[*GrouseFlocks: Steerable Exploration of Graph Hierarchy Space*. Archambault, Munzner, and Auber. IEEE TVCG 14(4):900-913, 2008.]

# Idiom: **sfdp** (multi-level force-directed placement)

- data: compound graph
  - original: network
  - derived: cluster hierarchy atop it
- considerations
  - better algorithm for same encoding technique
    - same: fundamental use of space
    - hierarchy used for algorithm speed/quality but not shown explicitly
- scalability
  - nodes, edges: 1K-10K
  - hairball problem eventually hits

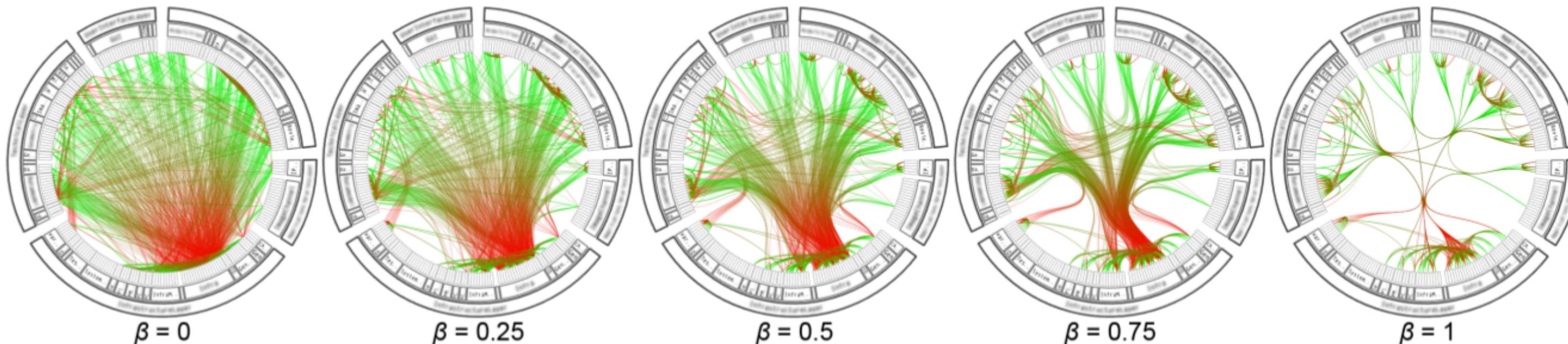


[Efficient and high quality force-directed graph drawing.  
Hu. *The Mathematica Journal* 10:37–71, 2005.]



# Idiom: hierarchical edge bundling

- data
  - any layout of compound network
    - network: software classes (nodes), import/export between classes (links)
    - cluster hierarchy: class package structure
  - derived: bundles of edges with same source/destination (multi-level)
- idiom: curve edge routes according to bundles
- task: edge clutter reduction



# Hierarchical edge bundling

- works for any layout: treemap vs radial

